



***GDR MEETICC Conférence plénière 2023***  
*Latresne - Bordeaux, 30 mai- 2 juin 2023*

# Phase transitions and spin dynamics of the quasi-1D Ising-like antiferromagnet $\text{BaCo}_2\text{V}_2\text{O}_8$ in a longitudinal magnetic field

**Béatrice GRENIER**

Univ. Grenoble Alpes & CEA-IRIG-MEM  
Grenoble, France

# Introduction on XXZ 1D spin $\frac{1}{2}$ antiferromagnets

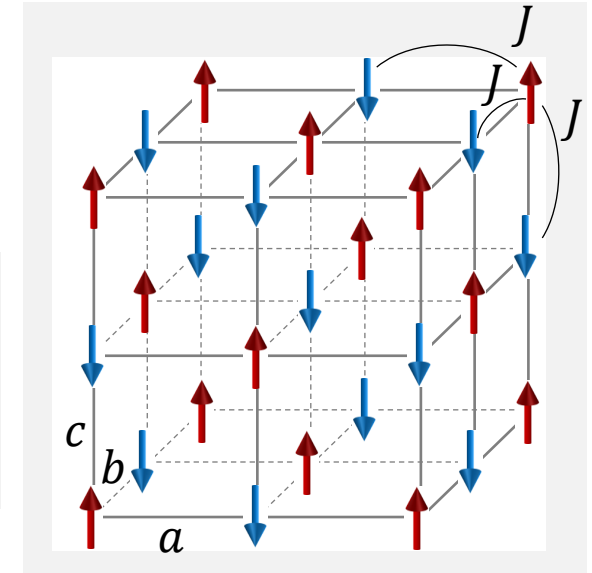
# Introduction: Classical 3D vs quantum 1D spin 1/2 antiferromagnets

$$\mathcal{H} = J \sum_i \vec{S}_i \cdot \vec{S}_{i+1}$$

Conventional Heisenberg 3D antiferromagnet

isotropic spins

$J > 0$

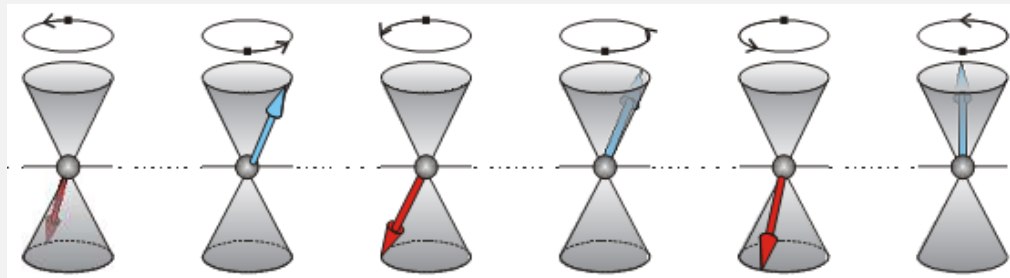


- **Ground state: AF (Néel) ordering** below  $T_N \sim J$

Example: cubic AF  $\rightarrow$  same  $J$  along the 3 directions of space  $\rightarrow \vec{k} = \left(\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right)$

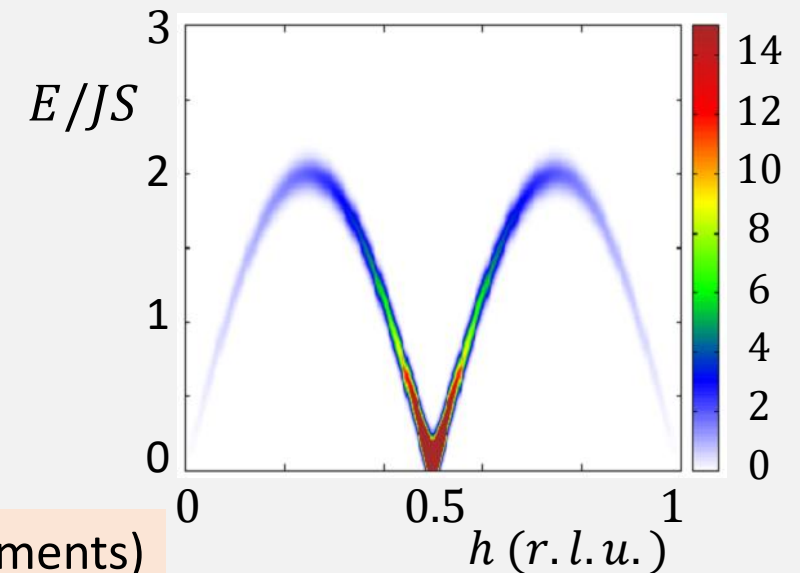
- **Excitations: spin waves / magnons**

(precession of the spin around its equilibrium position)



$$E(k) = 2JS|\sin(ka)|$$

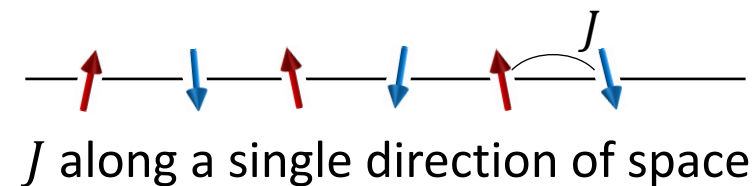
$\rightarrow$  **transverse excitation** (fluctuations  $\perp$  ordered magnetic moments)



# Introduction: *Classical 3D vs quantum 1D spin 1/2 antiferromagnets*

$$\mathcal{H} = J \sum_i \vec{S}_i \cdot \vec{S}_{i+1}$$

Quantum Heisenberg 1D antiferromagnet



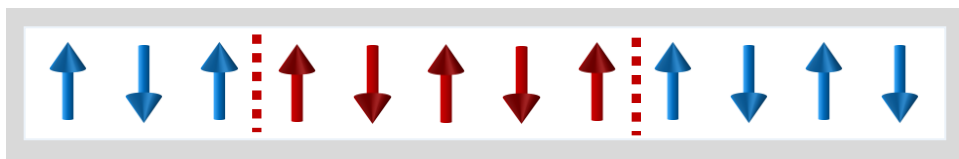
Quantum fluctuations  $\Rightarrow$  exotic static and dynamical properties

- **Ground state: Tomonaga-Luttinger Liquid (TLL)**

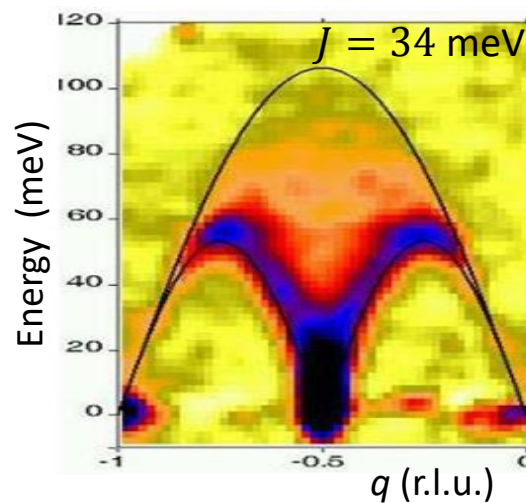
No magnetic LRO down to  $T = 0$

- **Excitations: Ungapped 2-spinons continuum**

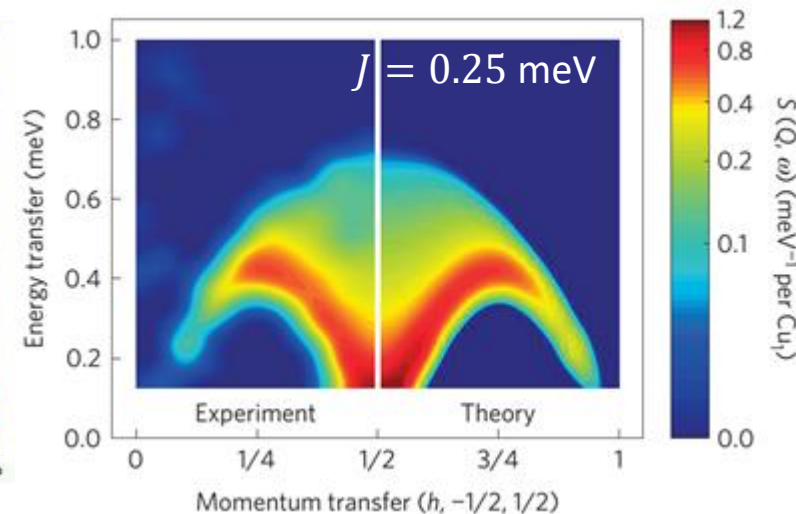
(= "domain walls")



Bethe, Z. Phys. (1931); Haldane, PRL (1983)



KCuF3  
Nagler *et al.*, PRB (1991)



