



# Experimental study of spinon-phonon coupling in spin chain cuprates

*David Msika, Dalila Bounoua, Olivier Demortier  
Francoise Damay, Sylvain Petit*

*LLB*

*Romuald Saint-Martin, David Berardan  
Loreynne Pinsard-Gaudart*

*ICMMO*

*Rolf Heid*

*KIT (Karlsruhe)*

*Alexandre Ivanov, Andrea Piovano  
Frederic Bourdarot*

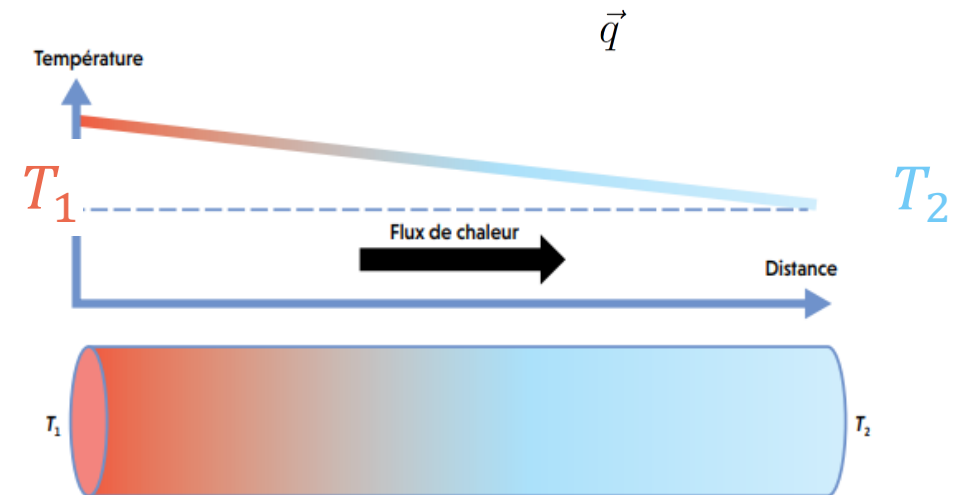
*ILL & CEA-Grenoble*

\*Submitted to PRB, Dec 2022

## Transport coefficients From macroscopic...

Perturbation	Response	Coefficient (tensor)
Magnetic field	Magnetization	Magnetic susceptibility $\mu$
Electric potential	Electric current	Electric conductivity $\sigma$
Temperature gradient	Heat flow	Heat conductivity $\kappa$

