

Réunion Plénière du GDR, Lastresne 2023

Spin triplet superconductivity in bulk strongly correlated materials.

J.P. Brison

Collaborations between:

Univ. Grenoble Alpes:

Pheliqs/MEM-CEA

LNCMI-CNRS

Institut Néel-CNRS

IMR-Toku university



Interplay with ... all electronic instabilities ?

- Magnetism (all SCES families ?) [Erik Linnér](#)
- Charge order (NbSe₂, Cuprates, Nickelates) [Alvaro Adrian Carrasco Alvarez](#)
- *Nematicity (iron pnictides)*
- *Multipolar ordering (URu₂Si₂, PrOs₄Sb₁₂)*
- Topological properties (band structure) [Valentin Taufour](#)

Between Fields:

- “Nano-physics”:
 - *Phase manipulation (meso phys. – quantum engineering)*
 - Current manipulation (non reciprocal superconductivity) [Shamashis Sengupta](#)
 - Thin films / surface spectroscopies [Florent Condaminas](#)
 - *Topological properties (Majorana modes)*
- Solid-State Chemistry (novel/high quality materials !) [Araceli Gutiérrez Llorente](#), [Alain Demourgues](#)

Outline: spin-triplet superconductivity

1. Superconducting state in FM-SC

- Spin-triplet superconductivity
- Effect of transverse fields
- Field dependence of the pairing

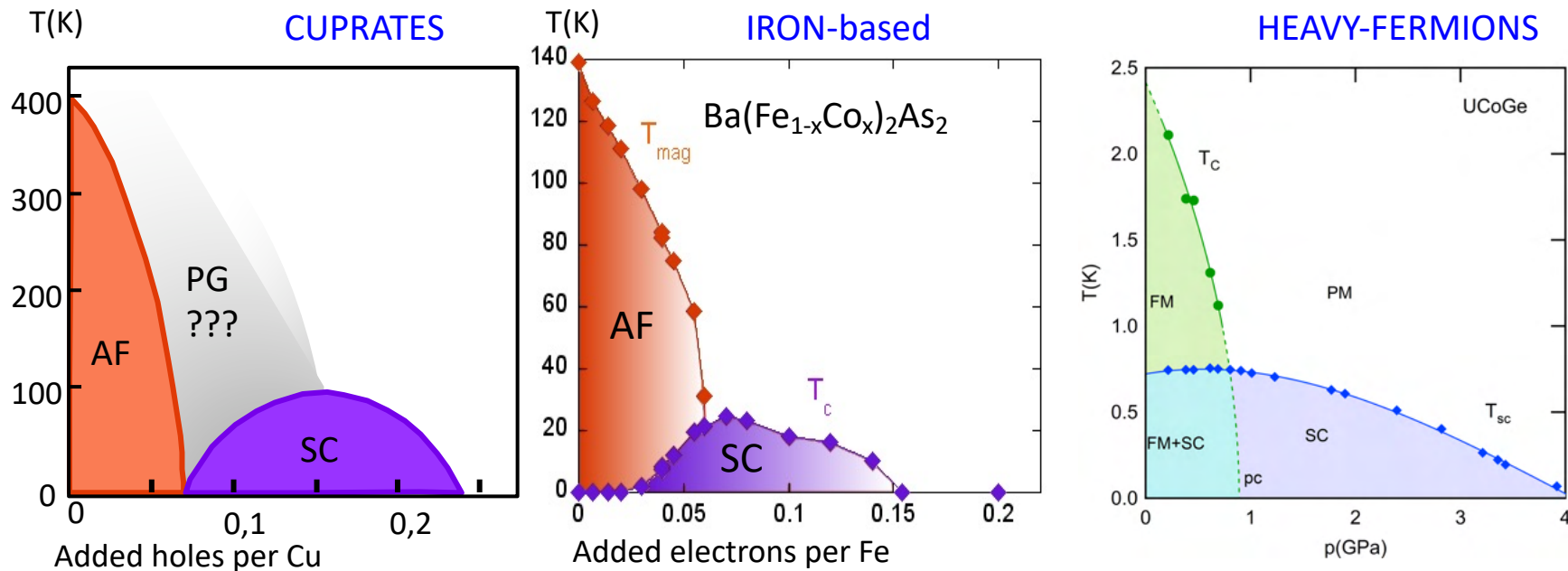
2. UTe₂

- Spin triplet superconductor ($T_{\text{sc}} \sim 2\text{K}$)
- Field reinforced superconductivity
- Multiple superconducting phases
- Comparison with FM superconductors

Unconventional superconductivity in SCES

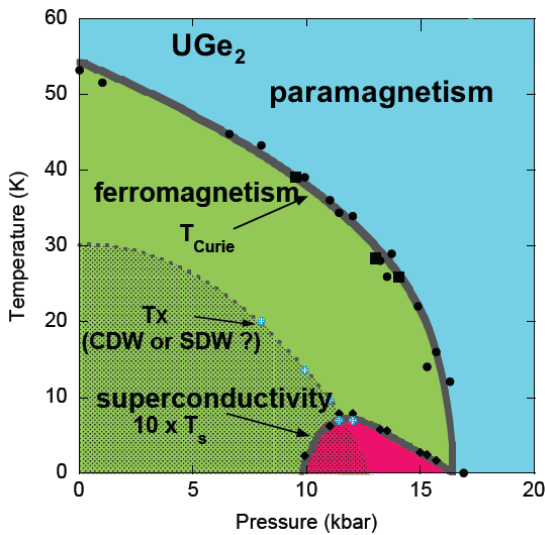
Superconductivity the verge of “magnetic instabilities”:

- Pairing mechanism related to the exchange of magnetic excitations ?
- Competing interactions : which one controls pairing ?

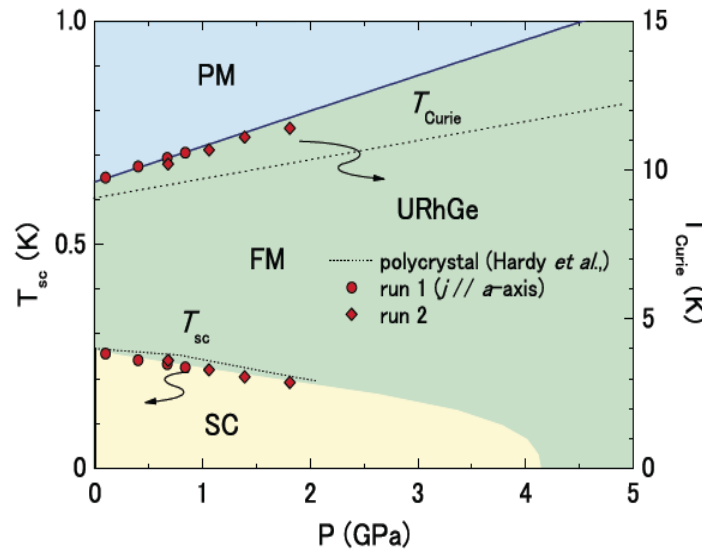


FM-SC in uranium-based systems

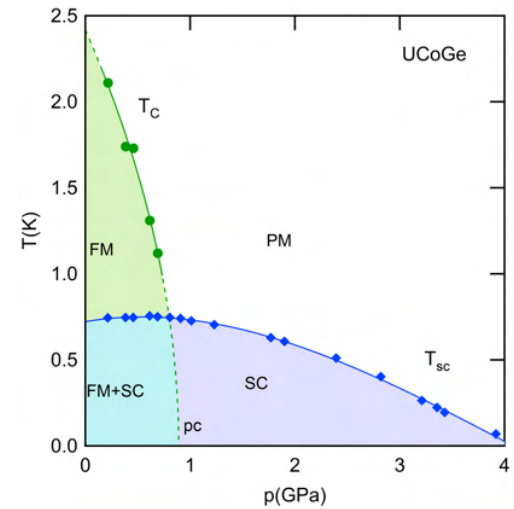
Three known systems, always with $T_{\text{Curie}} > T_{\text{sc}}$



Saxena et al. Nature 2000
Huxley et al. PRL 2003



Aoki et al Nature 2001
Hardy et al. PRL 2005



Huy et al, PRL 2007
E. Hassinger et al., PRB 2008
E. Slooten et al., PRL 2009
G Bastien et al. PRB 2016

Uranium-based FM-SC

- Orthorhombic, with « zig-zag » U-chains
- Uranium: $\sim 5f^3$ (Fujimori JPSJ 2012, 81, 014703)
- 5f bands at E_F (Fujimori et al. PRB 2014-2015)
- « **Ising** type », **weak** itinerant (?) ferromagnets
- SCES: $m^*/m_0 \geq 50$

UGe₂: $T_{c_max} \sim 0.8K$,

$T_{curie} \sim 35K$, at 12kbars

$m_s \sim 1.4\mu_B$ at 0kbar.

URhGe: $T_{sc} \sim 0.25K$,

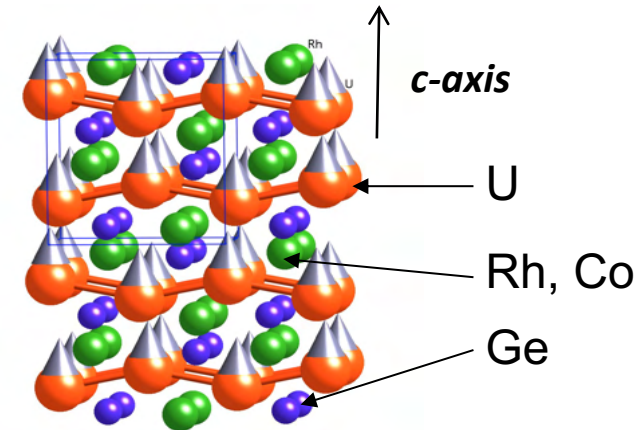
$T_{Curie} \sim 9.5K$, $m_s \sim 0.4\mu_B$

$n_e^{5f} \sim 2.61$, $\mu_L/\mu_S \sim -2.1$

UCoGe: $T_{sc} \sim 0.5K$,

$T_{Curie} \sim 2.5K$, $m_s \sim 0.04\mu_B$

$n_e^{5f} \sim 2.84$, $\mu_L/\mu_S \sim -2.3$



S. Saxena et al. Nature 406 (2000) 587

D. Aoki et al. Nature 413 (2001) 613

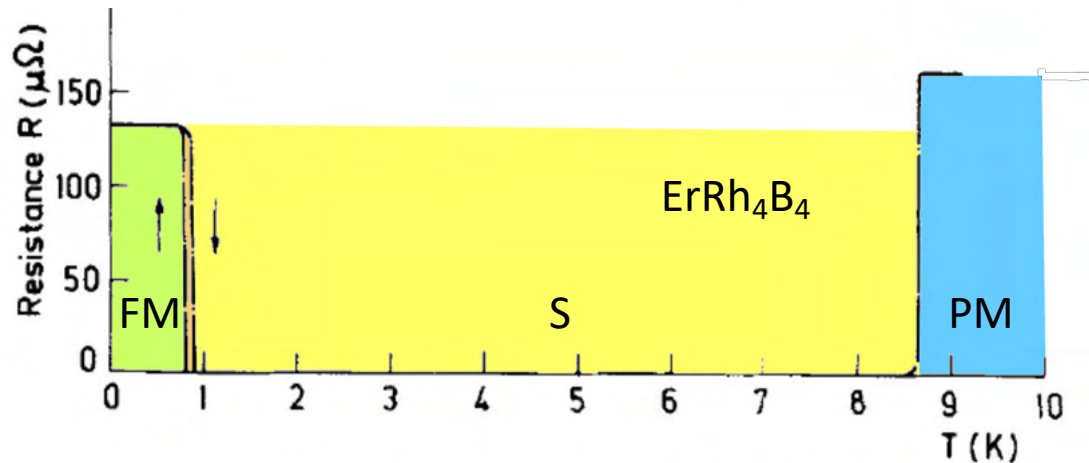
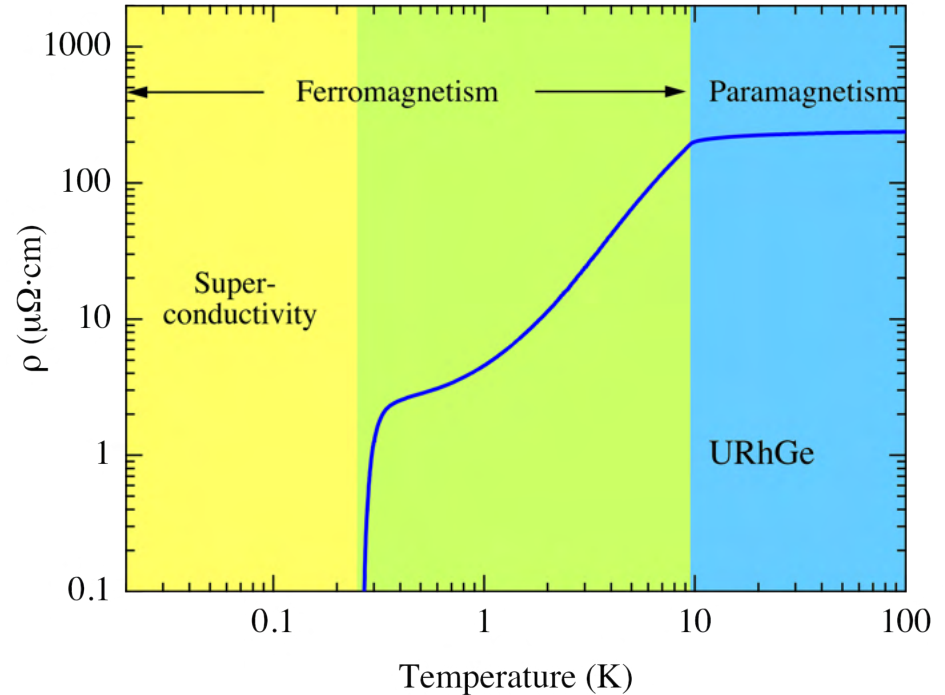
N.T. Huy et al.: Phys. Rev. Lett. 99 (2007) 067006

Superconductivity in FM-SC

In heavy fermion systems:

- $T_{\text{Curie}} > T_{\text{sc}}$
- true coexistence (e.g. muons:
Huy et al. PRL **2007**, 99, 067006)
- the same 5f-electrons yield
 - ferromagnetism
 - superconductivity

Why/how is it possible ?