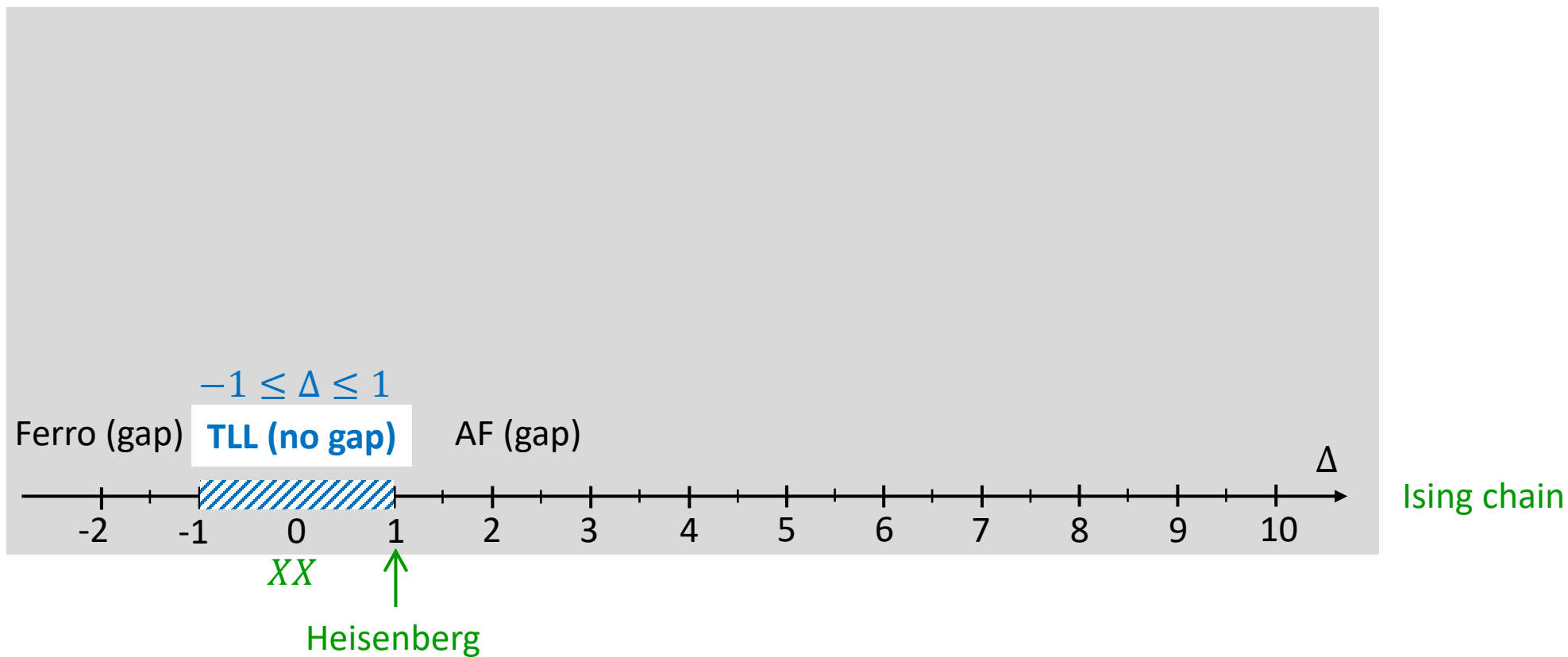
CuSO4·5D2O  
Mourigal *et al.*, Nat. Phys. (2013)

# Introduction: $XXZ$ antiferromagnetic spin 1/2 chains

$$\mathcal{H}_{XXZ} = J \sum_i (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y + \Delta S_i^z S_{i+1}^z)$$

anisotropy parameter

$\Delta = 1$ :	Heisenberg	
$0 < \Delta < 1$ :	$XX$ -like	( $\Delta = 0$ : pure $XX$ )
$\Delta > 1$ :	Ising-like	( $\Delta \rightarrow +\infty$ : pure Ising)



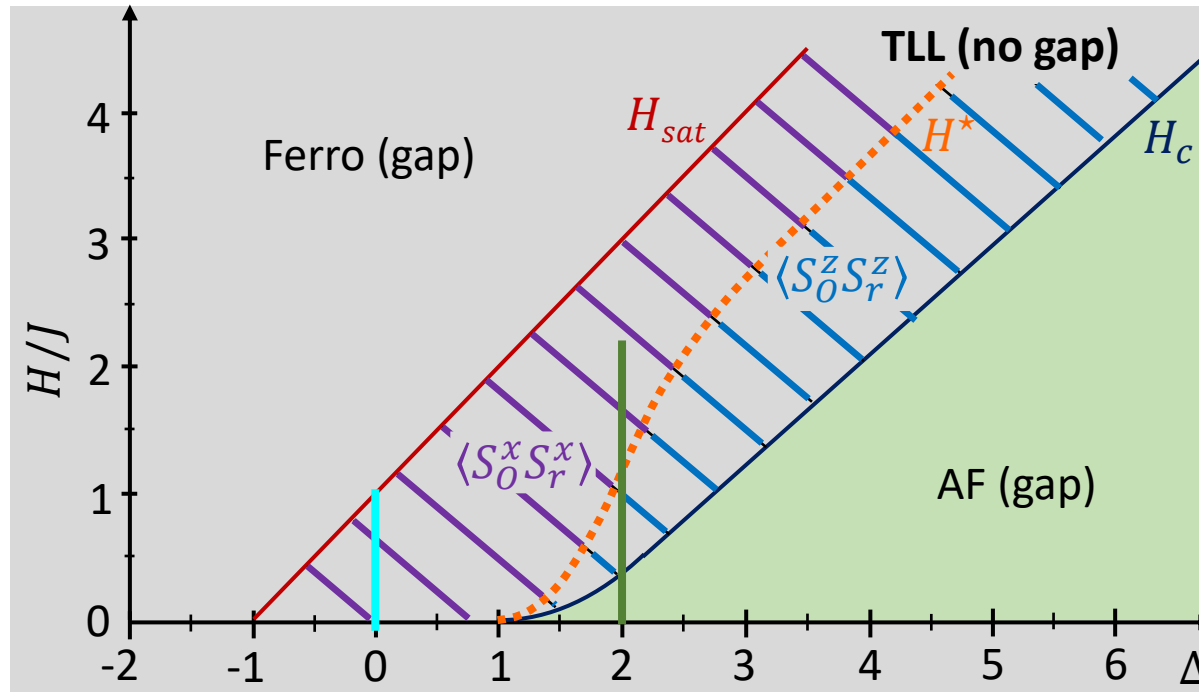
# Introduction: $XXZ$ antiferromagnetic spin 1/2 chains

$$\mathcal{H}_{XXZ} = J \sum_i (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y + \Delta S_i^z S_{i+1}^z)$$

$XXZ$  AF  $S = 1/2$  chain  
in a magnetic field  $H \parallel z$

$$\mathcal{H} = \mathcal{H}_{XXZ} - H \sum_i S_i^z$$

S. Wessel and S. Haas,  
PRB (2000)



$\langle S_0^x S_r^x \rangle$ :  
**Commensurate**  
**Transverse AF correlations**

$\langle S_0^z S_r^z \rangle$ :  
**Incommensurate**  
**longitudinal AF correlations**  
incommensurability increases  
with increasing the field

$\langle S_0^z S_r^z \rangle$ :  
**Commensurate**  
**Longitudinal AF correlations**

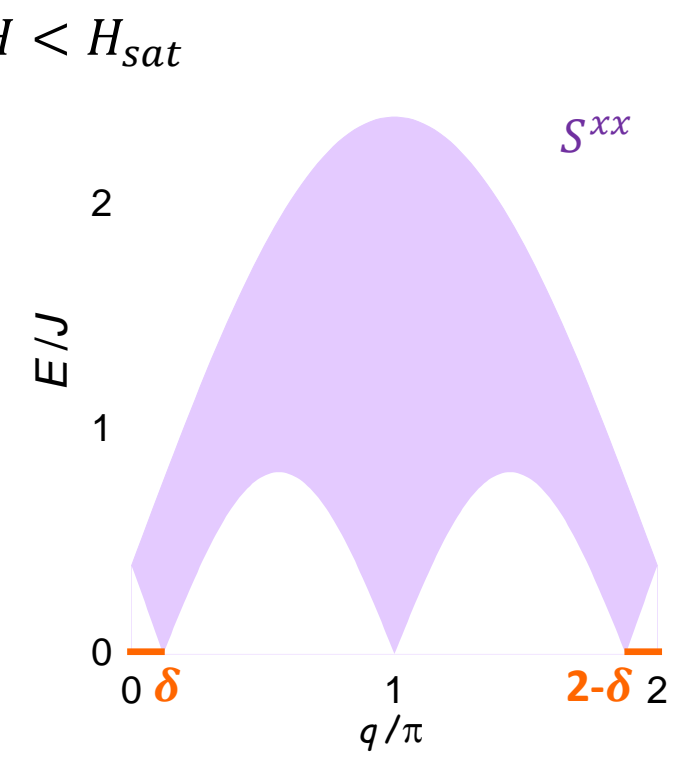
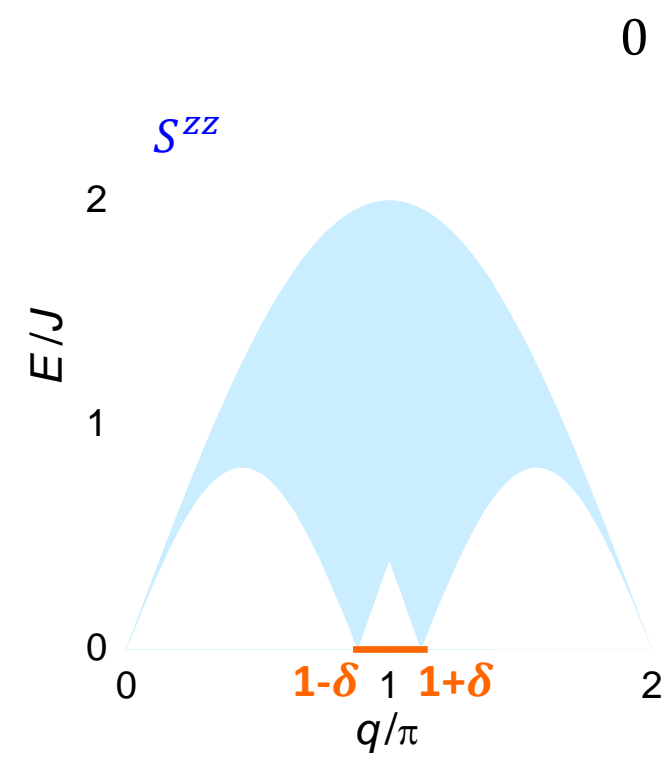
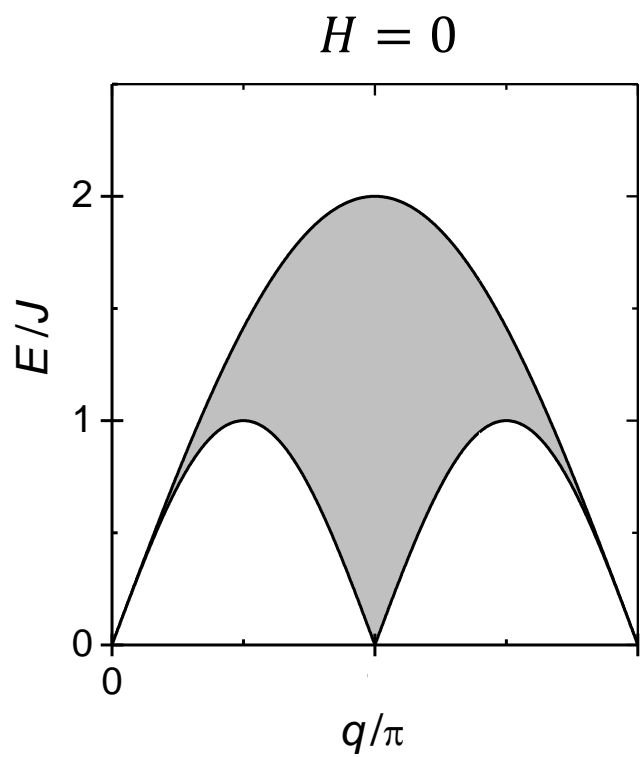
**Experimental realizations:**