$$\vec{q} = -\kappa \vec{\nabla} T$$



## Transport coefficients ... to microscopics

Insulators : no contribution from electrons

$$\kappa \approx \frac{1}{\Omega} \sum_{k,s} C_{k,s} v_{k,s} \ell_{k,s}$$

mean free path

$$v \tau = \ell$$

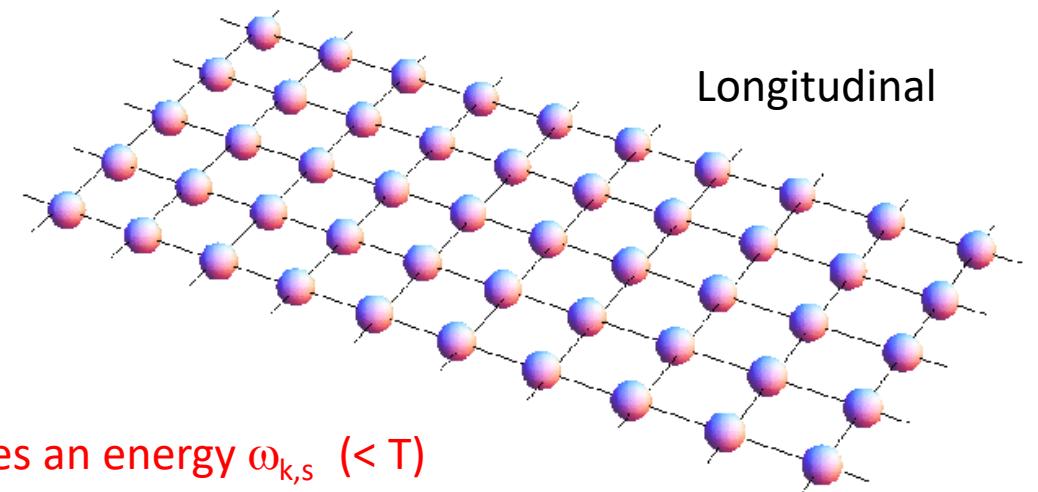
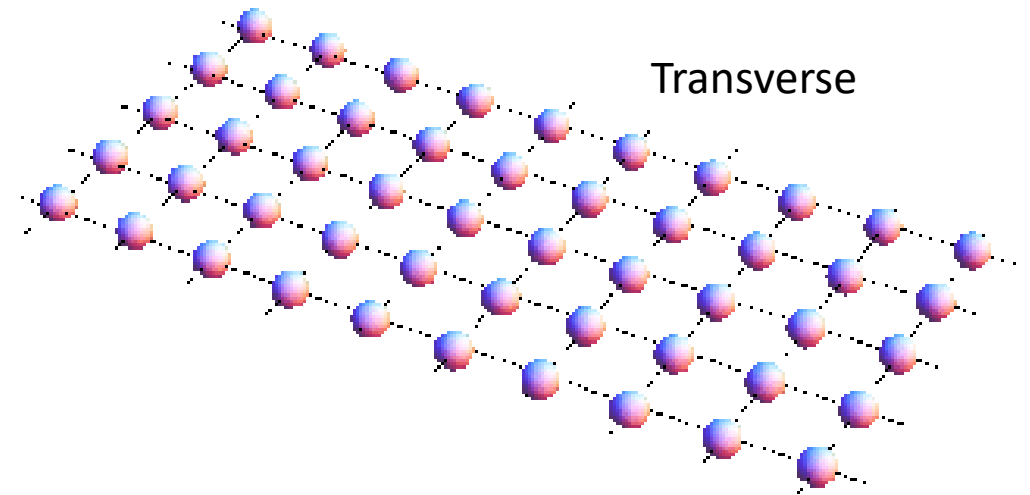
Relaxation time