Dipolar and exchange fields

Ferromagnet/paramagnet: exchange or dipolar-governed

$$\mathbf{B}_{dip} \sim \mu_0 \mathbf{M} \sim \frac{\mu_0 \mu_{ord}}{V_{at}} \approx 0.3 \text{ T}/\mu_B$$

\mathbf{B}_{ex} from Coulomb interaction: can be $\sim 100 \text{ T}$

$$\hat{\mathcal{H}}^{spin} = -g\mu_B \mathbf{B}_{ex} \cdot \mathbf{S}$$

\mathbf{B}_{dip} : real magnetic field, acts on orbital & Pauli limits

\mathbf{B}_{ex} : effective field, acts on spins only => Pauli limit ONLY.

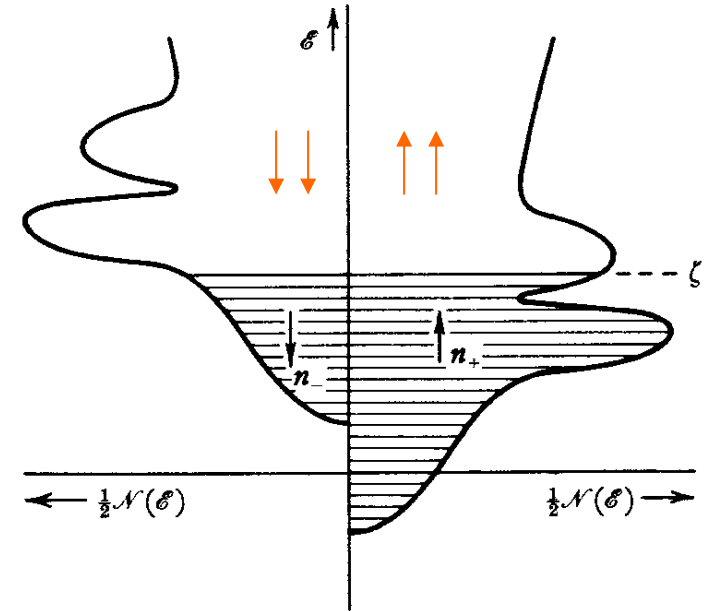
Superconductivity in FM heavy-fermions

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Why/how is it possible ?

	UGe ₂	URhGe	UCoGe
$\mu_{\text{ord}} / \text{uranium}$	$\sim 1 \mu_{\text{B}}$	$\sim 0.4 \mu_{\text{B}}$	$\sim 0.045 \mu_{\text{B}}$
$B_{\text{dip}} \sim \mu_0 M$	0.2T	0.09T	0.01T
$B_{\text{ex}} > (k_{\text{B}}/\mu_{\text{B}})T_{\text{Curie}}$	>50T	>13T	>4.5T



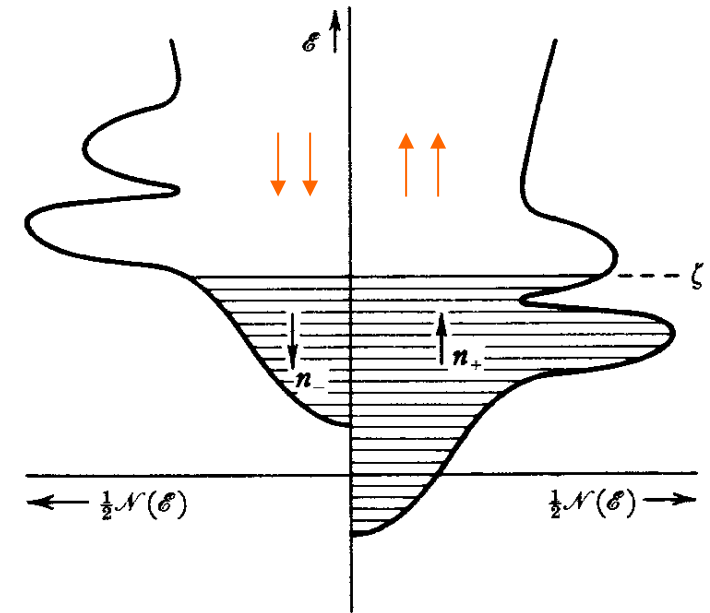
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→ $\ll H_{c2}^{\text{orb}}$: no problem for HF

Always in the mixed state : Paulsen et al. PRL **109** 237001 (2012),
 Deguchi et al. JPSJ, **79**, 083708 (2010)

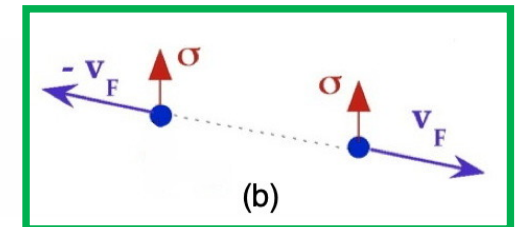
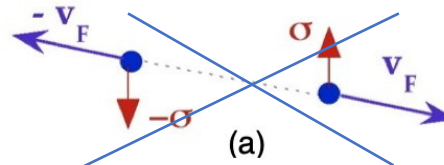
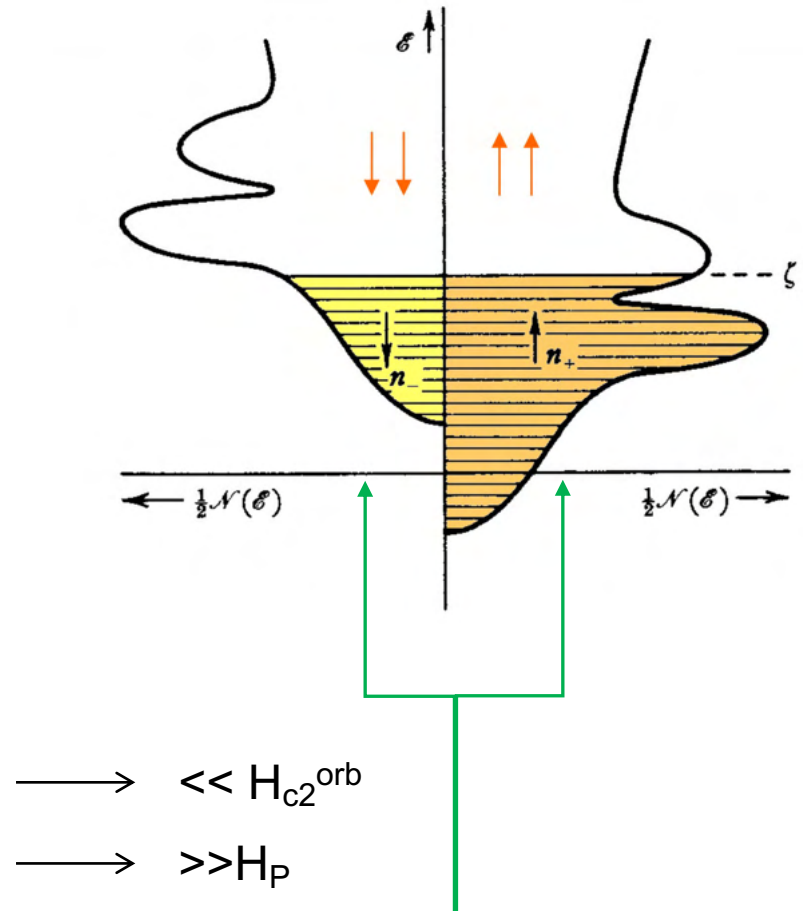
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$B_{\text{Pauli}} (\sim 2T_{\text{sc}})$	1.6T	.5T	1T



Superconductivity in FM heavy-fermions

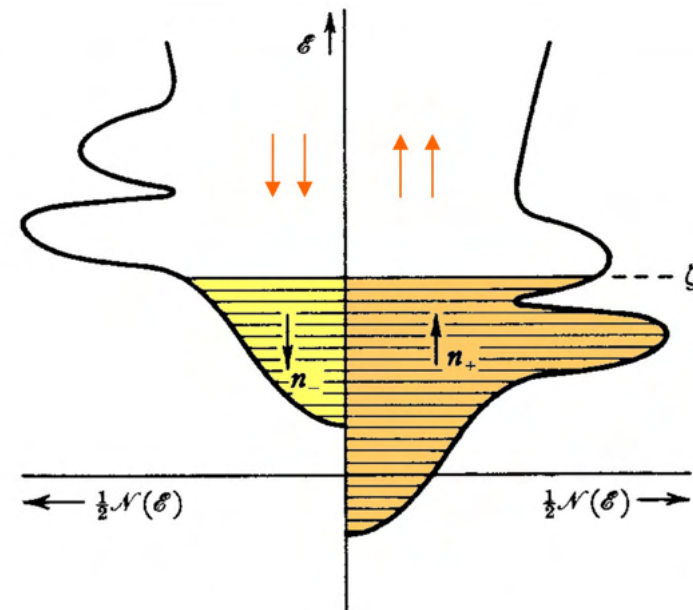
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→ $\ll H_{\text{c2}}^{\text{orb}}$
 → $\gg H_{\text{p}}$



$T_{\text{Curie}} \gg T_{\text{sc}}$ implies **a different superconducting state :**
a spin-triplet, ESP, superconducting state

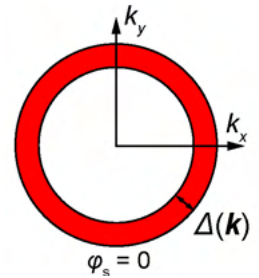
Spin-singlet Superconductors

Conventional superconductors

- **s-wave** (singlet) superconductors
- pairing mechanism: phonons

$$(k, \uparrow) \quad (-k, \downarrow) \quad \text{with:} \quad |\psi \rangle = \varphi(\mathbf{k})(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

$$\varphi(\mathbf{k}) = \varphi(-\mathbf{k}) \quad \text{and} \quad \varphi(\mathbf{k}) \text{ isotropic (s-wave)}$$



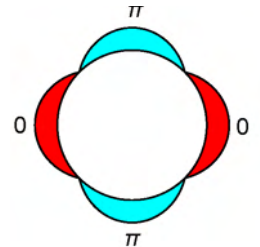
Unconventional Superconductors (e.g. cuprates):

- **d-wave** (singlet) superconductivity
- pairing mechanism: AF correlations

$$(k, \uparrow) \quad (-k, \downarrow) \quad \text{with:} \quad |\psi \rangle = \varphi(\mathbf{k})(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

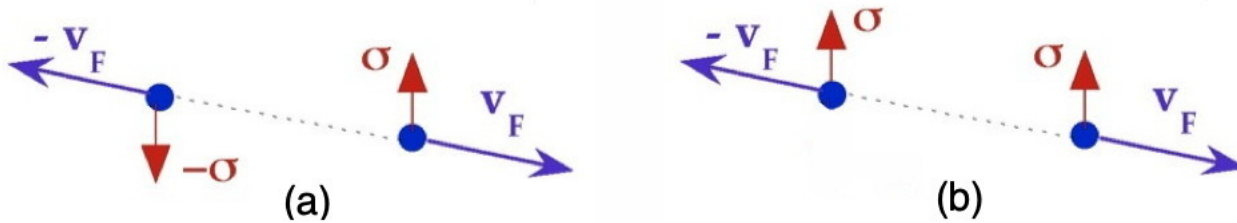
$$\varphi(\mathbf{k}) = \varphi(-\mathbf{k}) \quad \text{and} \quad \varphi(\mathbf{k}) \text{ anisotropic (d-wave)}$$

$$\Delta(\hat{\mathbf{k}}) = \Delta_0 \left| \hat{k}_x^2 - \hat{k}_y^2 \right| = \Delta_0 |\cos(2\theta)|$$



Spin-triplet superconductors

- **Unconventional superconductors (uranium based...)**
 - p-wave (triplet) superconductivity
 - pairing mechanism: ferromagnetic fluctuations (FM superconductors)



$$(k, \uparrow) \quad (-k, \uparrow) \quad \text{or:} \quad (k, \downarrow) \quad (-k, \downarrow) \dots$$

$$|\psi\rangle = \varphi(\mathbf{k}) |\uparrow\uparrow\rangle \quad \text{or} \quad |\psi\rangle = \varphi(\mathbf{k}) |\downarrow\downarrow\rangle \quad \text{or}$$

$$|\psi\rangle = \varphi(\mathbf{k}) (|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle)$$

$$\varphi(\mathbf{k}) = -\varphi(-\mathbf{k}) \quad \text{and} \quad \varphi(\mathbf{k}) \text{ anisotropic (p-wave, f-wave...)}$$

Odd/
triplet

ESP spin-triplet superconducting state

- Most general form (Cooper pair wave function or Order Parameter):

$$|\Psi(\hat{\mathbf{k}})\rangle = \varphi(\hat{\mathbf{k}})|S=1\rangle$$

$$|\Psi\rangle = \varphi_{11}(\mathbf{k})|\uparrow\uparrow\rangle + \varphi_{22}(\mathbf{k})|\downarrow\downarrow\rangle + \varphi_{12}(\mathbf{k})|\uparrow\downarrow + \downarrow\uparrow\rangle$$

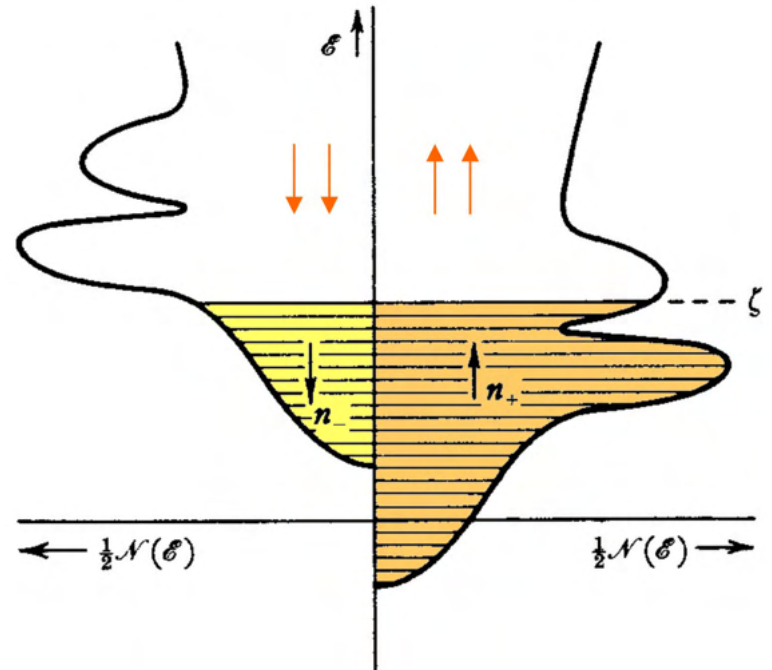
ESP spin-triplet superconducting state

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- **ESP** = Equal Spin Pairing:

Cooper pairs with only $|\uparrow\uparrow\rangle$ or $|\downarrow\downarrow\rangle$ spin states