$\Delta = 1$ : most of the systems (KCuF<sub>3</sub>, CuSO<sub>4</sub>·5D<sub>2</sub>O, CuPzN ...)

$\Delta = 10$ : CsCoX<sub>3</sub> (X=Br, Cl) extensively studied in 70's and 80's  $\rightarrow H_c \simeq 75$  T

**$\Delta = 2$ : BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>** Kimura *et al.*, PRL (2008)  $\rightarrow H_c \simeq 4$  T  $\rightarrow$  easily reachable with neutron scattering experiments

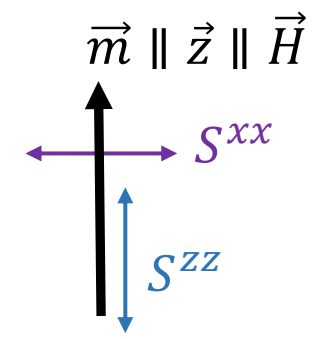
# Introduction: Heisenberg antiferromagnetic spin 1/2 chains



$H = 0$ : ungapped two-spinon continuum  $\Leftrightarrow$  TLL spin-dynamics

$\vec{H} \parallel \vec{z}$  (TLL phase:  $0 < H < H_{sat}$ ): Incommensurability  $\delta$  develops with  $\delta = 2\pi \langle S^z \rangle \propto H$

- Around  $q = \pi$  for longitudinal  $S^{zz}$  fluctuations
- Around  $q = 0$  and  $2\pi$  for transverse  $S^{xx}$  fluctuations



G. Müller, PRB (1981)

## Introduction on $\text{BaCo}_2\text{V}_2\text{O}_8$

- crystallographic structure
- magnetic structures in a longitudinal field
- zero-field magnetic excitations

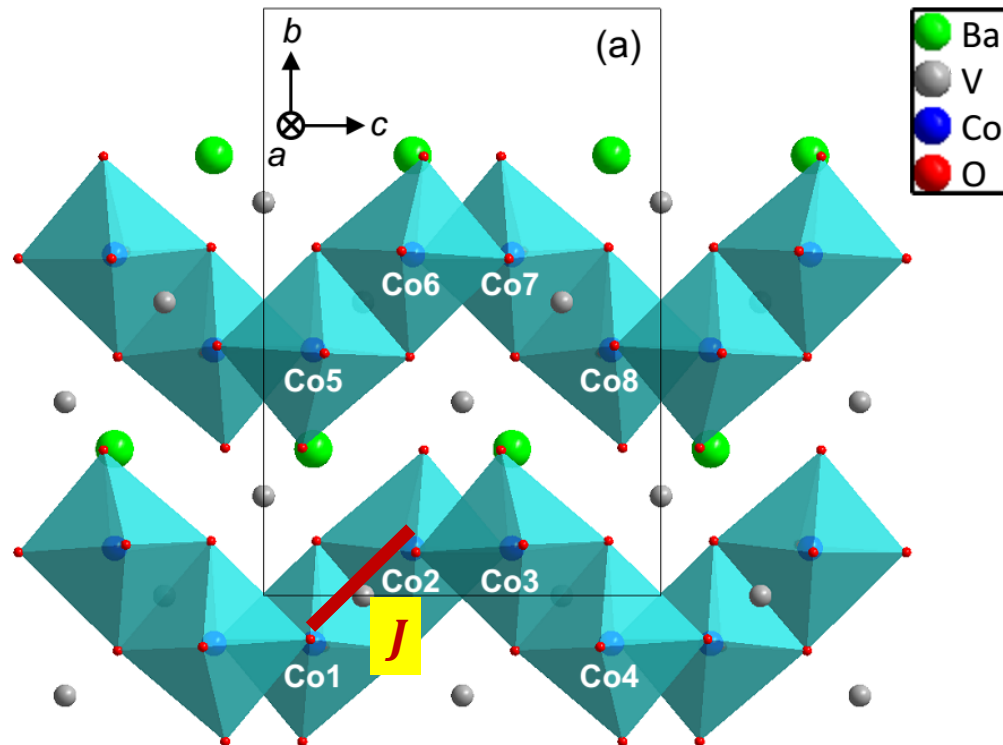


# BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>: Crystallographic structure

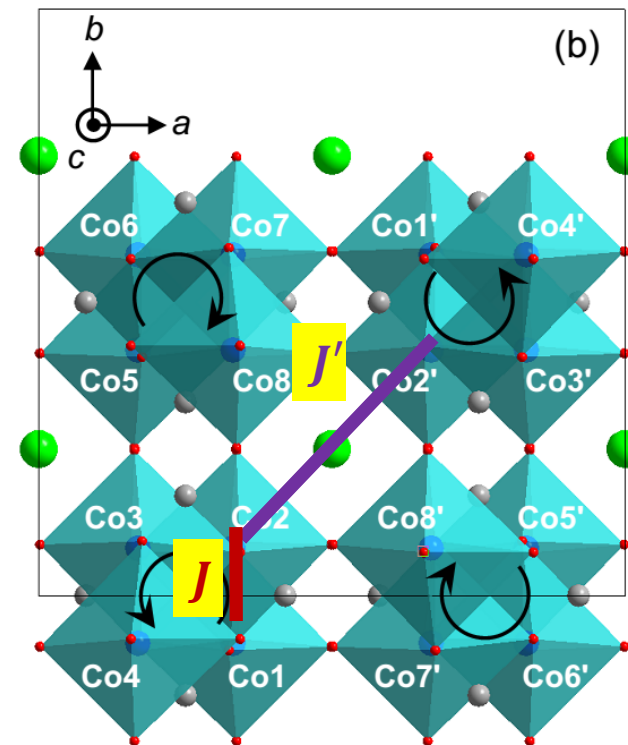
- Screw chains of effective spin 1/2 || *c*-axis (tetragonal space group)
- Ising-like AF 1D model with  $\Delta \sim 2$ ; Easy-axis  $z = c$  chain axis ( $J_z \sim 2J_x \sim 2J_y$ )  
S. Kimura *et al.*, J. Phys.: Conf. Series (2006) & JPSJ (2013)
- Non-negligible inter-chain interactions (quasi-1D)  
→ AF LRO at  $T < 5.6$  K

XXZ Hamiltonian

$$\mathcal{H}_{XXZ} = J \sum_i (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y + \Delta S_i^z S_{i+1}^z)$$