$$v_{k,s} = \frac{\partial \omega_{k,s}}{\partial \vec{k}}$$

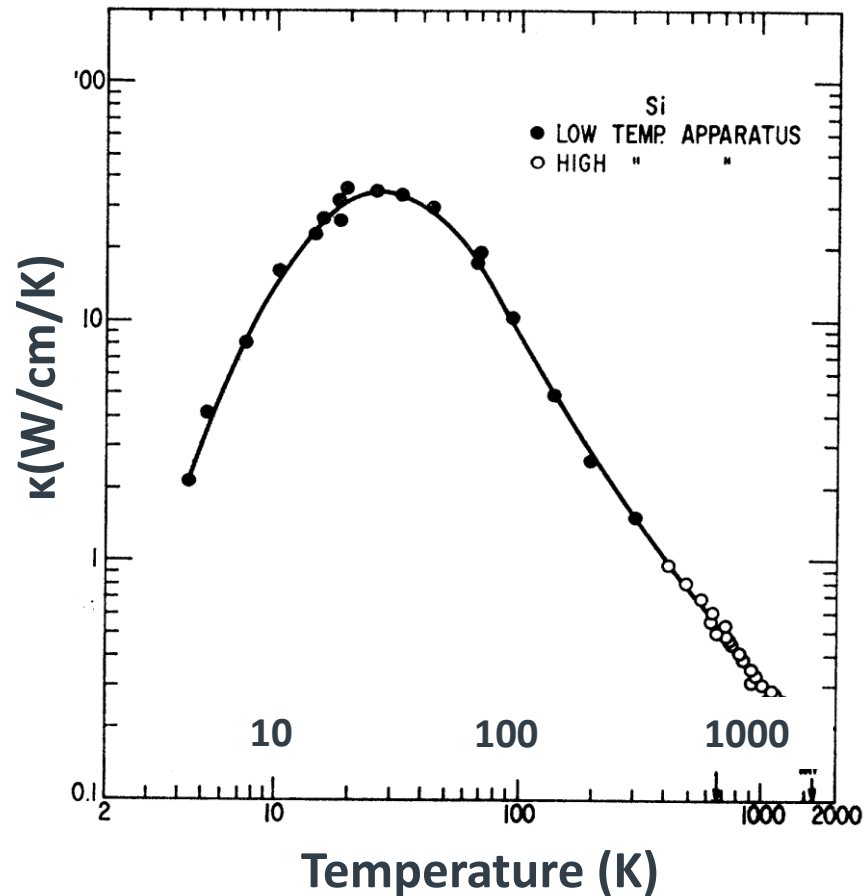
Velocity of the particles

$$C_{k,s} = k_B \frac{x^2 e^x}{(e^x - 