ESP spin-triplet superconducting state

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$$|\Psi\rangle = \varphi_{11}(\mathbf{k})|\uparrow\uparrow\rangle + \varphi_{22}(\mathbf{k})|\downarrow\downarrow\rangle + \varphi_{12}(\mathbf{k})|\uparrow\downarrow\rangle + \varphi_{21}(\mathbf{k})|\downarrow\uparrow\rangle$$

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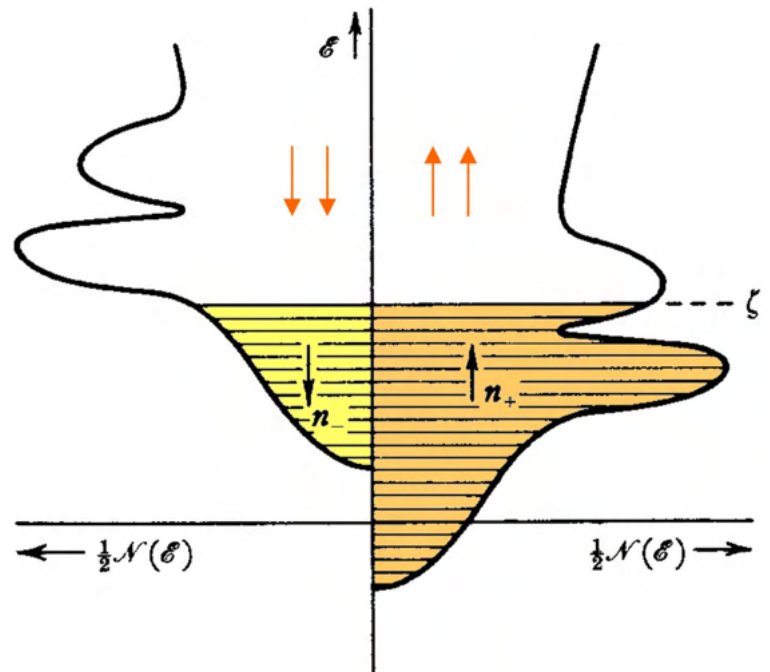
Cooper pairs with only $|\uparrow\uparrow\rangle$ or $|\downarrow\downarrow\rangle$ spin states

$$|\Psi\rangle = \Delta^\uparrow|\uparrow\uparrow\rangle + \Delta^\downarrow|\downarrow\downarrow\rangle$$

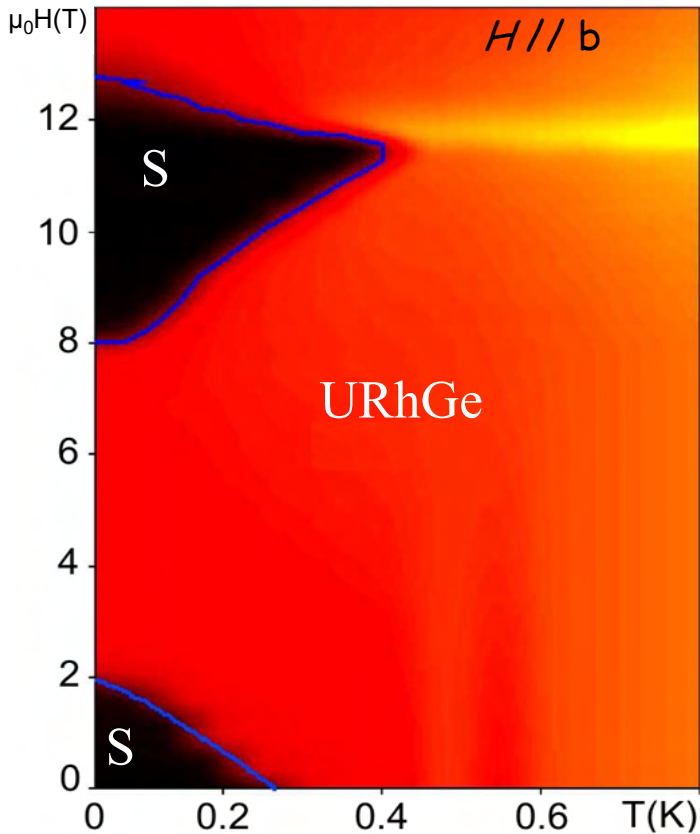
Phase & amplitude of Δ^\uparrow and Δ^\downarrow may change on the F.S.

“Explains” the coexistence FM-SC
(survival to B_{ex})

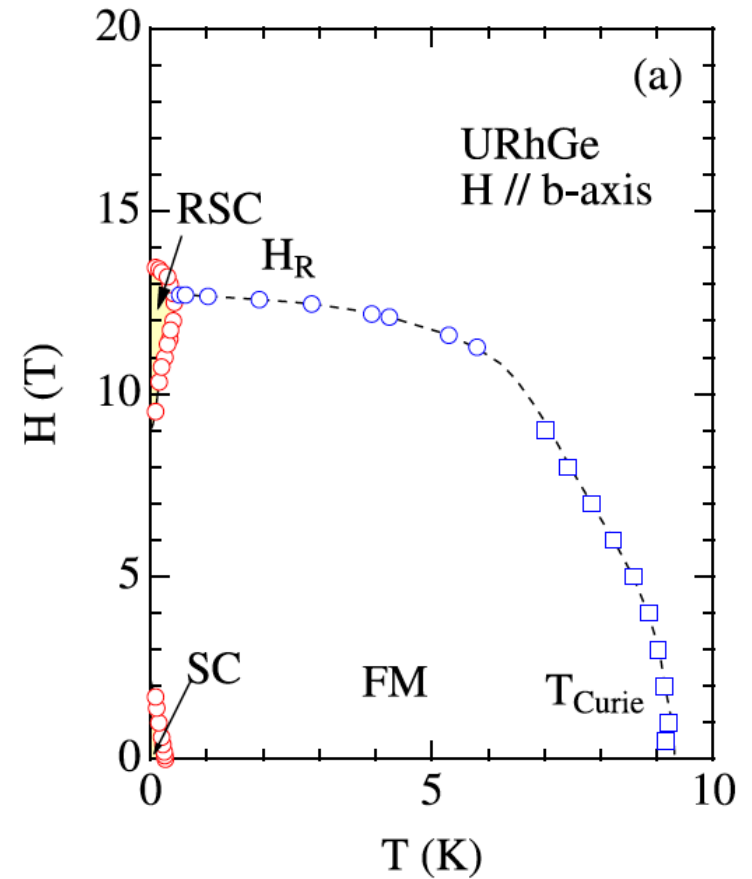
But it does not explain everything...



Effect of transverse field: reinforced superconductivity



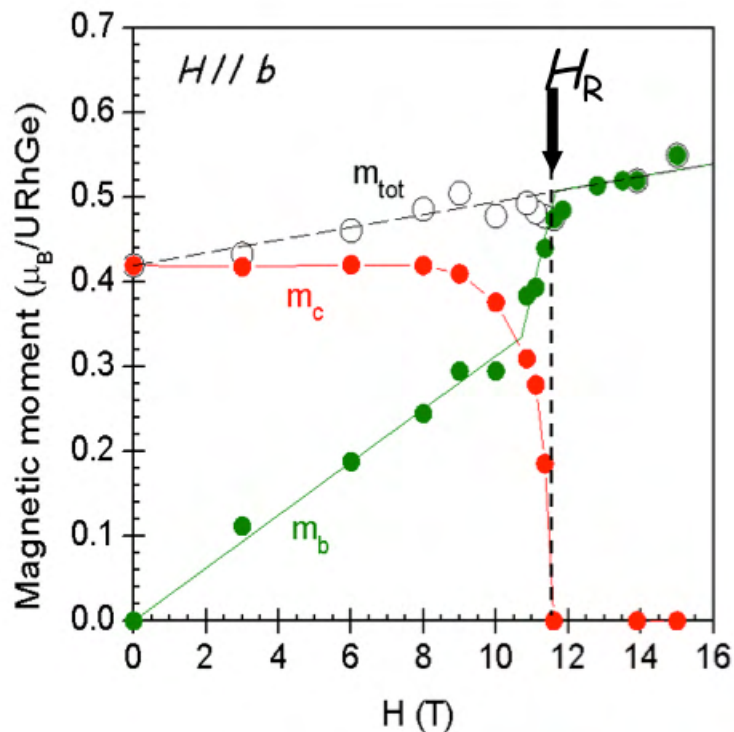
Levy et al. *Science*, **2005**, 309, 1343-1346



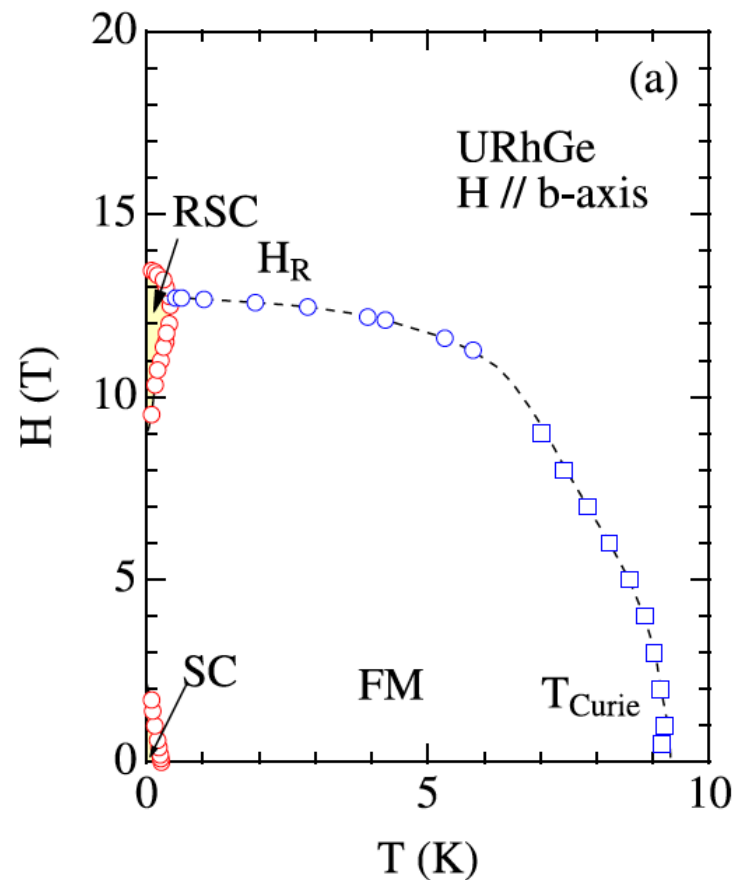
D. Aoki et al., *Compt. Rendus. Phys.* 12, 573 (2011)