Intrachain interaction:  $J$  AF



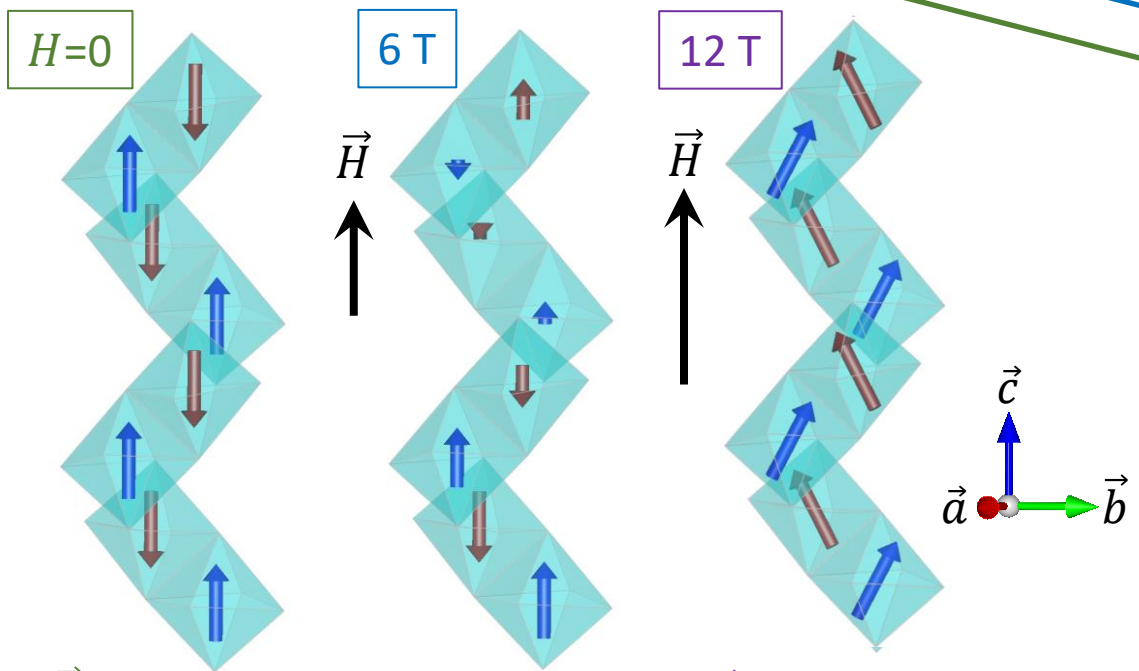
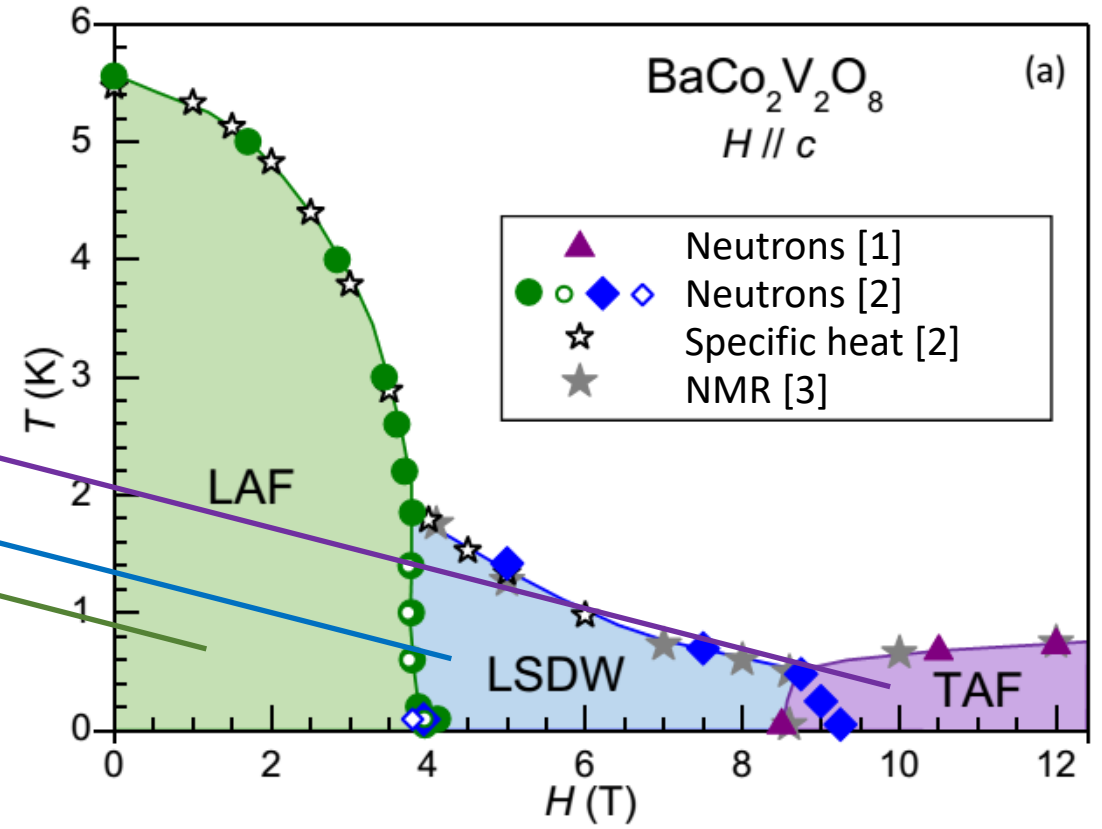
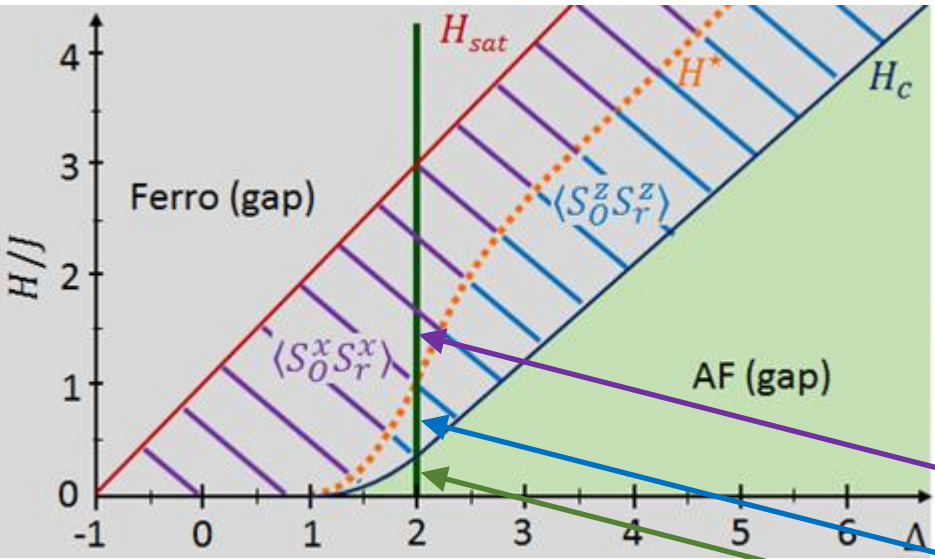
Relevant interchain interaction:  $J'$  diagonal, AF

$$\begin{aligned} x &\equiv a \\ y &\equiv b \\ z &\equiv c \end{aligned}$$

$$J' \ll J$$

# BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>: Magnetic structures for $H \parallel c$

Single crystal diffraction on D23 @ ILL



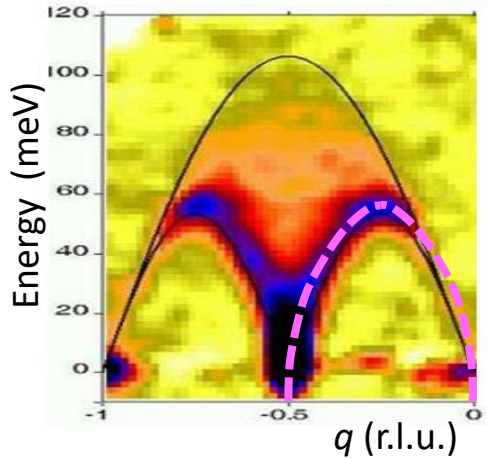
$\vec{k}_{AF} = (1,0,0)$   $\vec{k}_{LSDW} = (1,0,\delta)$   $\vec{k}_{AF} = (1,0,0)$

**LAF:** Longitudinal AF ( $\vec{m}_{AF} \parallel \vec{c}$ )  
**LSDW:** Longitudinal Spin Density Wave ( $\vec{m}_{IC} \parallel \vec{c}$ )  
**TAF:** canted Transverse AF ( $\vec{m}_{AF} \parallel \vec{a}$ )

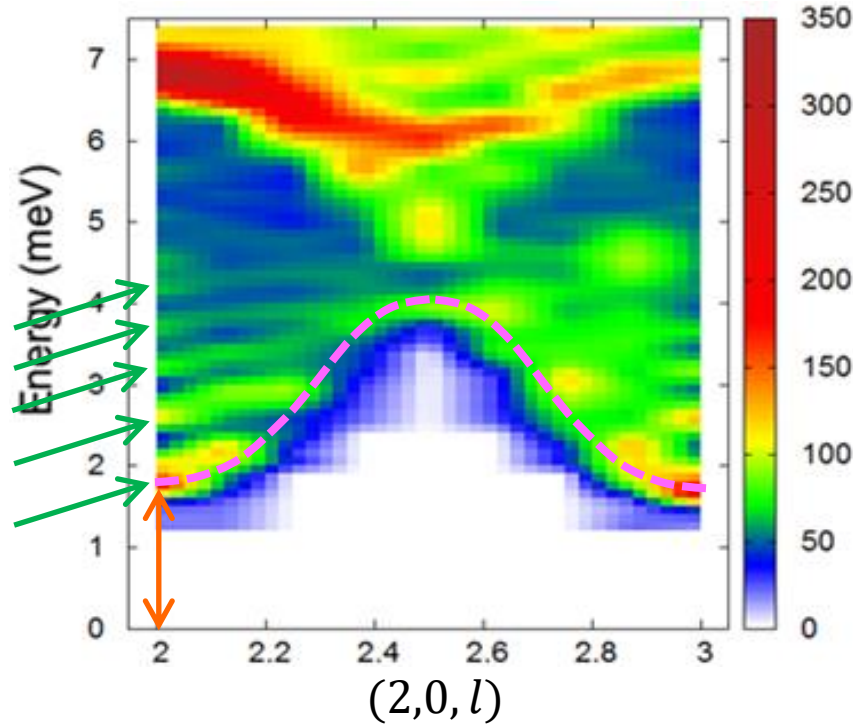
[1] B. Grenier *et al.*, PRB (2015); [2] E. Canévet *et al.*, PRB (2013);  
 [3] M. Klanjšek *et al.*, PRB (2015)

# BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>: Zero-field spinon excitations

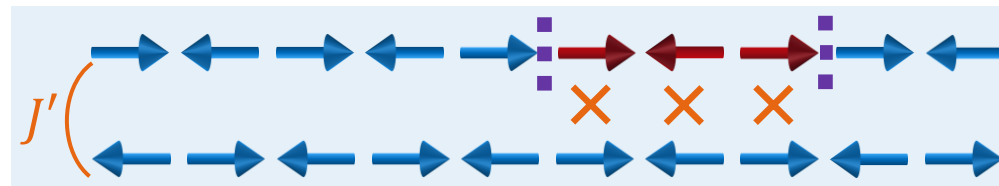
- Heisenberg 1D AF KCuF<sub>3</sub>:  
Deconfined spinons