1)^2}, \quad x = \omega_{k,s}/T$$

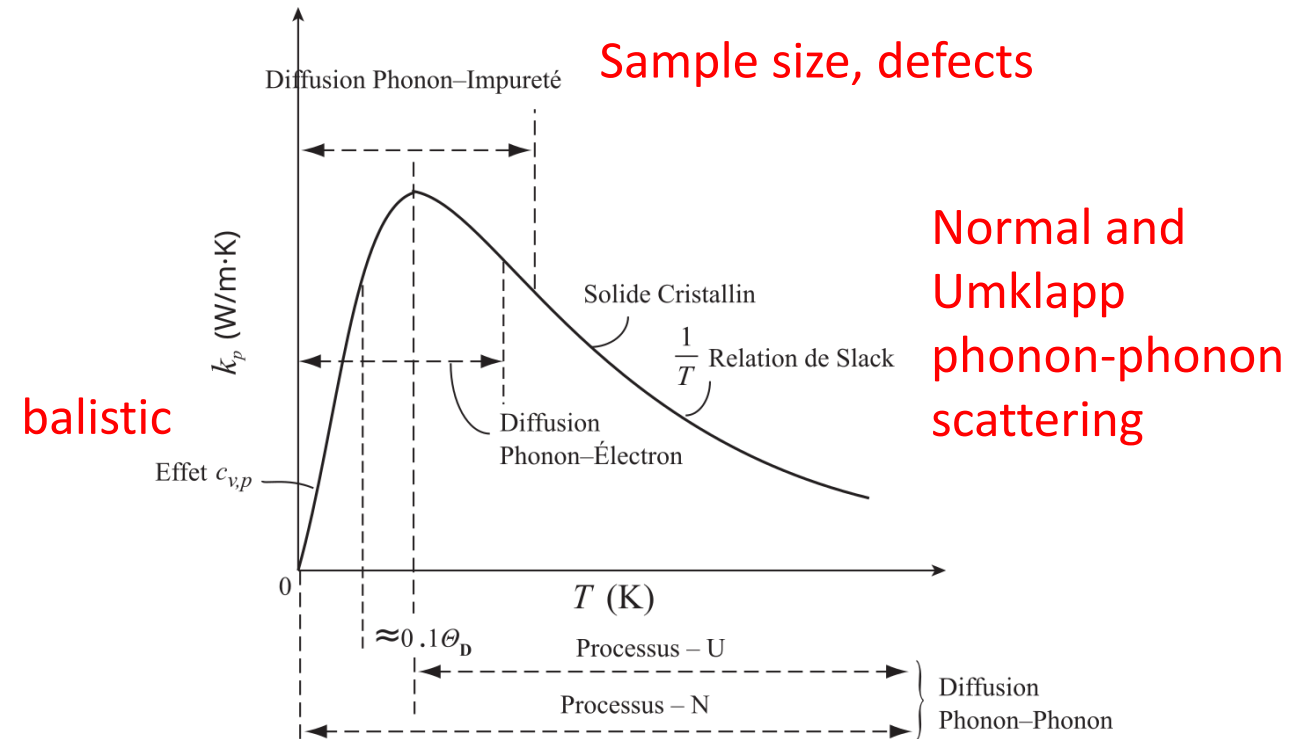
Each populated mode contributes an energy  $\omega_{k,s}$  ( $< T$ )  
Acoustic modes only !!