The re-entrant superconducting phase, at the collapse of T_{Curie}

Effect of transverse field: moment re-orientation

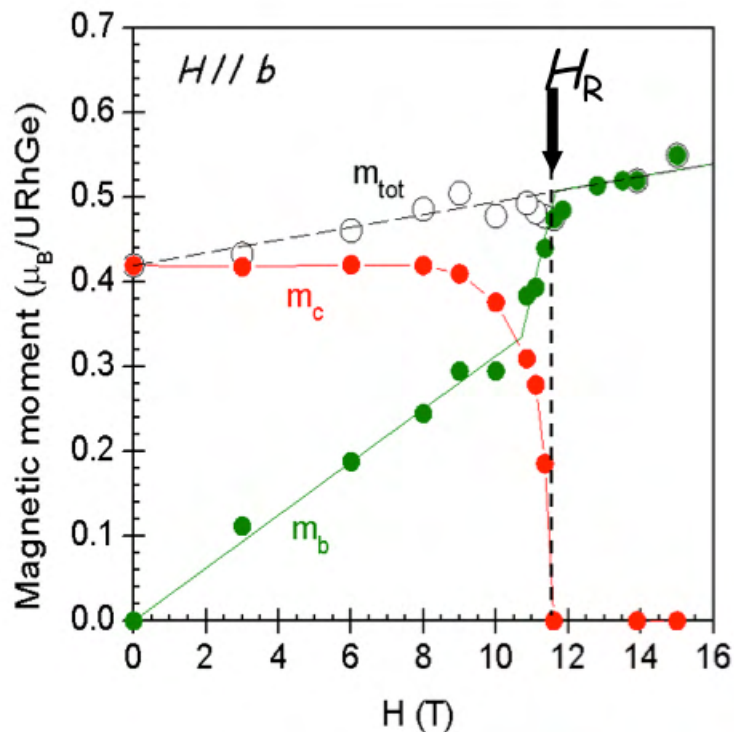


Levy et al. *Science*, **2005**, 309, 1343-1346

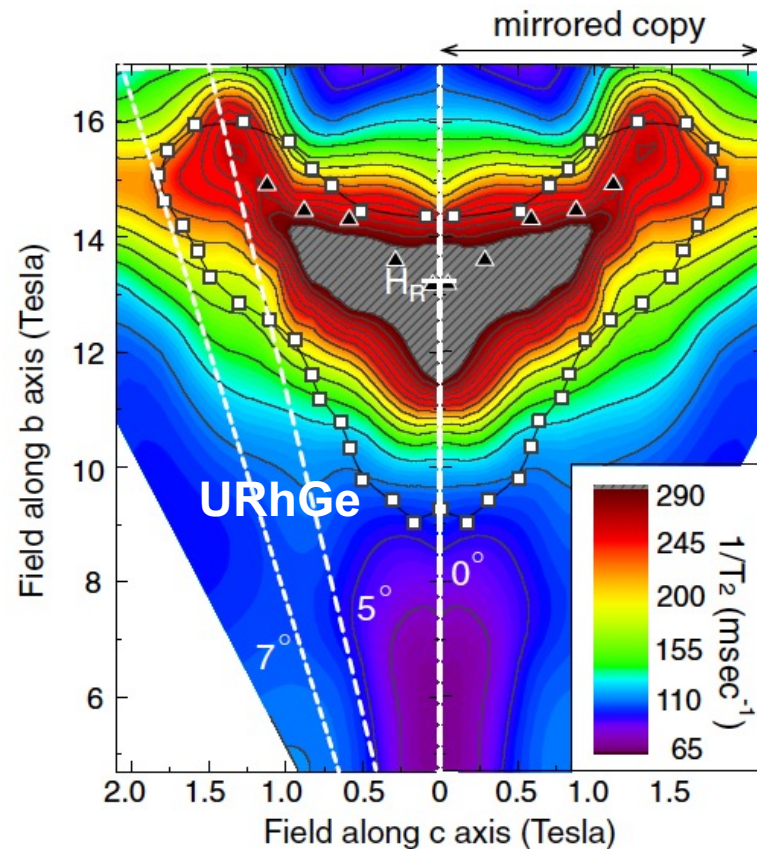


- Easy axis = c-axis; changed to b-axis for fields $\sim 12\text{T} // b$

Effect of transverse field: magnetic fluctuations



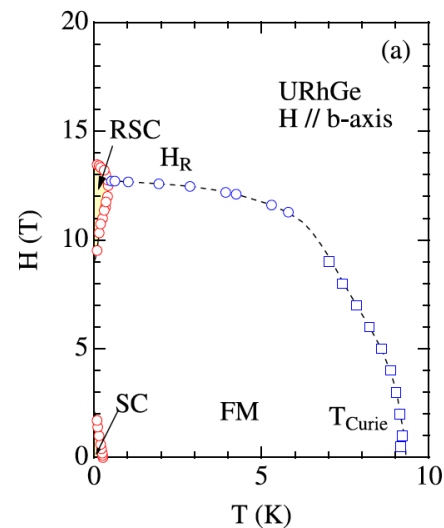
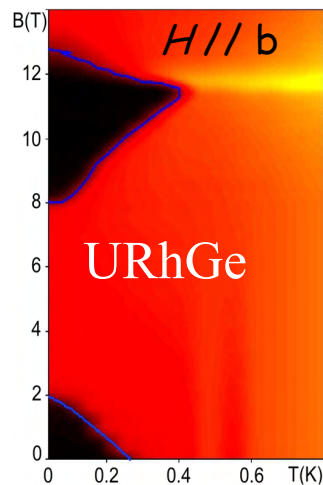
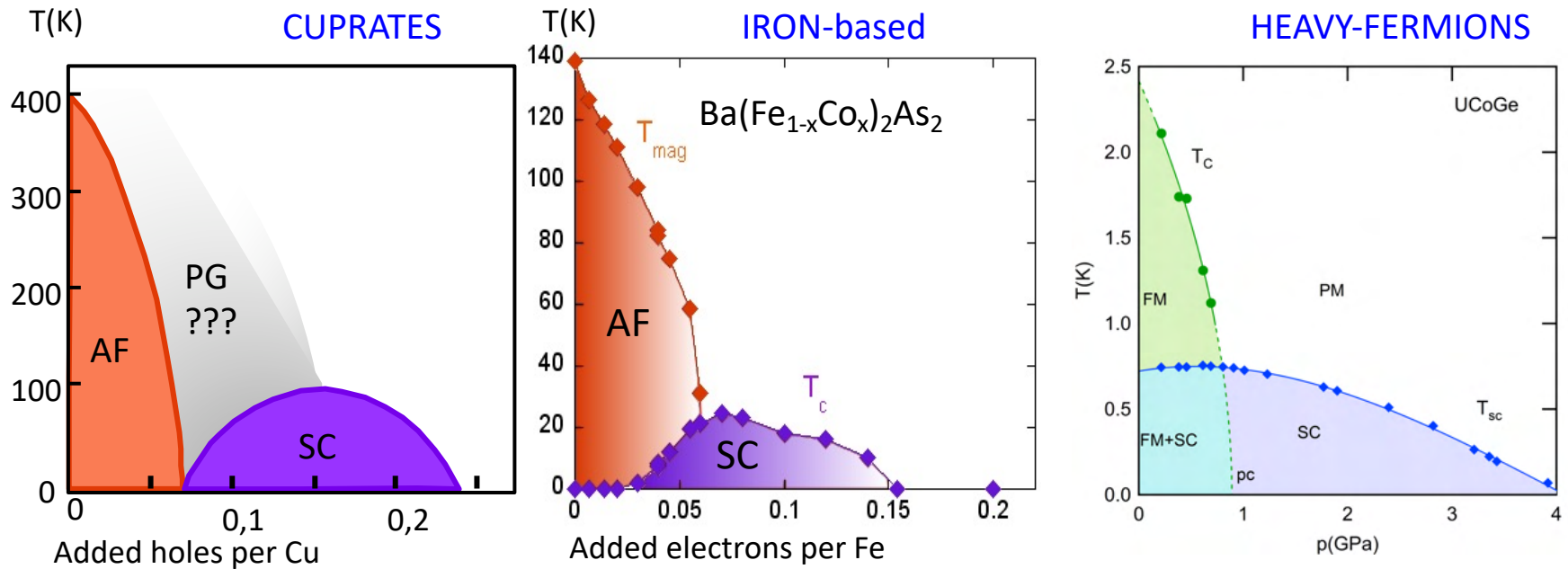
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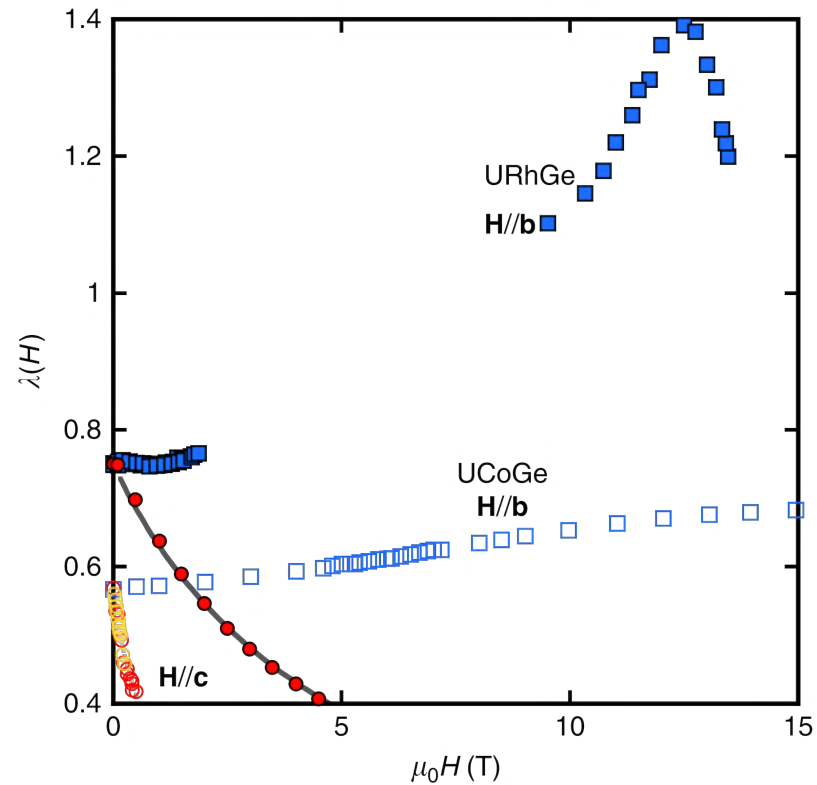
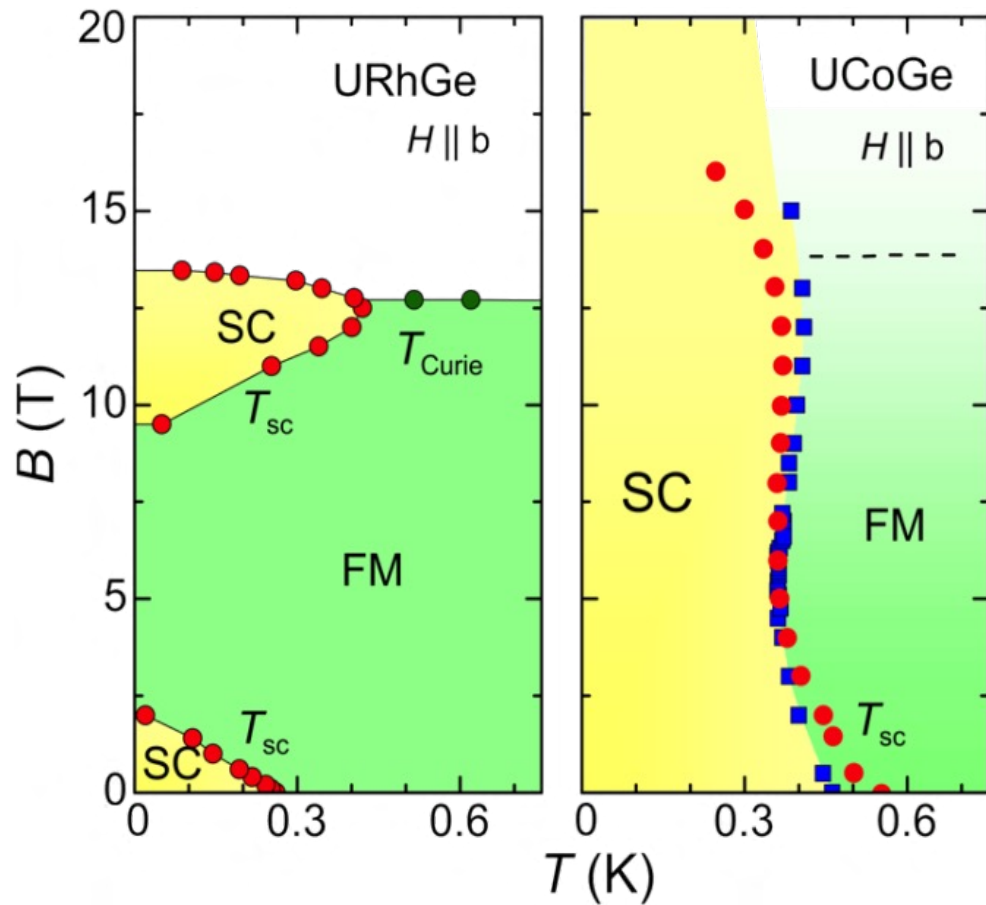
Tokunaga et al. *PRL* **2015**, 114, 216401

- Easy axis = c-axis; changed to b-axis for fields ~ 12 T//b
- Increase of the magnetic fluctuations (NMR)

Effect of a transverse field: a field-induced QCP



Field dependence of the pairing in FM-SC



Levy et al Science 2005,
Nature 2007

Aoki et al. JPSJ 2009

B. Wu et al., Nature Com. **2017**, 8, 14480

Precise microscopic theoretical model still missing...

Summary – FM-SC

- FM imposes an ESP spin-triplet state:
Chiral and non-unitary (TRS breaking by orbital & spin)
- Pairing due to FM fluctuations:
Reinforced when $T_{\text{curie}} \rightarrow 0$ ($B \perp$ easy axis)
Suppressed when $B //$ easy axis
- 2 gap superconductor (Δ^\uparrow and Δ^\downarrow):
 T_{sc} larger for “non-Ising” type fluctuations
- No microscopic model for:
 - the magnetic state
 - $\mathbf{d}(\mathbf{k})$ under transverse fields !

“New” system: **UTe₂**

PhD work of **Adrien Rosuel**

Diplomarbeit **Nils Marquardt** -> see poster this afternoon

Collaboration with **C Marcenat** and **T Klein**

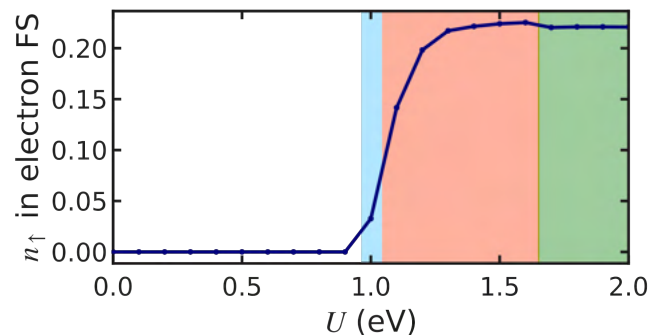
(High field experiments)

+ **Pheliqs/CEA team: G Knebel, D Braithwaite, A Pourret, G Lapertot.**

+ **D Aoki** (IMR Sendai)

UTe₂ a correlated anisotropic metal

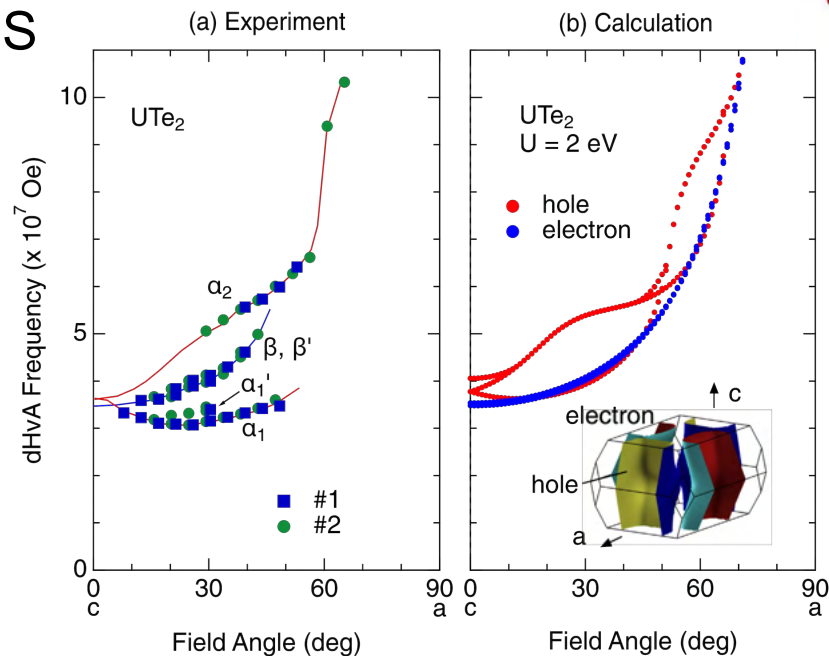
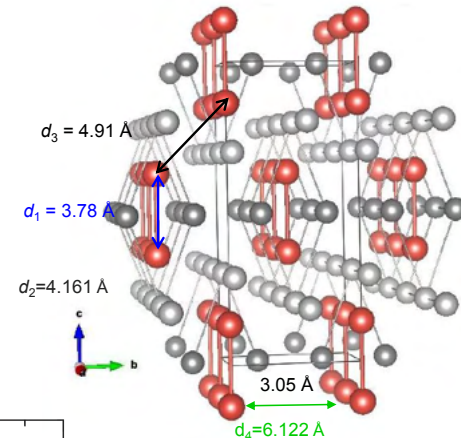
- Superconductivity discovered in 2018 (Ran et al. Science 2019)
- A band insulator, metallic thanks to correlations !