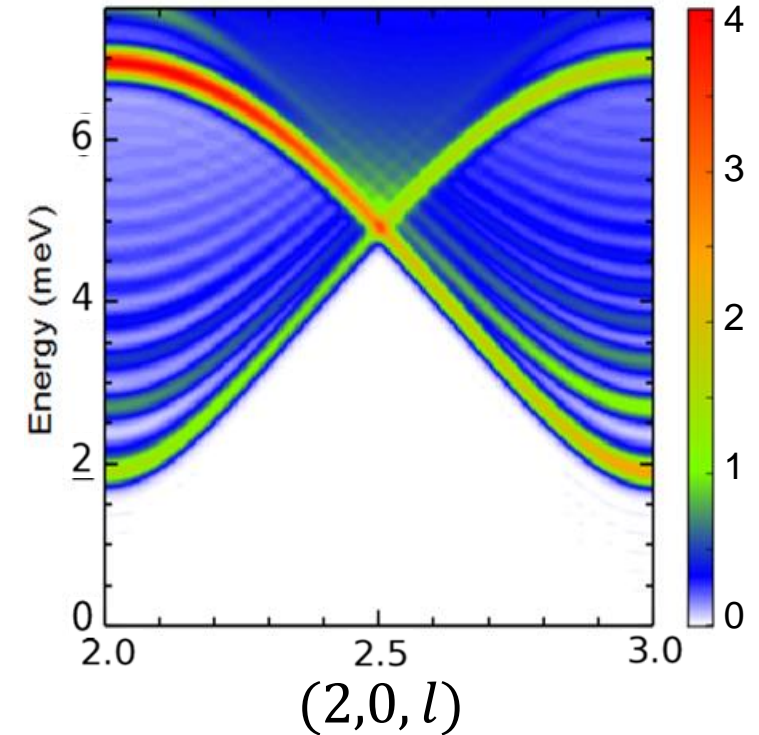
- Ising-like quasi-1D AF BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>  
Inelastic neutron scattering on IN12 @ ILL



Gap ← Ising-like anisotropy  
Discretization ← Confined spinons ←  $J'$



Numerics: TEBD + mean field  
(S. Takayoshi and T. Giamarchi)



$$J = 5.8 \text{ meV}, \Delta = 1.89, J' = 0.17 \text{ meV}$$

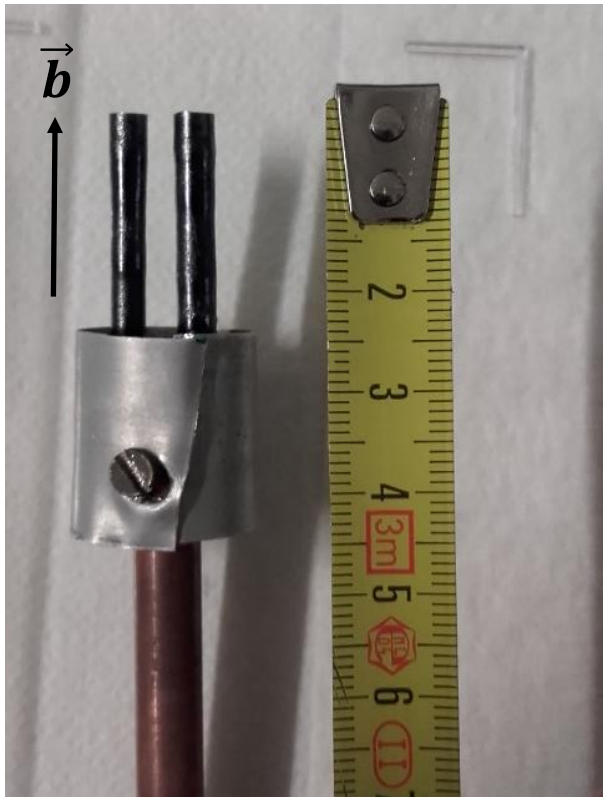
B. Grenier *et al.*,  
PRL (2015)

Q. Faure, S. Takayoshi *et al.*,  
Nature Physics (2018)

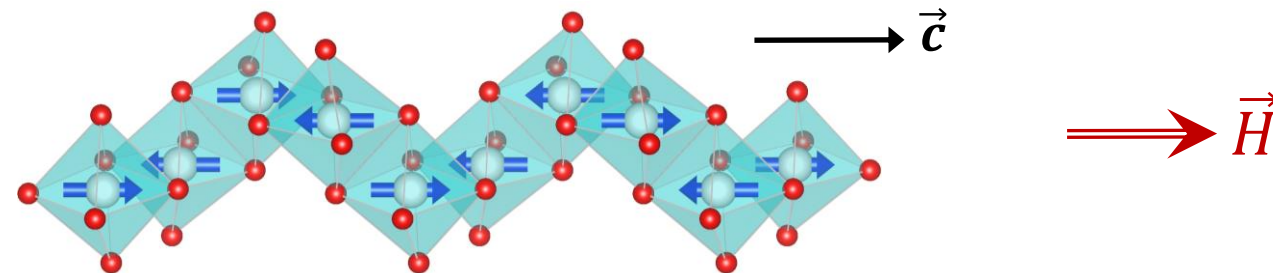
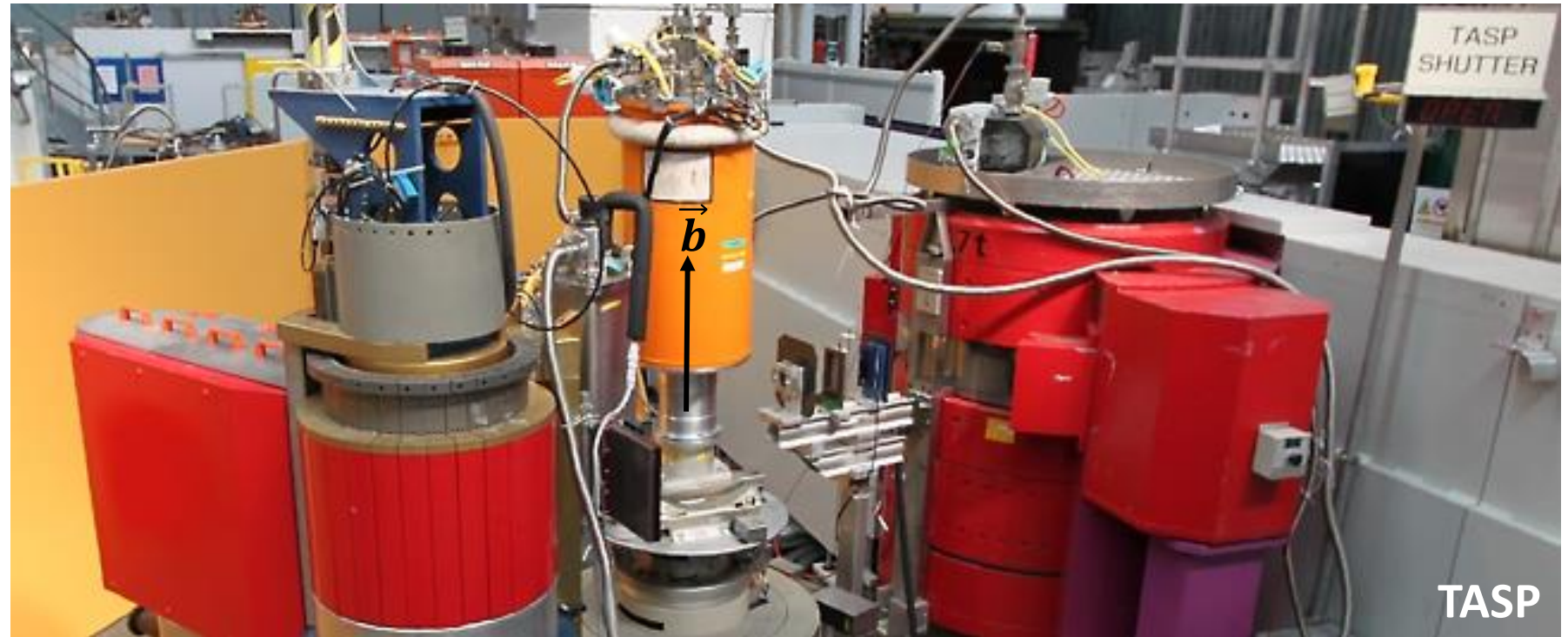
## Spin dynamics of $\text{BaCo}_2\text{V}_2\text{O}_8$ in a longitudinal field

- 1- in the LSDW phase (up to 6.8 T, on TASP)
- 2- across LSDW – TAF phase transition (up to 10 T, on IN5)