## Ex : heat conductivity in Silicon



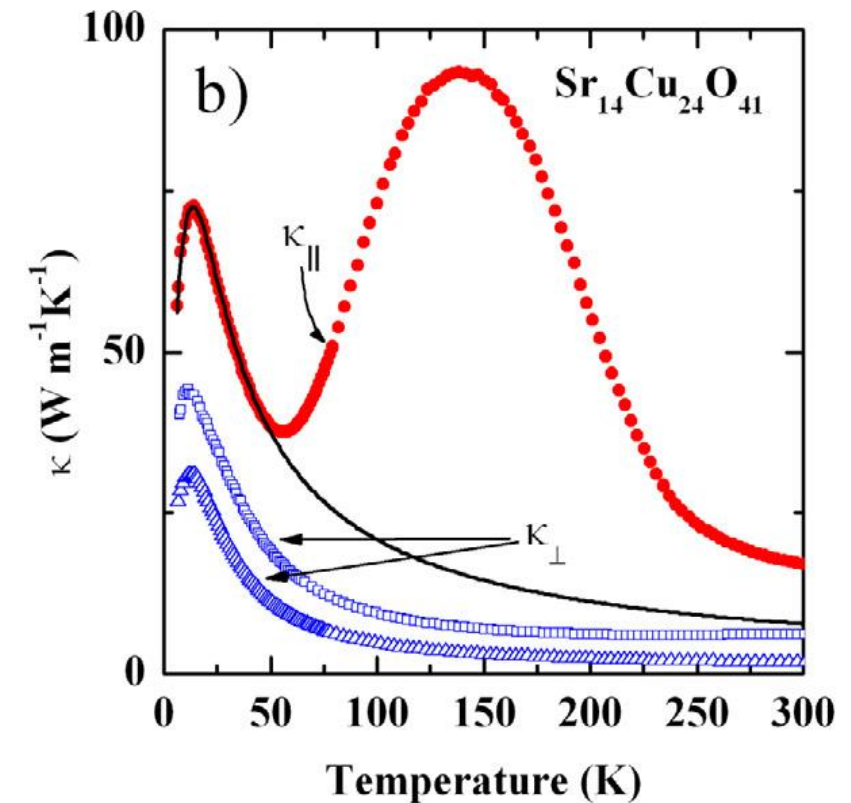
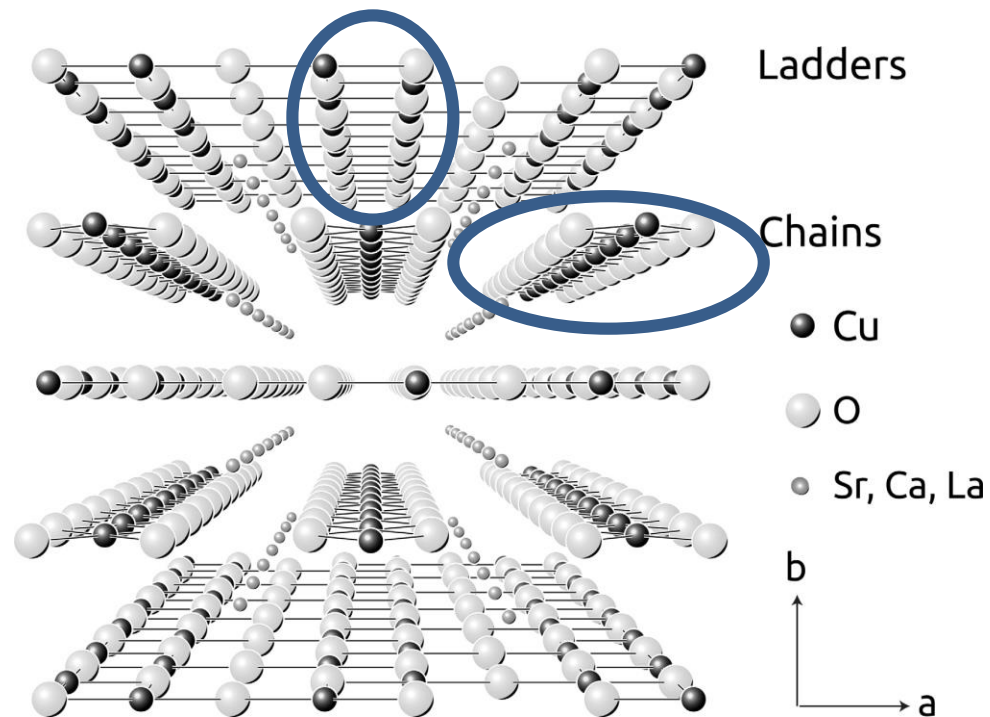
$$\tau_{tot}^{-1} = \tau_S^{-1} + \tau_D^{-1} + \tau_N^{-1} + \tau_U^{-1}$$