Ishizuka et al. PRL 2019

- 3D metal but quasi 2D FS
- $m^*/m_0 \sim 50$

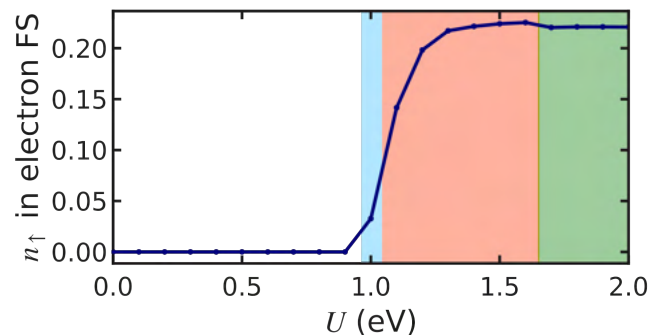
body centered orthorhombic
space group Immm (#71, D_{2h}^{25})



Aoki et al. JPSJ 2022

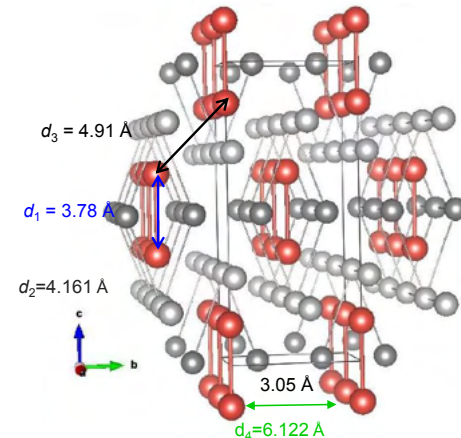
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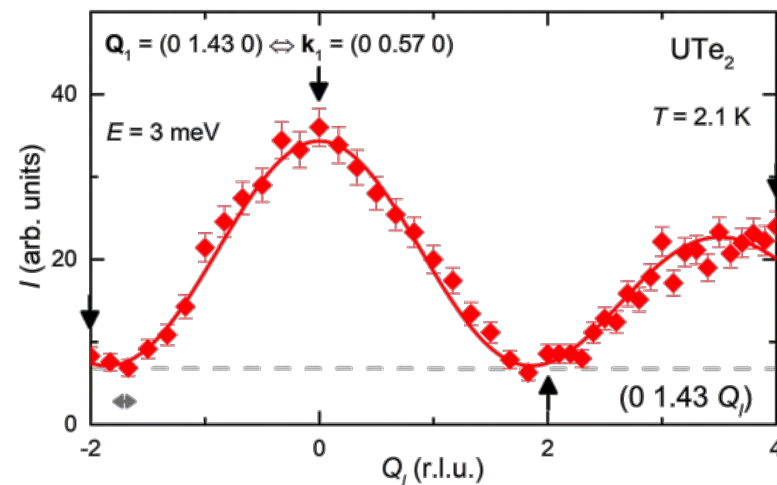
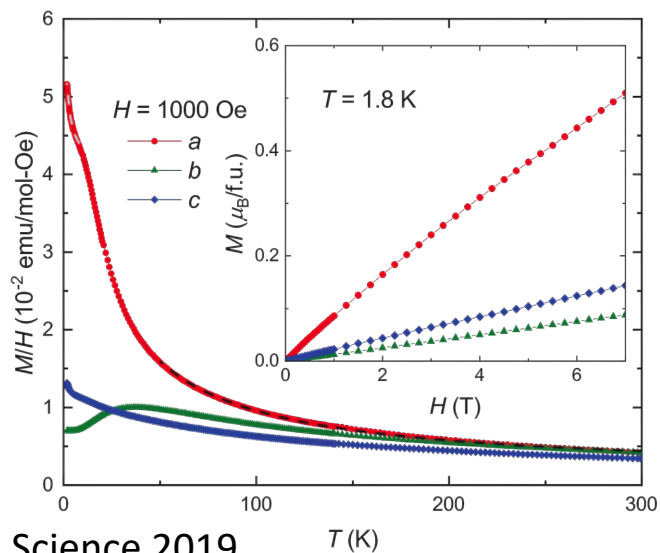


Ishizuka et al. PRL 2019

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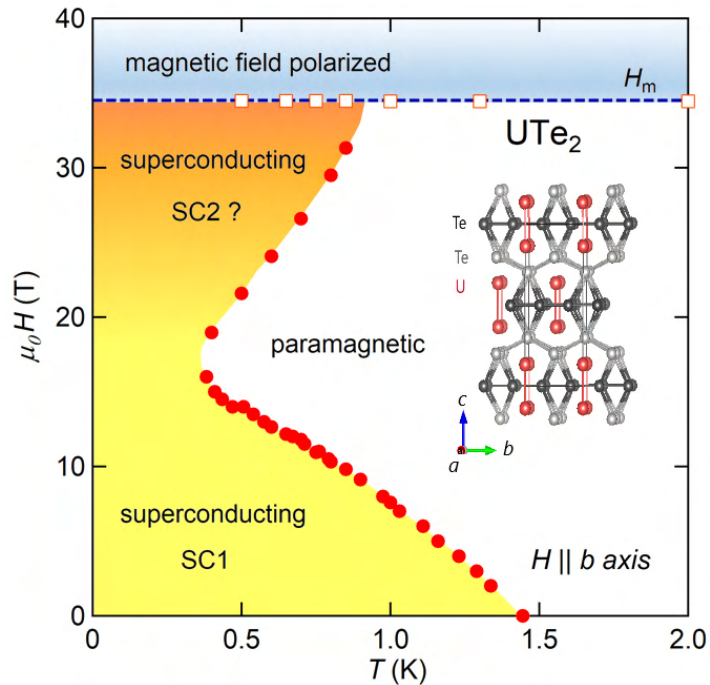
- 3D anisotropic paramagnet, with low-D fluctuations



Knafo et al. PRB 2021

Ran et al. Science 2019

UTe₂: field reinforced and field induced phases !

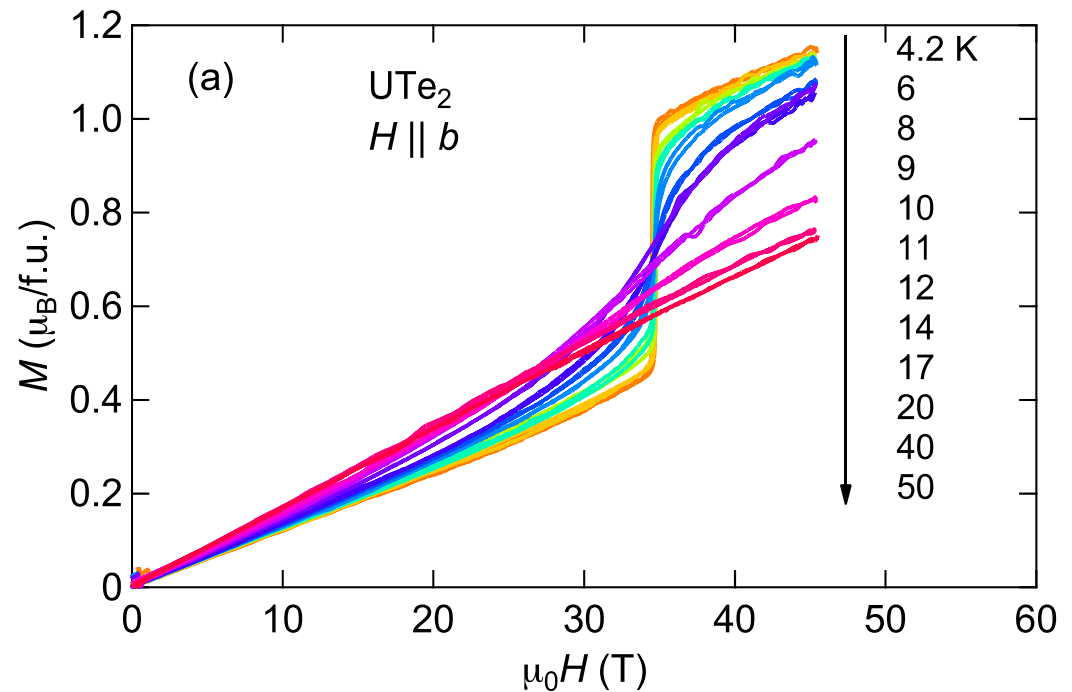


Knebel et al. JPSJ 88 063707 (2019)

Ran et al. Science 2019

Ran et al. Nature Phys 2019

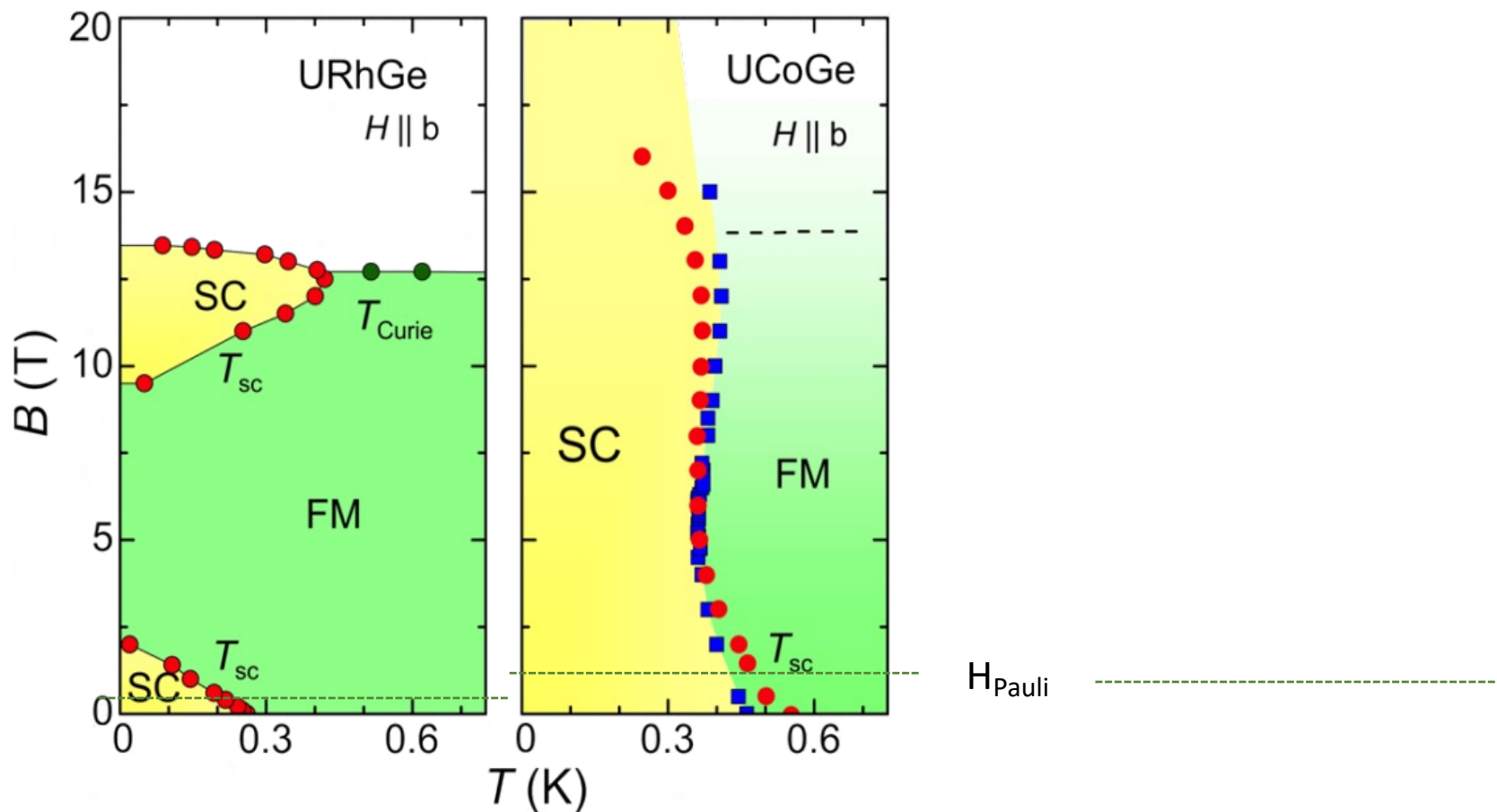
- Spin triplet superconductivity: violation of Pauli limit in the three directions.
- Field-reinforced SC for transverse field ($H \parallel b$)
- SC stopped by metamagnetic transition



K. Miyake et al. et al. JPSJ 88 063706 (2019)

4- UTe₂ and FC-SC

Re-entrant or reinforced superconductivity under applied field

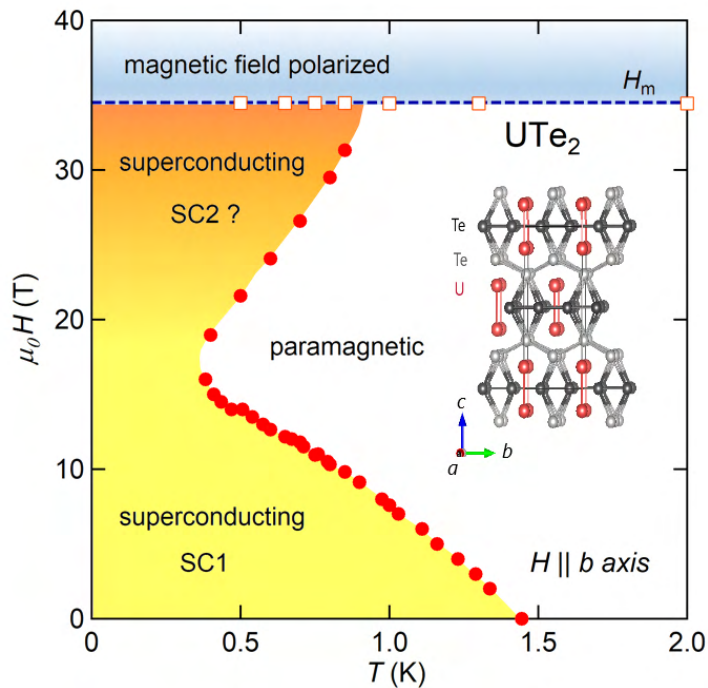


Levy et al Science2005,
Nature 2007

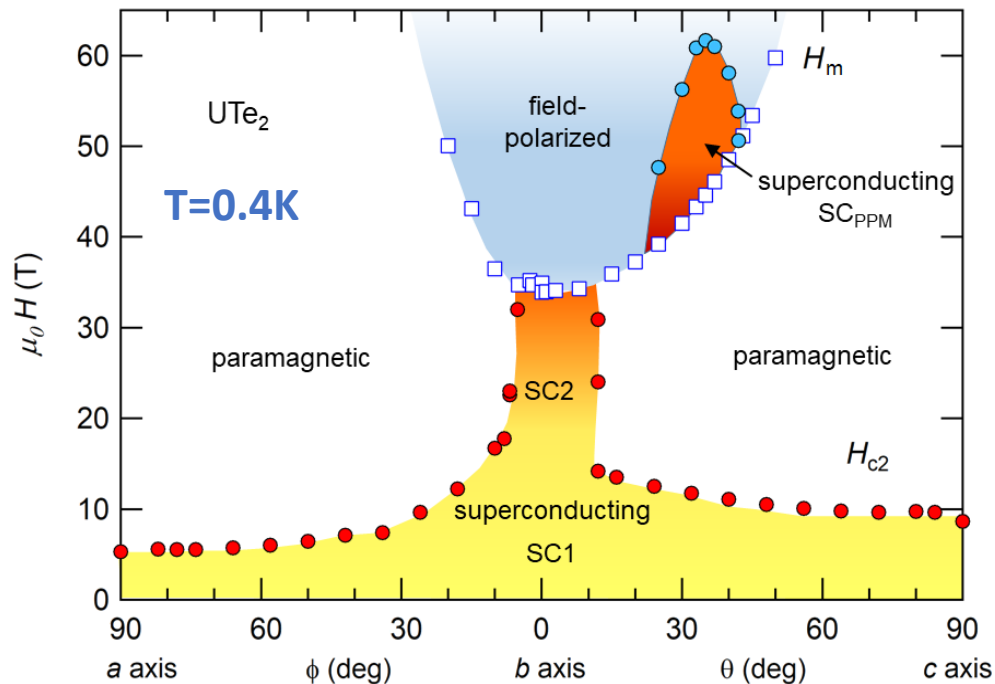
Aoki et al. JPSJ 2009

G Knebel et al. JPSJ 2019

UTe₂: field reinforced and field induced phases !