2 co-aligned single-crystals  
with  $\vec{c}$  horizontal

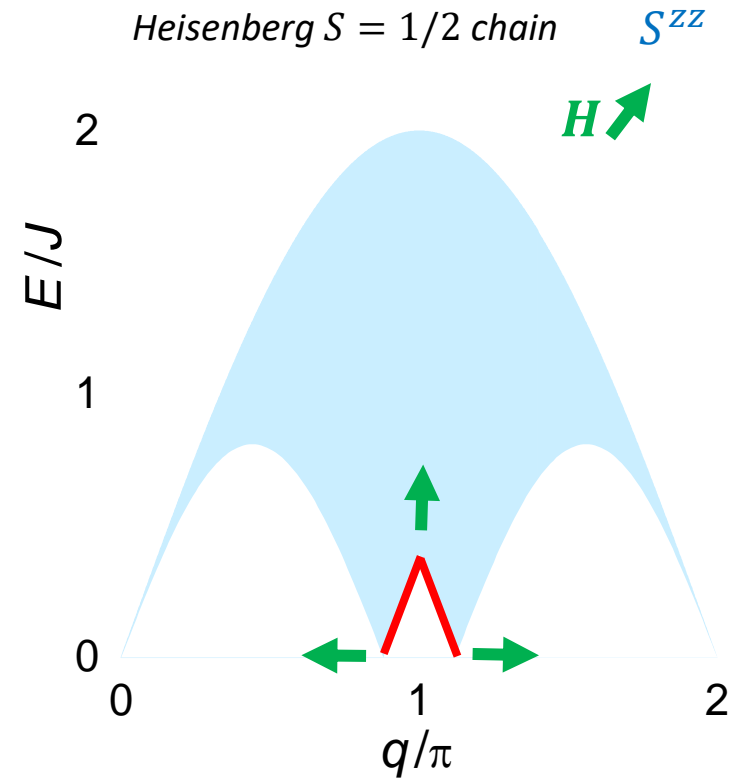
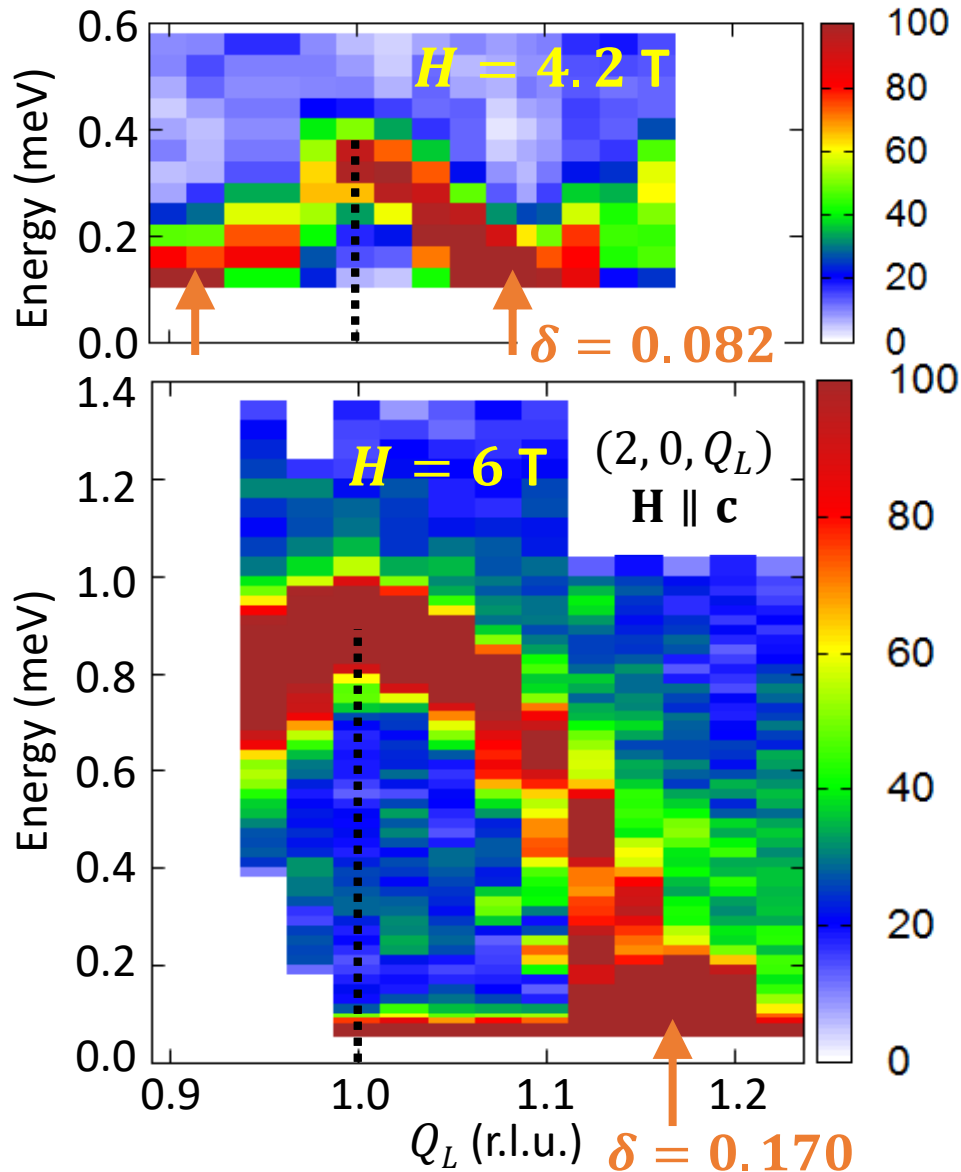


Three-axis spectrometer **TASP** @ PSI, Villigen (Switzerland)  
with **6.8 T horizontal cryomagnet** + dilution



Q. Faure, S. Takayoshi *et al.*,  
PRL 2019

• **INS intensity maps** around the AF position  $Q = (2,0,1)$ : **field dependence**

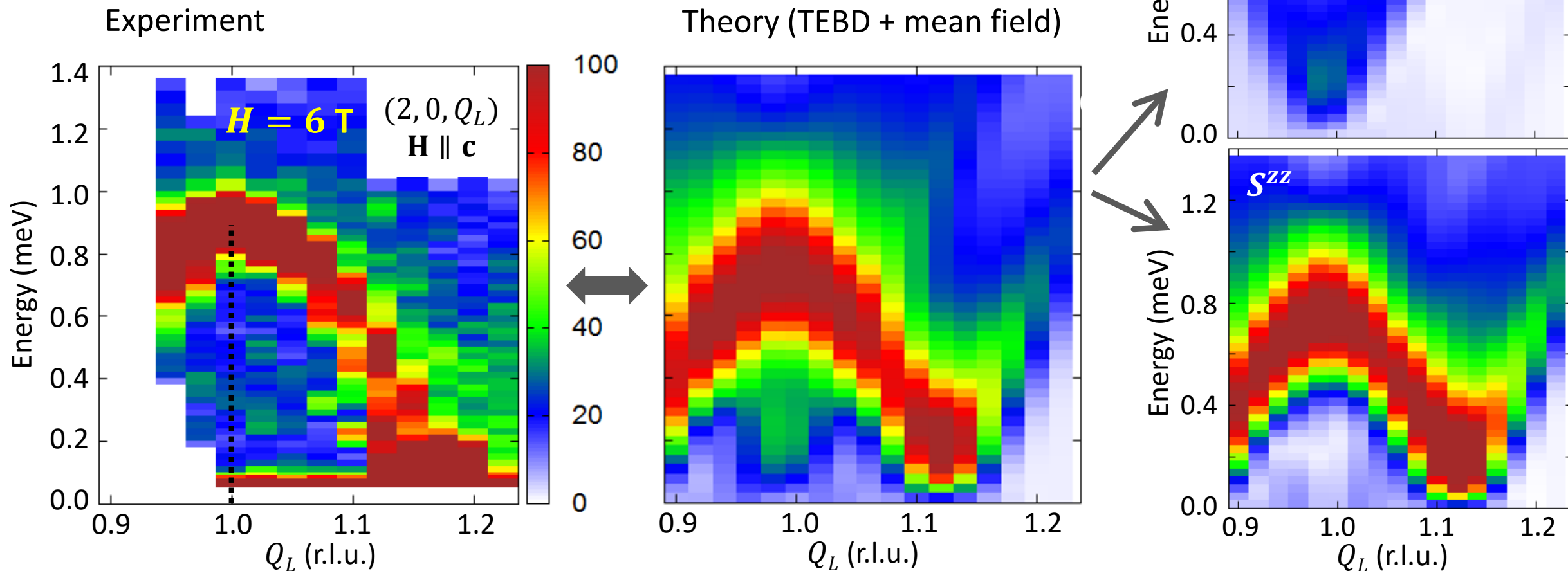


**Minima of energy** at the IC positions  $Q_L = 1 \pm \delta$   
(and local maximum at  $Q_L = 1$ )

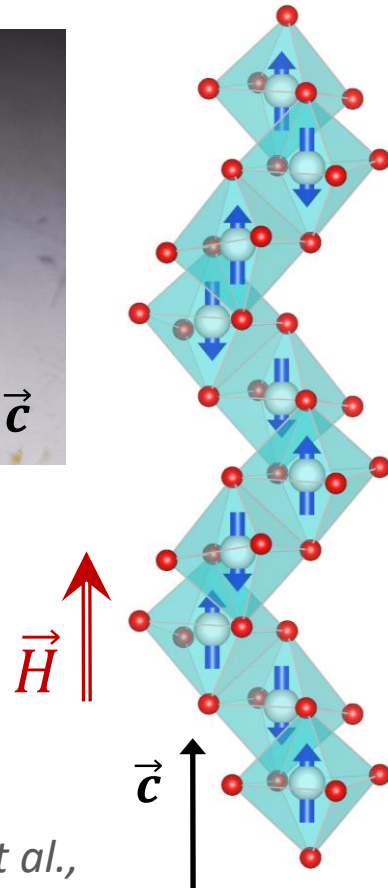
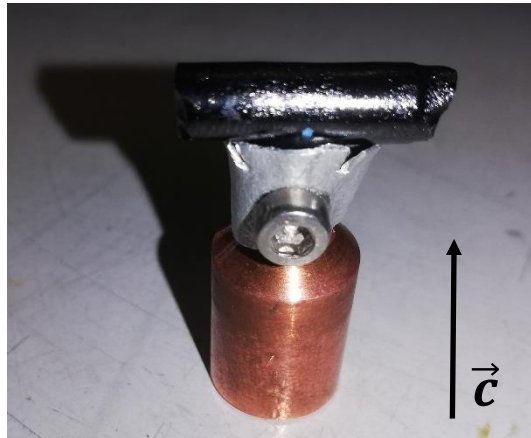
$\delta$  increases when  $H$  increases  
 $\Rightarrow$  **the maximum of energy** at  $Q_L = 1$  also increases

- INS intensity maps around the AF position  $Q = (2,0,1)$ :  
Comparison experiment/theory

→ the longitudinal fluctuations  $S^{zz}$  are the dominant ones



1 single-crystal  
with  $\vec{c}$  vertical



Time-Of-Flight spectrometer **IN5** @ ILL, Grenoble  
with **vertical 10 T cryomagnet + dilution**