Glassbrenner & Slack, Phys. Rev. 134, A1058 (1964)  
 Kaviani, Heat transfert Physics (2012)

# New materials : $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$

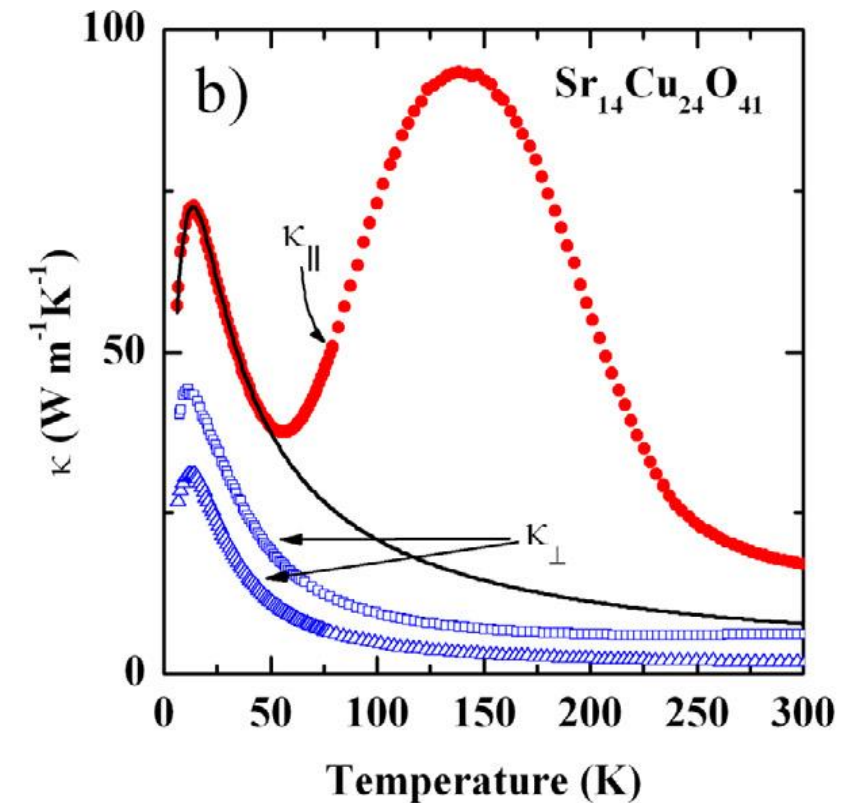
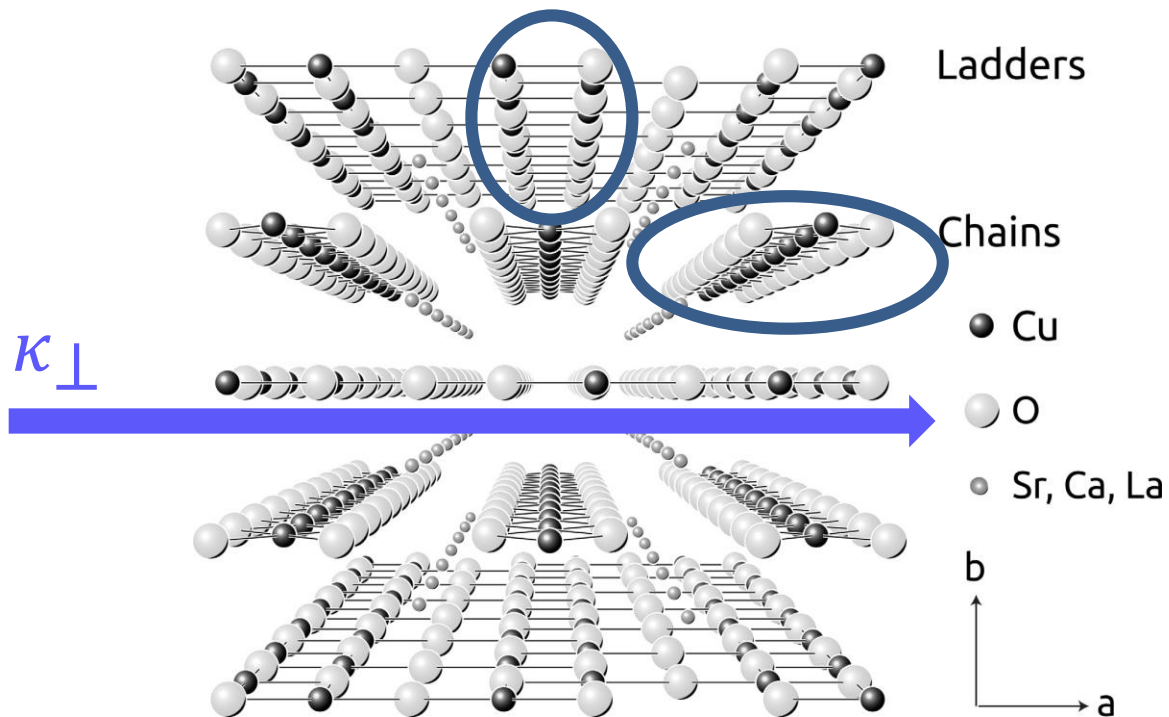
In addition to phonons, emergent particles propagate along chains and ladders (spin  $\frac{1}{2}$   $\text{Cu}^{2+}$ ) and participate to heat transport.  $\kappa$  is strongly anisotropic.