Knebel et al. JPSJ 88 063707 (2019)



Ran et al. Science 365 684 (2019)

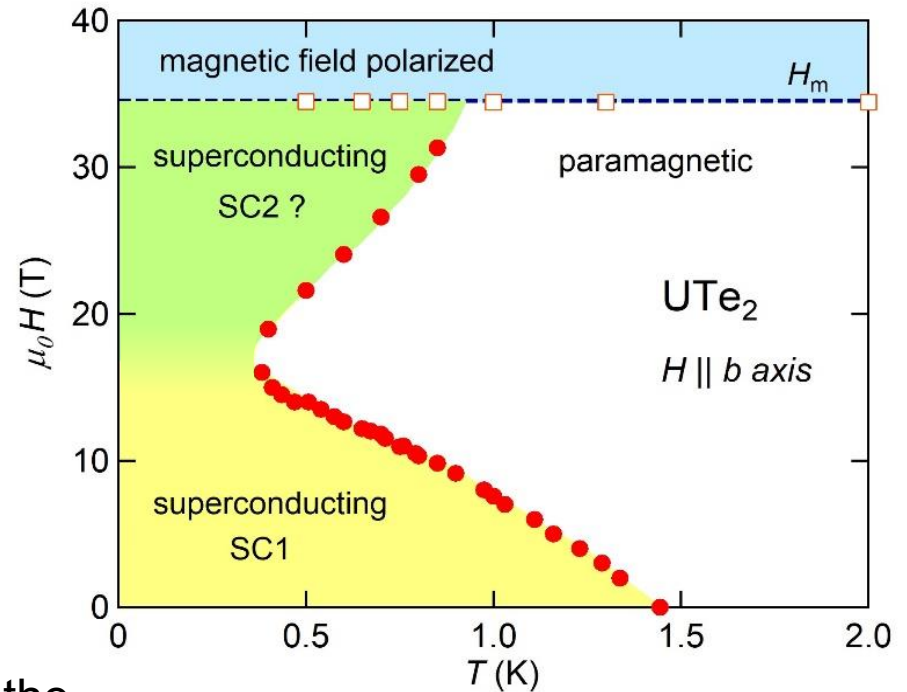
- At 34T, metamagnetic transition “stopping” superconductivity for $H \parallel b$
- With re-entrant phase above 40T at 30° between b and c

(some) Questions in UTe_2

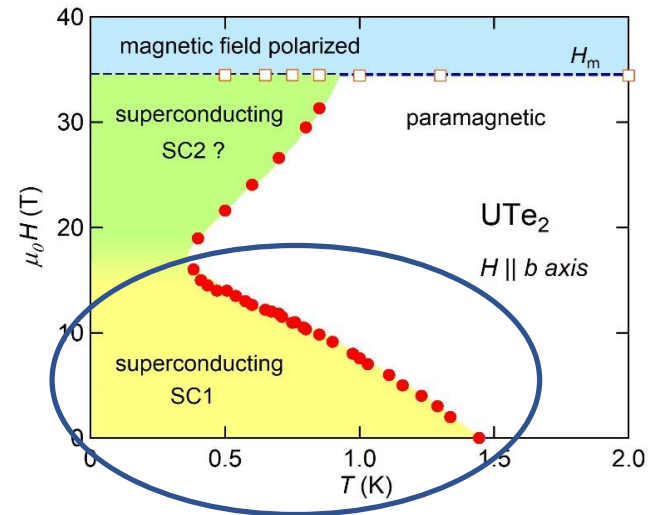
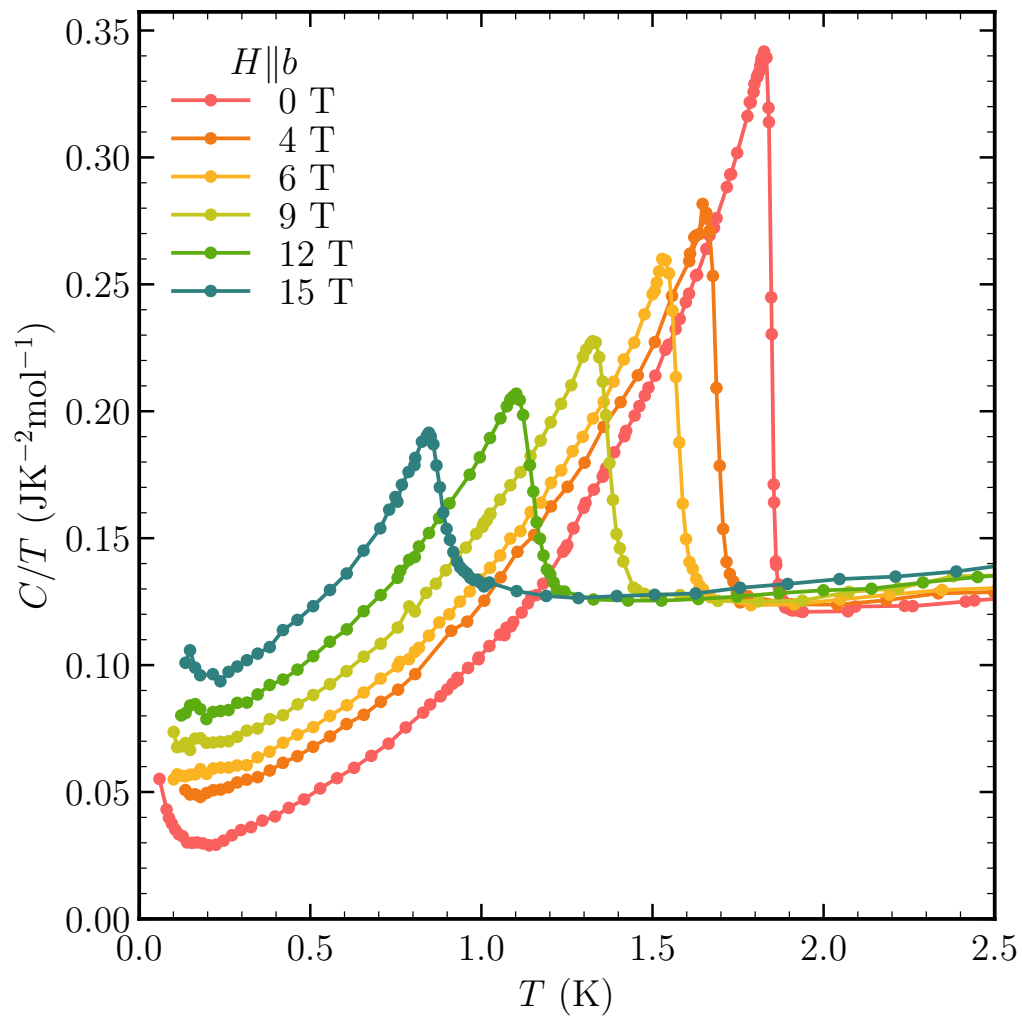
Questions ($H//b$) :

- Two different phases ?
- Difference SC1 / SC2 ?
- Comparison to FM SC ?

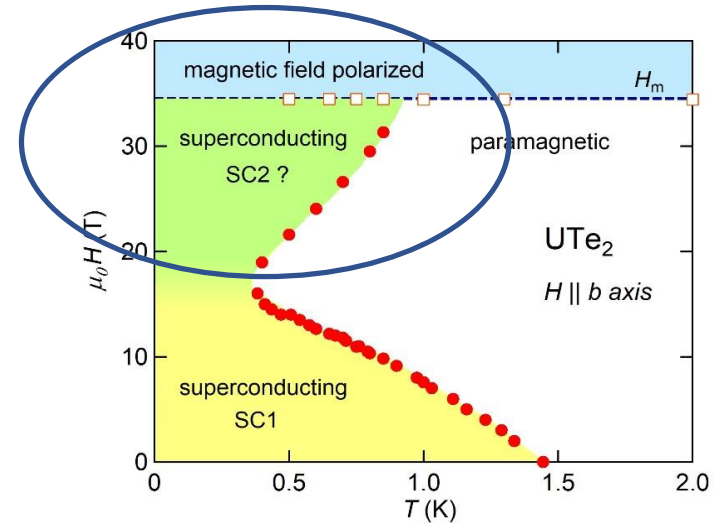
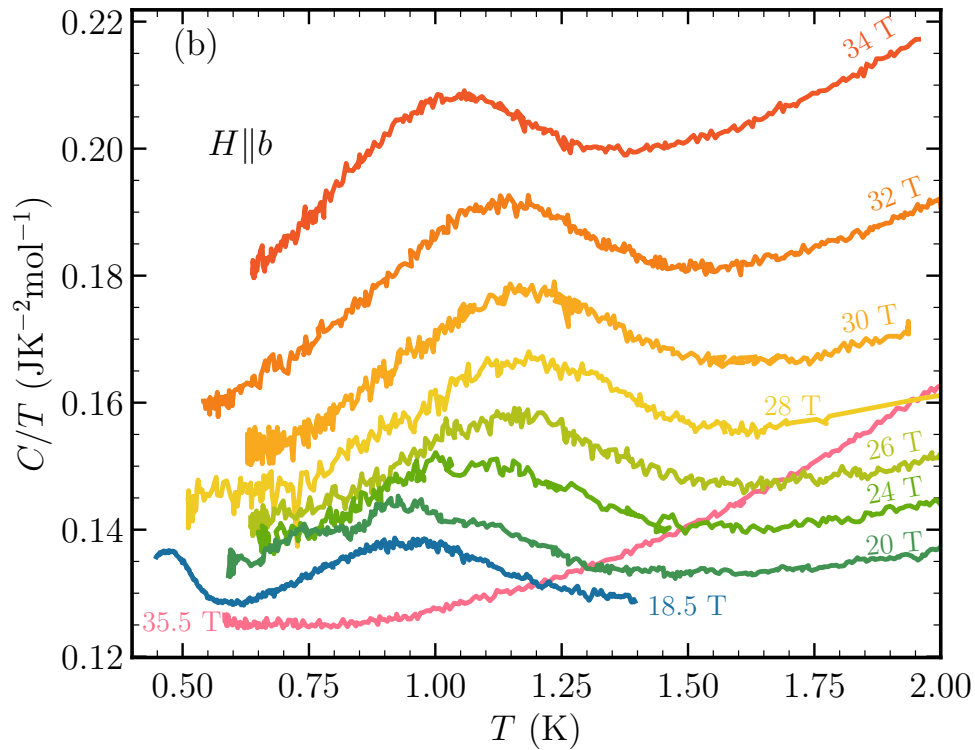
↓
Reinforcement of the
zero-field pairing



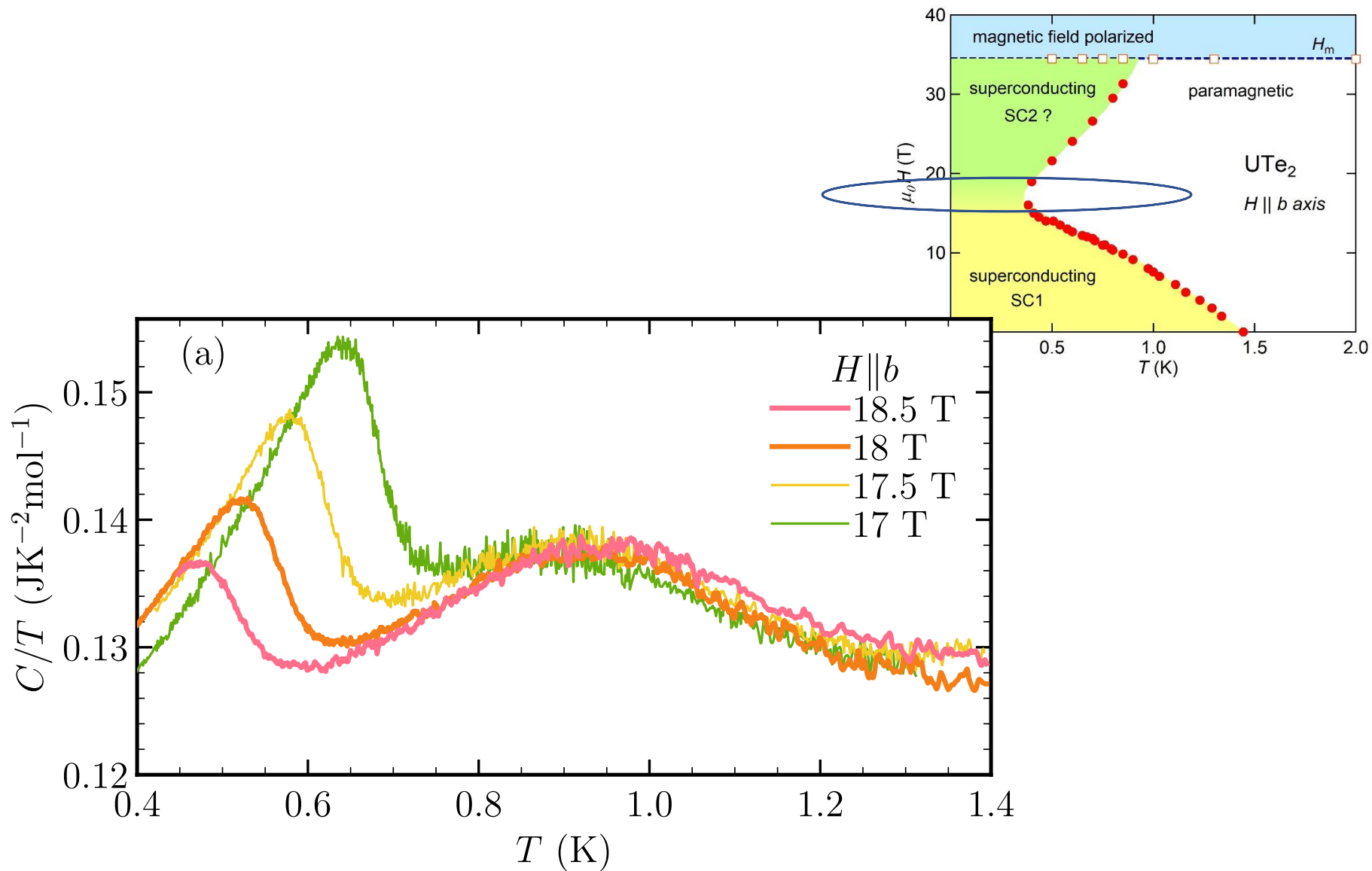
Specific heat under magnetic field, $H//b$