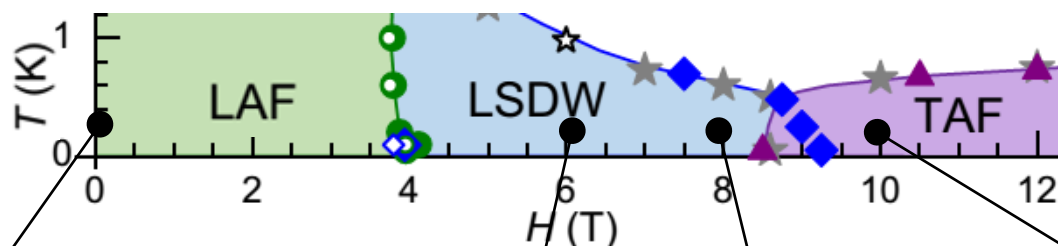
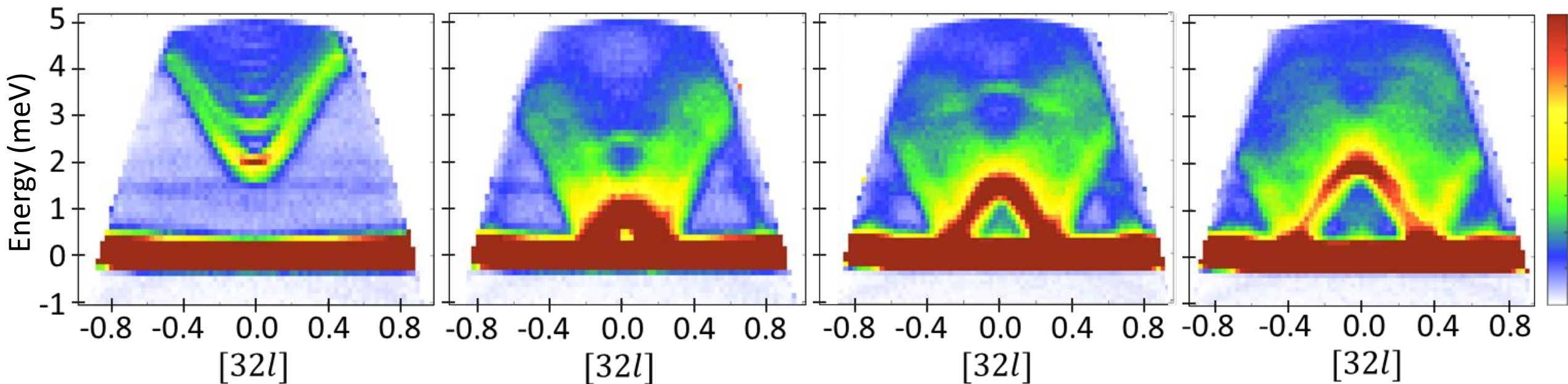


S. Takayoshi, Q. Faure *et al.*,  
arXiv:2302.03833v1,  
to appear in PRR

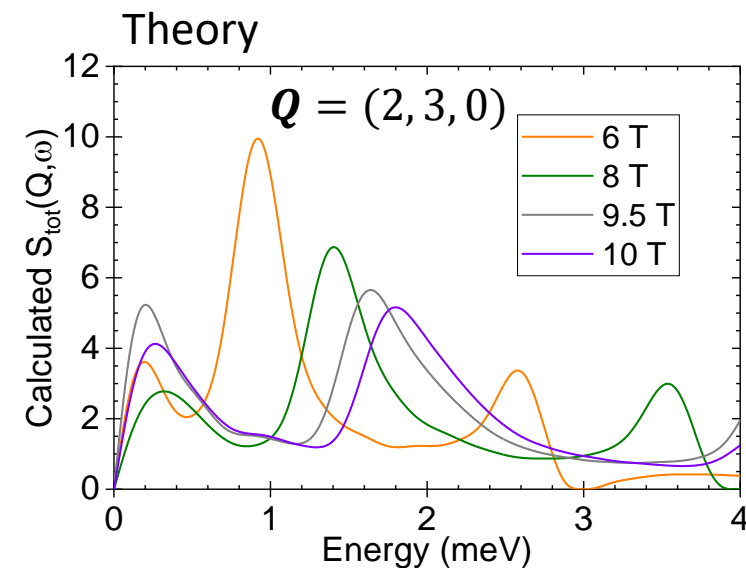
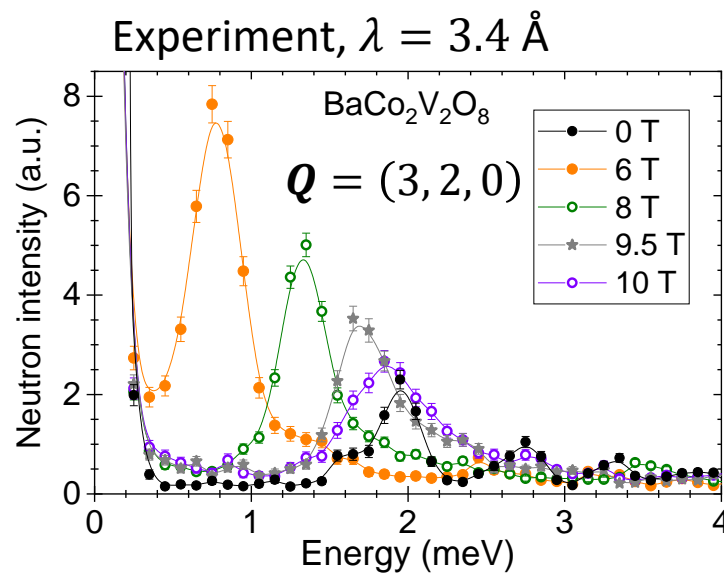
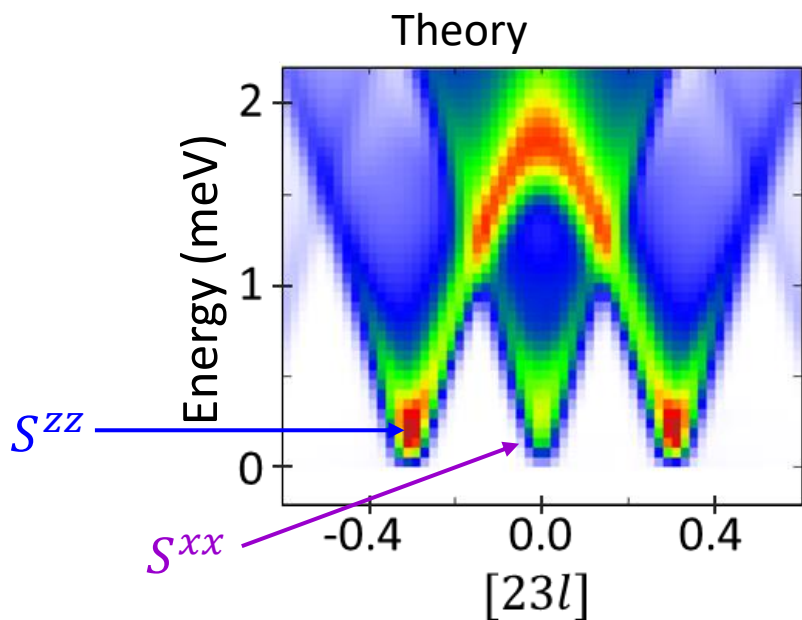
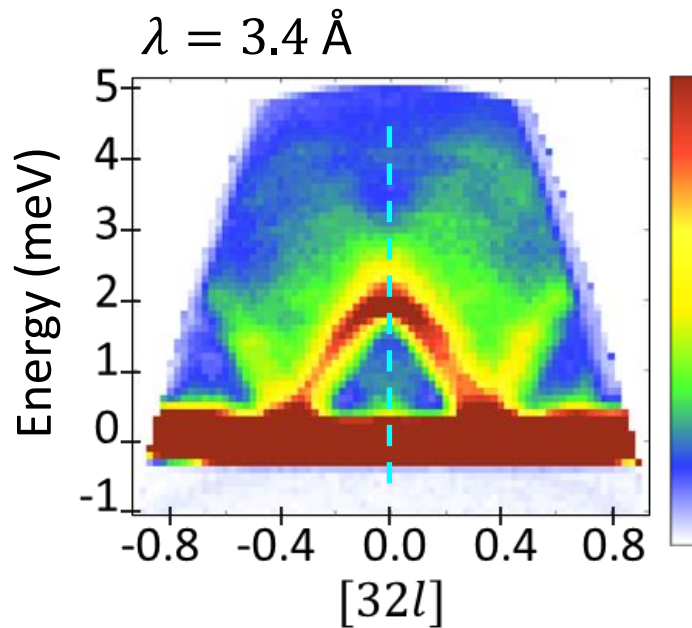
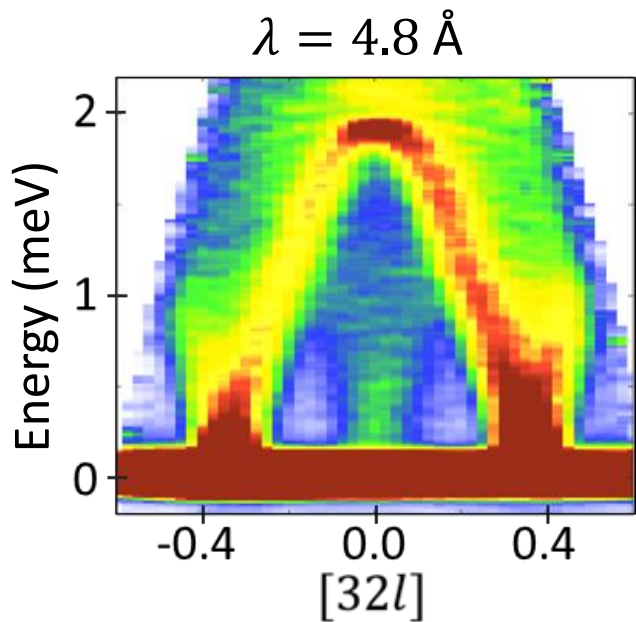