Hess et al., Physics Reports 811 (2019)

# New materials : $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$

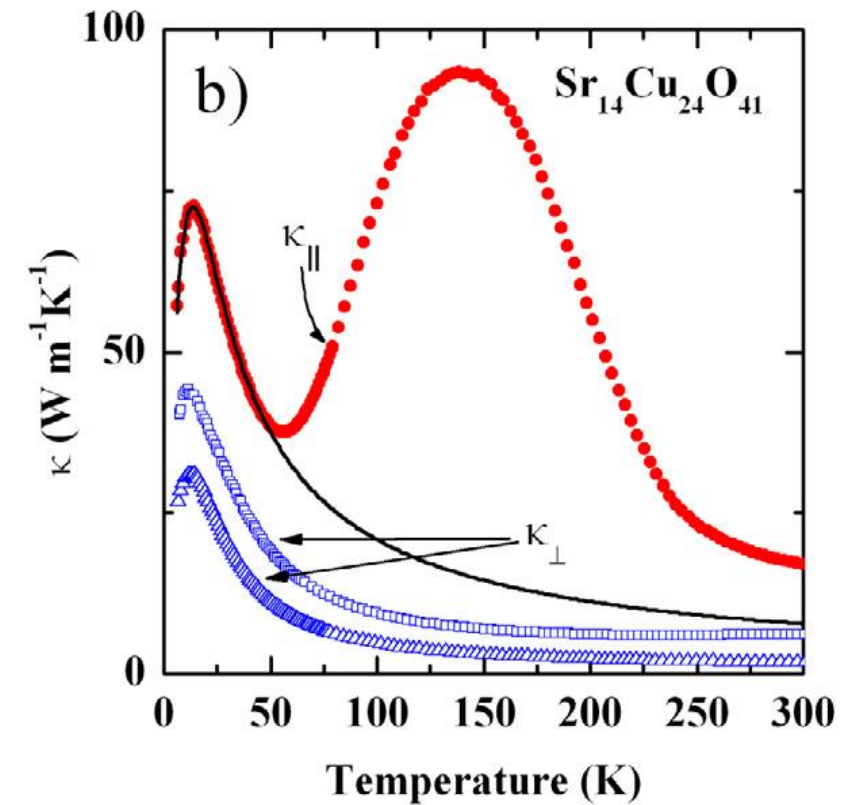
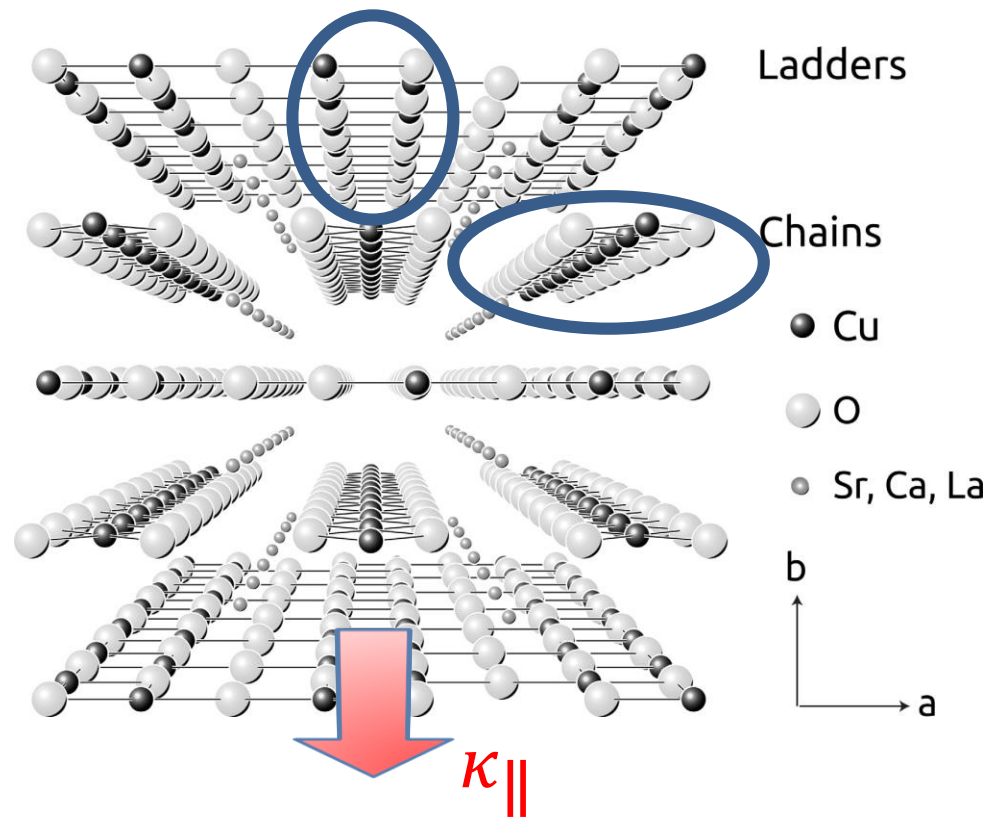
In addition to phonons, emergent particles propagate along chains and ladders (spin  $\frac{1}{2}$   $\text{Cu}^{2+}$ ) and participate to heat transport.  $\kappa$  is strongly anisotropic.