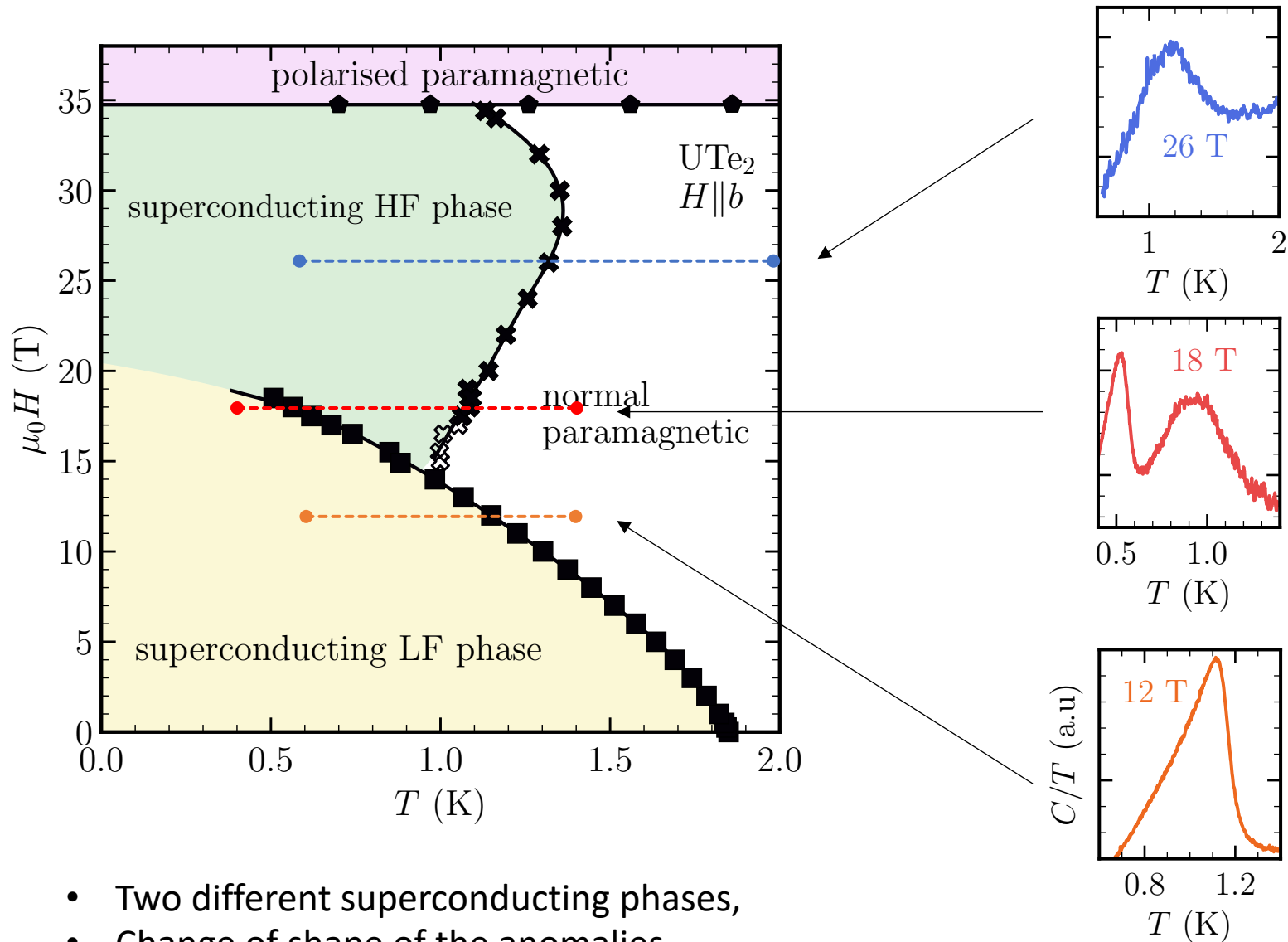
Specific heat under magnetic field, $H//b$



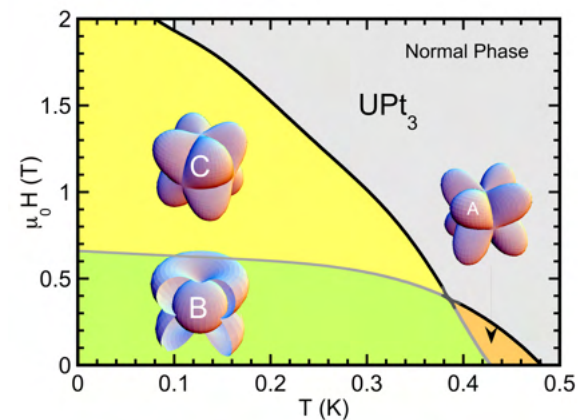
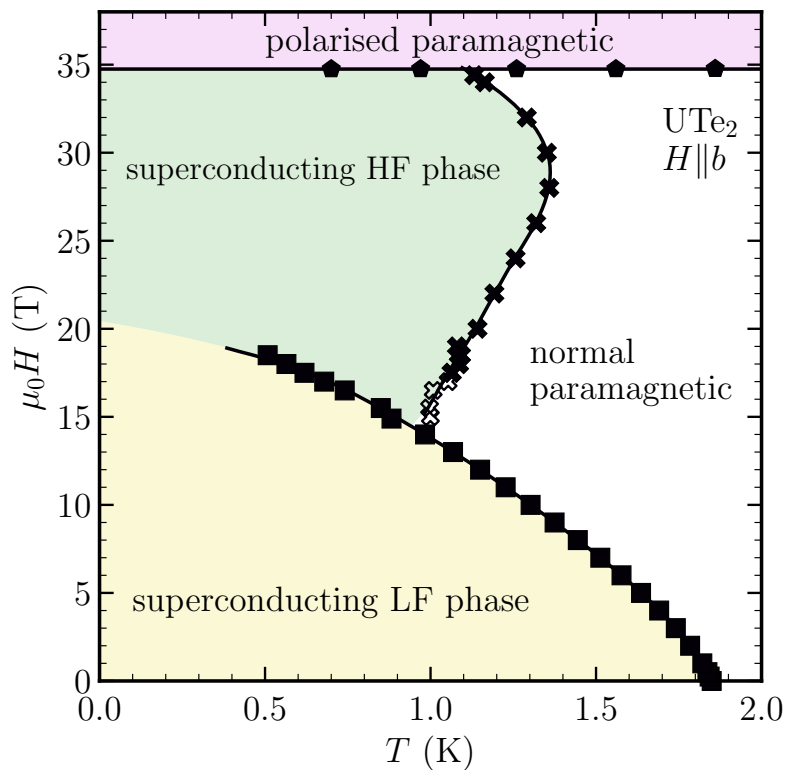
Specific heat under magnetic field, $H//b$



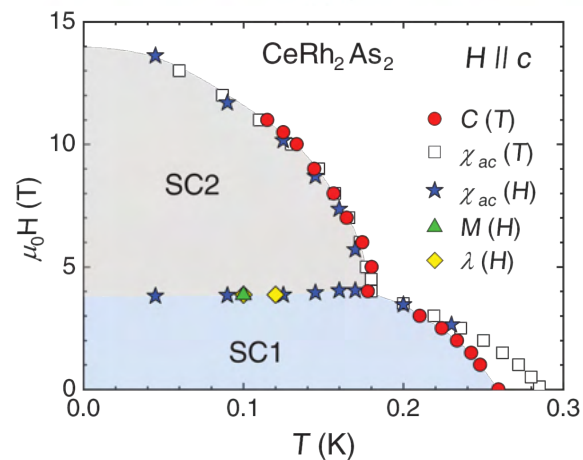
Phase diagram by specific heat



Multiphase superconductivity



Physica B 280, 165 (2000)



Khim et al., Science, 2021, 373, 1012-1016

In UTe_2 , $H//b$:

- LF phase weakly enhanced under field & narrow transition
- HF phase strongly reinforced by field & wide transition

} Different mechanism

- Different from UPt_3 , CeRh_2As_2 ... transition triggered by change of T , H , $p \Rightarrow$ different symmetry favoured for the same pairing mechanism

Connection with pressure phase diagram ?

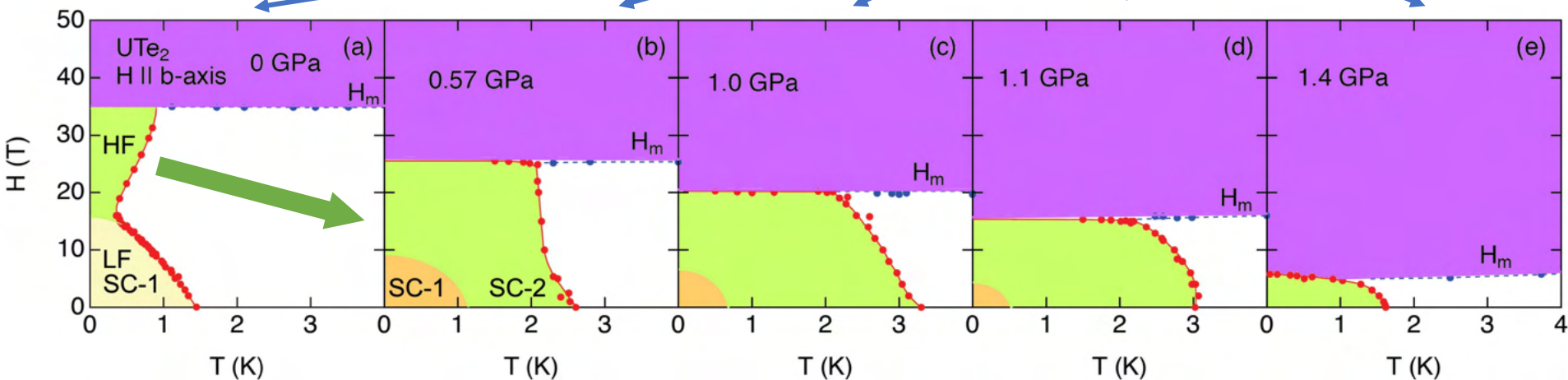
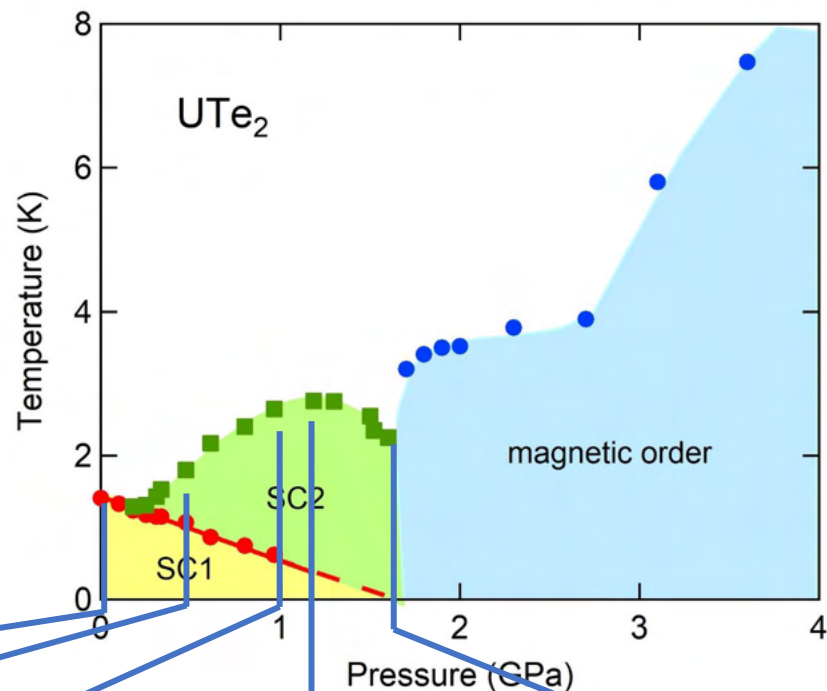
Under pressure,

- New “high temperature” SC phase
- Merges with the HF phase ?

Braithwaite et al., Comm. Phys 2019

Knebel et al. JPSJ 2020 + D Aoki 2022

Lin et al. npj Quantum Materials, **2020**

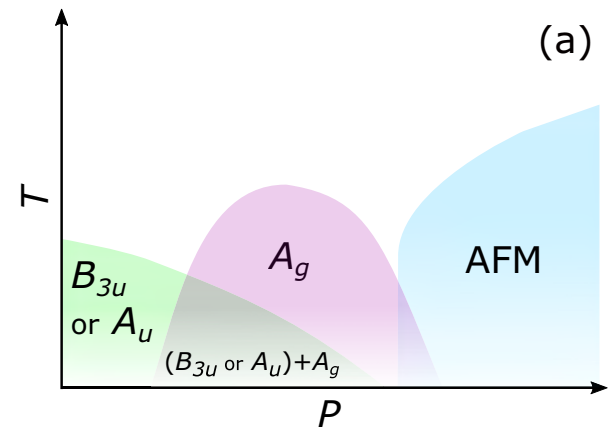
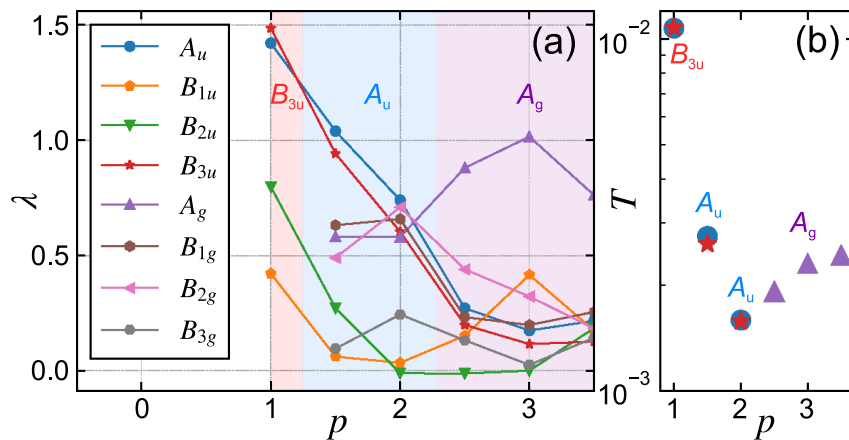


UTe₂ competing (pairing) interactions ?