$$\lambda = 3.4 \text{ \AA}$$

$$T = 50 \text{ mK}$$

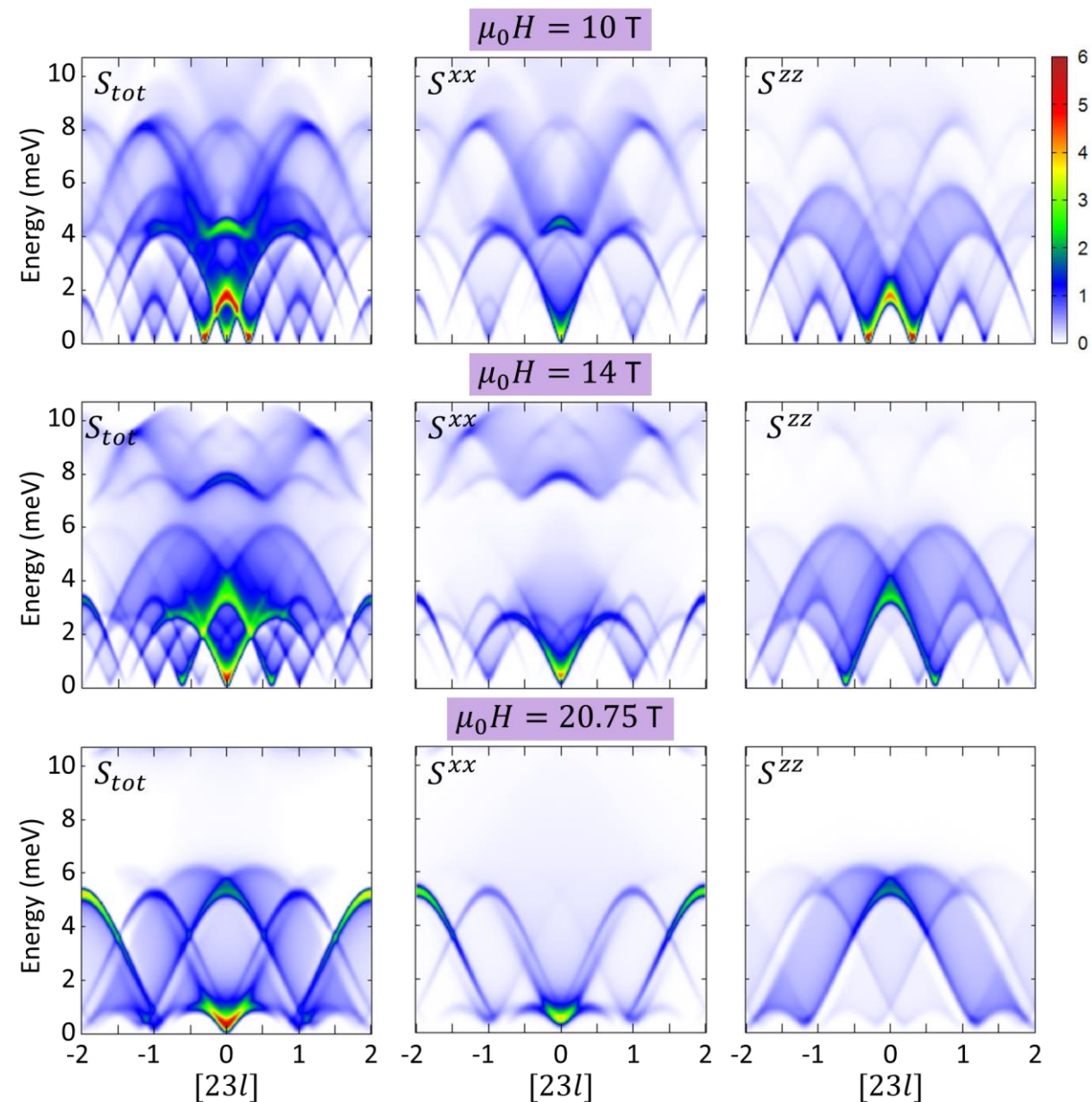
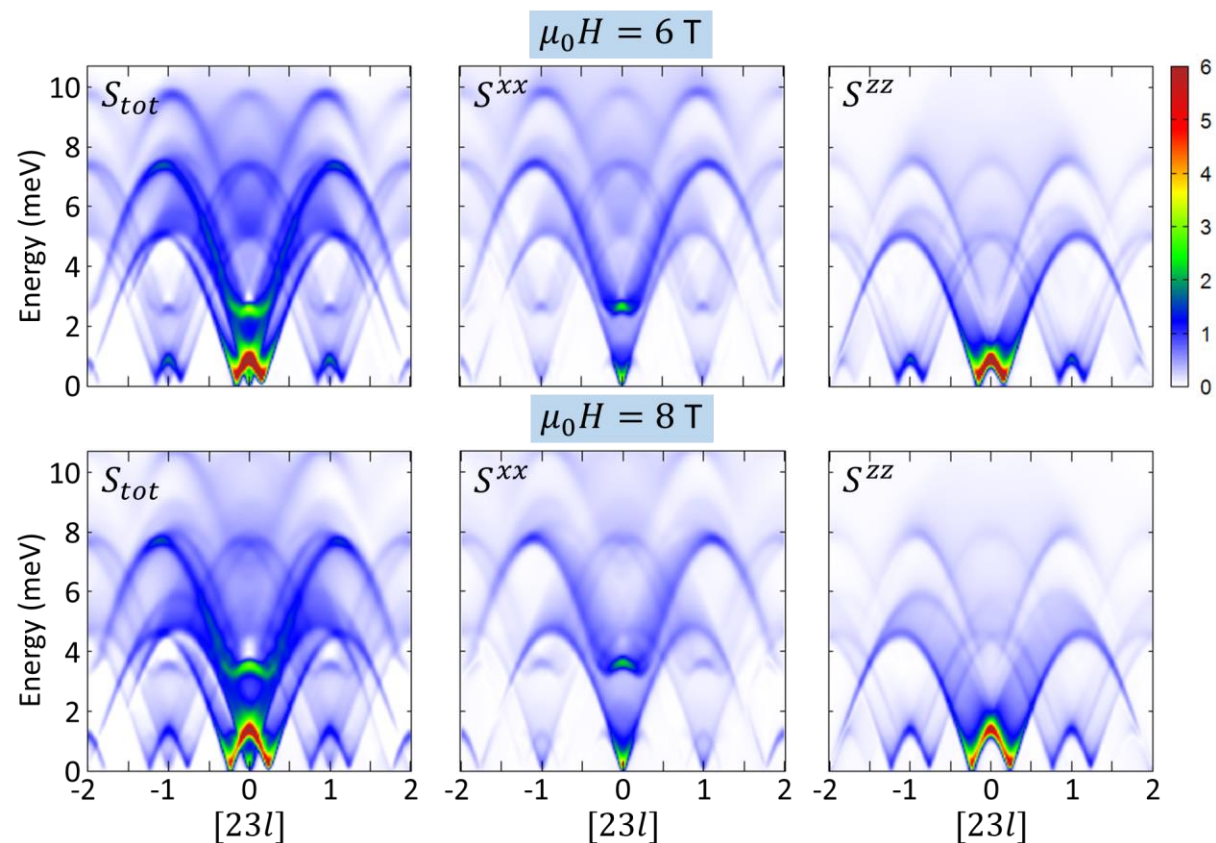

 $\mu_0 H = 0$ 
 $\mu_0 H = 6 \text{ T}$ 
 $\mu_0 H = 8 \text{ T}$ 
 $\mu_0 H = 10 \text{ T}$ 


$\mu_0 H = 10$  T  
 $T = 50$  mK



## TEBD calculations in the LSDW and TAF phases

(S. Takayoshi and T. Giamarchi)



# Conclusion

**BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub> in a longitudinal field ( $H \parallel c$ ):**

**Quantum phase transition** from Néel to LSDW phase described by the **XXZ model**

Clear **Tomonaga-Luttinger liquid** (TLL) signatures are observed in both the LSDW and TAF phases.

- Incommensurate dynamics in both phases, with a dominance of the longitudinal excitations:
  - in the LSDW phase
  - and in the low-field region of the TAF phase
- At higher field, the transverse excitations dominate

**Fingerprint of TLL quantum dynamics in Ising-like chain** observed for the first time

Shintaro Takayoshi, Quentin Faure, Virginie Simonet, Béatrice Grenier, Sylvain Petit, Jacques Ollivier, Pascal Lejay, Thierry Giamarchi  
arXiv:2302.03833v1, to appear in PRR

# Acknowledgments

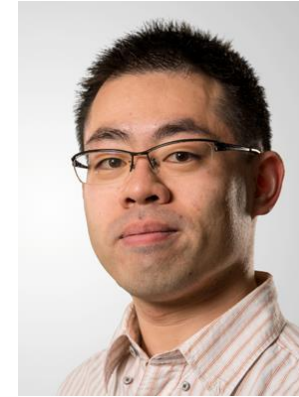


**Quentin FAURE**

(Ph-D 2015-2018)

UGA, CEA-IRIG & Inst. Néel,  
Grenoble, France

*now at LLB, CEA-Saclay*



**Shintaro TAKAYOSHI**

(Post-doc 2017-2019)

DQMP, Univ. Geneva,  
Geneva, Switzerland

*now at Konan univ., Kobe, Japan*



**Sylvain PETIT**

**Virginie SIMONET**

**Pascal LEJAY**

**Stéphane RAYMOND, Louis-Pierre REGNAULT**

**Jacques OLLIVIER**

**Christian RÜEGG, Martin MÅNSSON**

**Gregory S. TUCKER, Jonathan S. WHITE**

**Thierry GIAMARCHI**

LLB, CEA – Saclay, France

Institut Néel, Grenoble, France

Institut Néel, Grenoble, France

CEA-IRIG, Grenoble, France

ILL, Grenoble, France

PSI, Villigen, Switzerland

DQMP, Univ. Geneva, Switzerland



**Thank you for your attention**