Theory: competition/coexistence of AF and FM fluctuations

increase of f-character of FS under pressure => AF by nesting

- Low T_{SC} (field) phase: spin-triplet from FM fluctuations
- High T_{SC} (field) phase: spin-singlet from AF fluctuations



(Ishizuka & Yanase PRB 2021 **103** 094504)

Experimentally: AF fluctuations are dominant

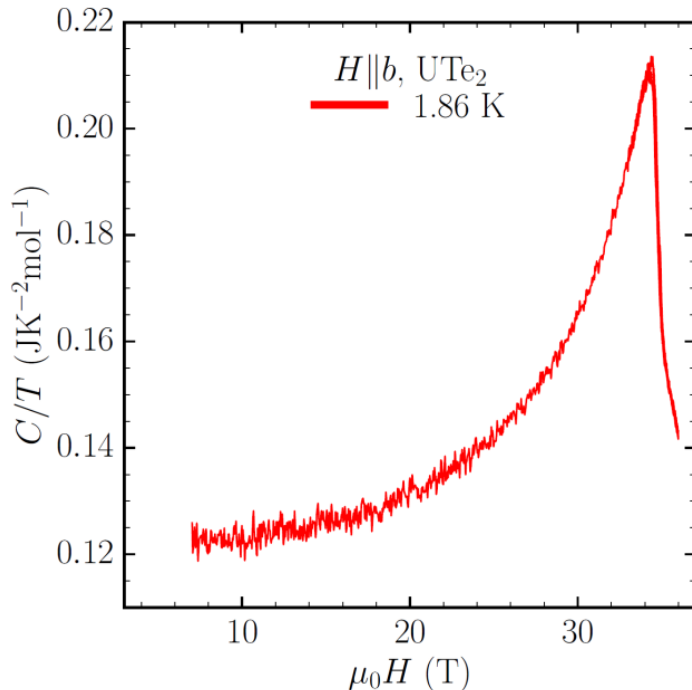
Durst et al. PRL **125** 237003 (2020),
Butch et al. *NPJ Qmat.* **2022**, 7,

Knafo et al. PRB **104** L100409 (2021)
Ambika et al PRB **105**, L220403 (2022)

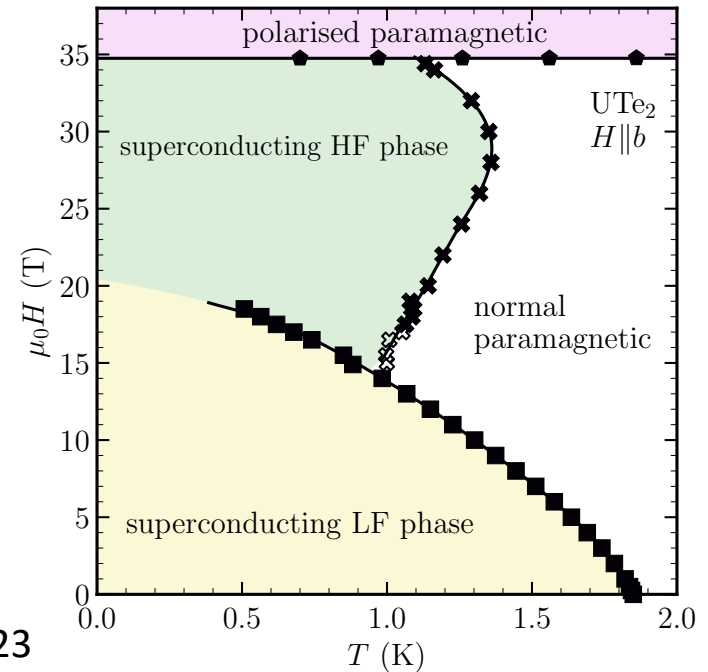
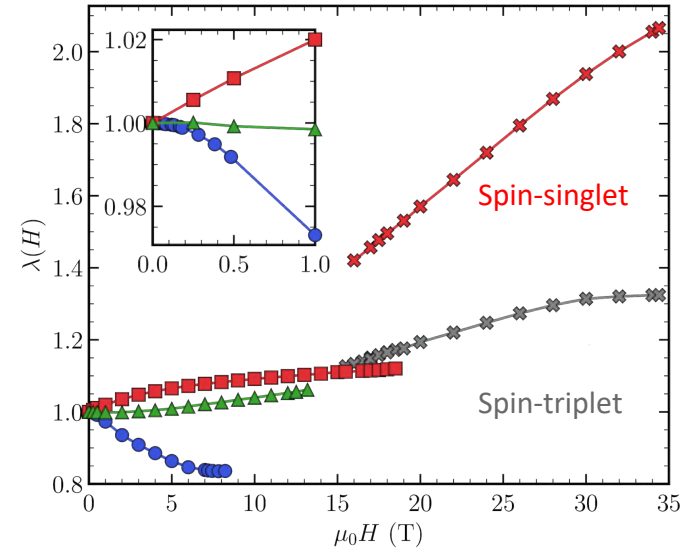
Experimental support for HF-spin singlet

Stronger increase of the pairing required for the spin-singlet scenario

HF phase connected to H_m : $\lambda(H) = \lambda(H/H_m)$
 distribution of $H_m \Rightarrow$ distribution of $T_c = T_c(H, \lambda)$



A. Rosuel et al. PRX 2023

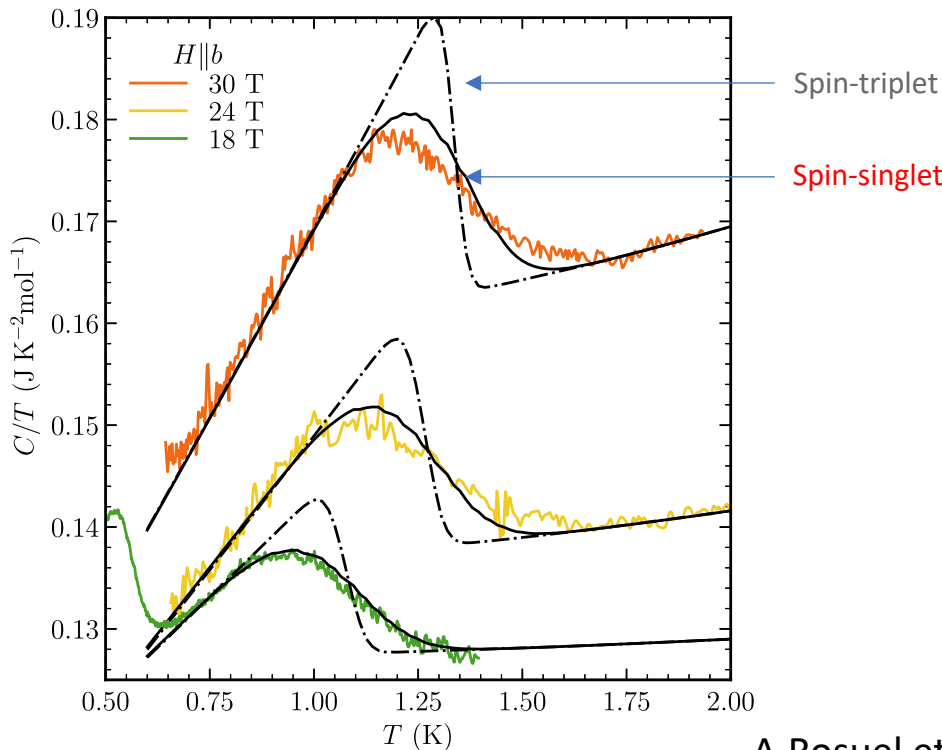


Experimental support for HF-spin singlet

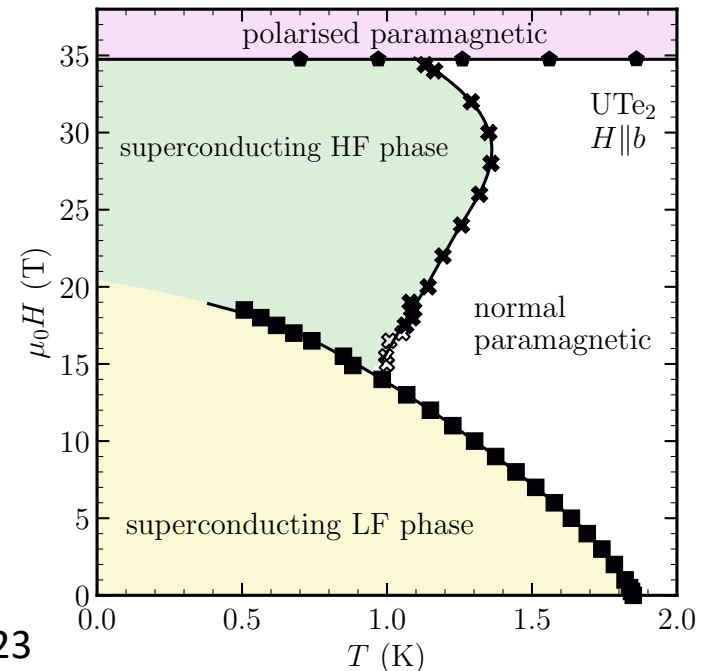
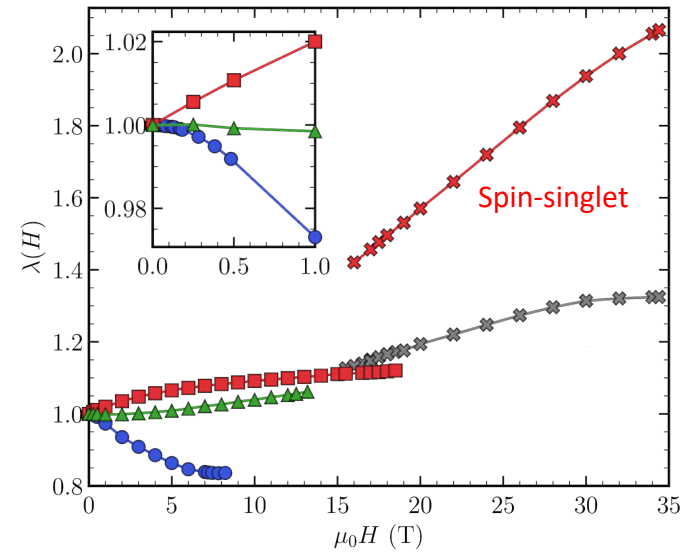
HF phase connected to H_m : $\lambda(H) = \lambda(H/H_m)$
 distribution of $H_m \Rightarrow$ distribution of $T_c = T_c(H, \lambda)$

Singlet Phase (saturating H_{c2}) explains partly
 - The large broadening in the HF phase

$$\left. \frac{\partial T_{sc}}{\partial H_m} \right|_H \propto \left. \frac{\partial T_{sc}}{\partial H} \right|_\lambda$$



A. Rosuel et al. PRX 2023



Perspectives

Possible spin-singlet phase at HF:

Competing pairing interactions

(FM/AF or AF and $\neq Q$ or local interactions ?)

Clear **phase transition** observed between a LF and HF phase.

- Also seen with

$\chi(\omega_L)$ Kinjo et al. PRB 2023

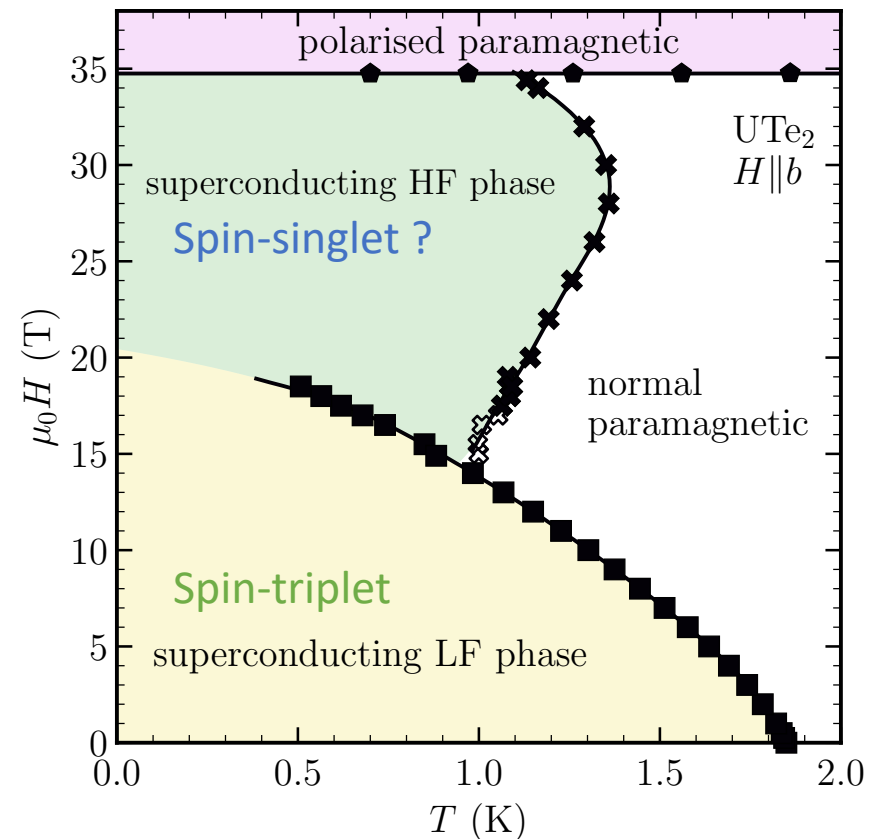
χ Sakai et al PRL 2023

MCE Schönemann et al. ArXiv 2206.06508v1

Open questions:

- Explaining the phase diagram H//b
- Connection with pressure phase diagrams
- Order of transitions
- Theory of field-reinforced phases

And see **Poster Nils Marquardt & Daniel Braithwaite**



9 October (Tutorial), 10 October - 12 October 2023

Topology, spin-orbit interactions and superconductivity in strongly correlated quantum materials under extreme conditions

Grenoble, France

[Registration](#)

Deadline: 30th June 2023

Registration fee: free

60 participants (maximum)

This workshop aims to discuss and exchange the recent progress on strongly correlated quantum materials under extreme conditions such as high field, high pressure, and low temperature between researchers. The topics include topological phenomena, spin-orbit interactions, superconductivity, multipole order, and fermiology.