Hess et al., Physics Reports 811 (2019)

# New materials : $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$

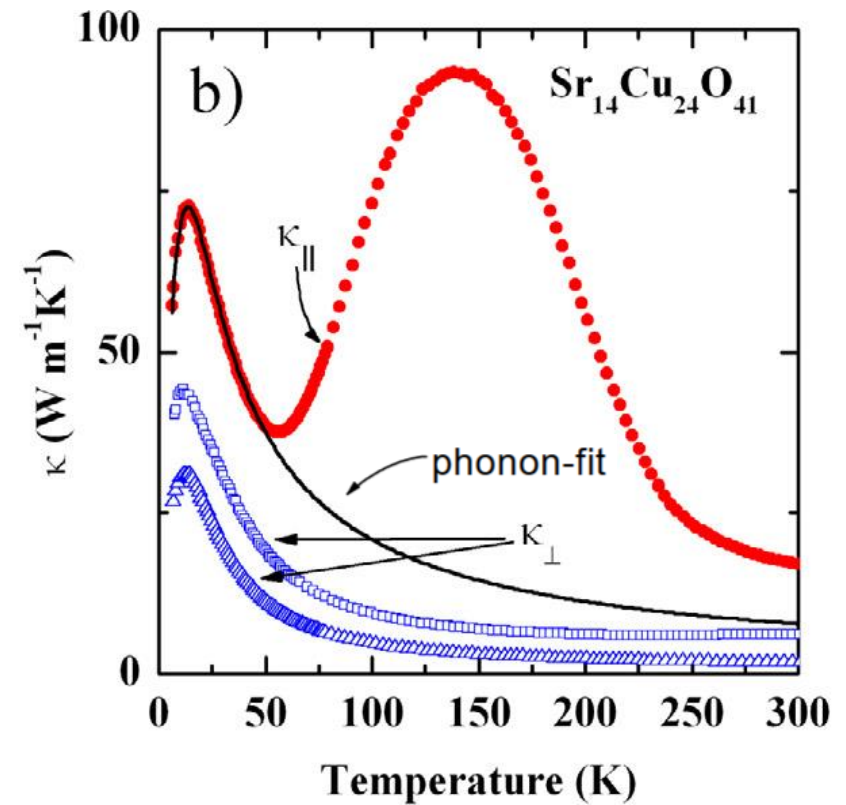
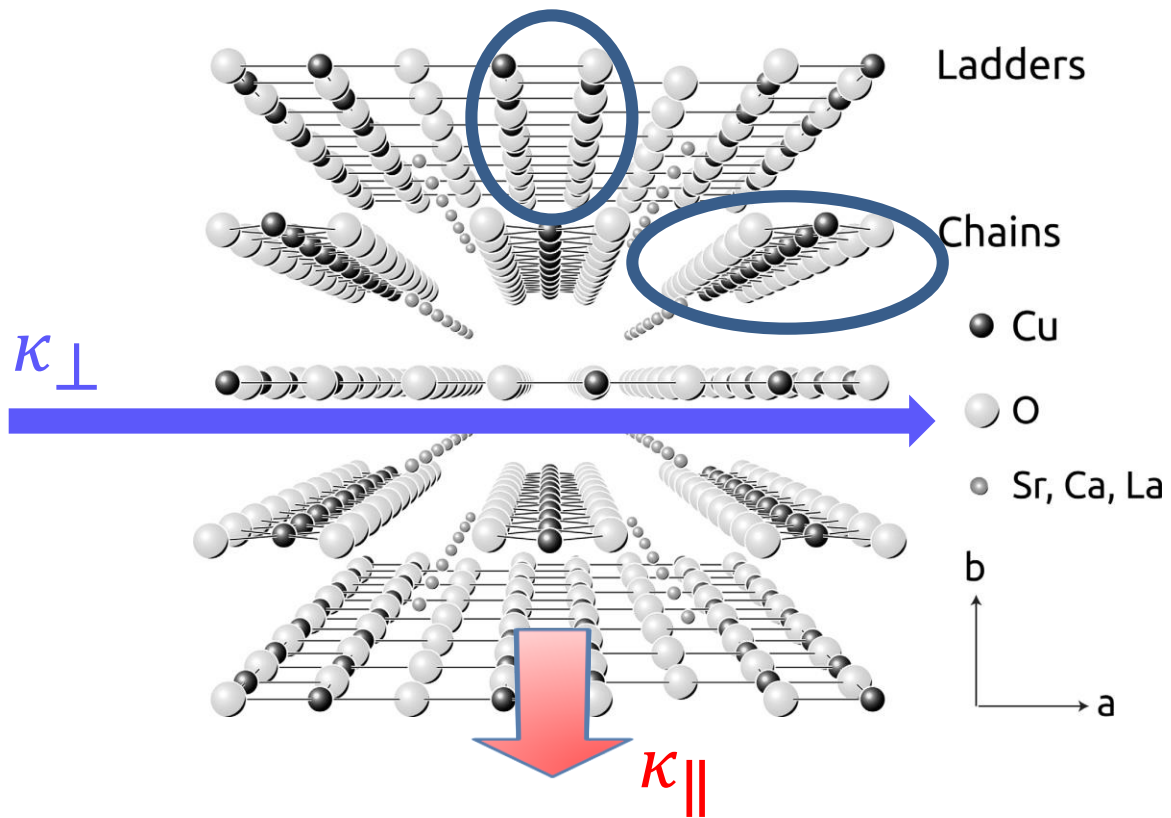
In addition to phonons, emergent particles propagate along chains and ladders (spin  $\frac{1}{2}$   $\text{Cu}^{2+}$ ) and participate to heat transport.  $\kappa$  is strongly anisotropic.



Hess et al., Physics Reports 811 (2019)

# New materials : $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$

$$\kappa_c = \kappa_{ph} + \kappa_{mag} \longrightarrow \kappa_{mag} = \kappa_{\parallel} - \kappa_{\perp}$$

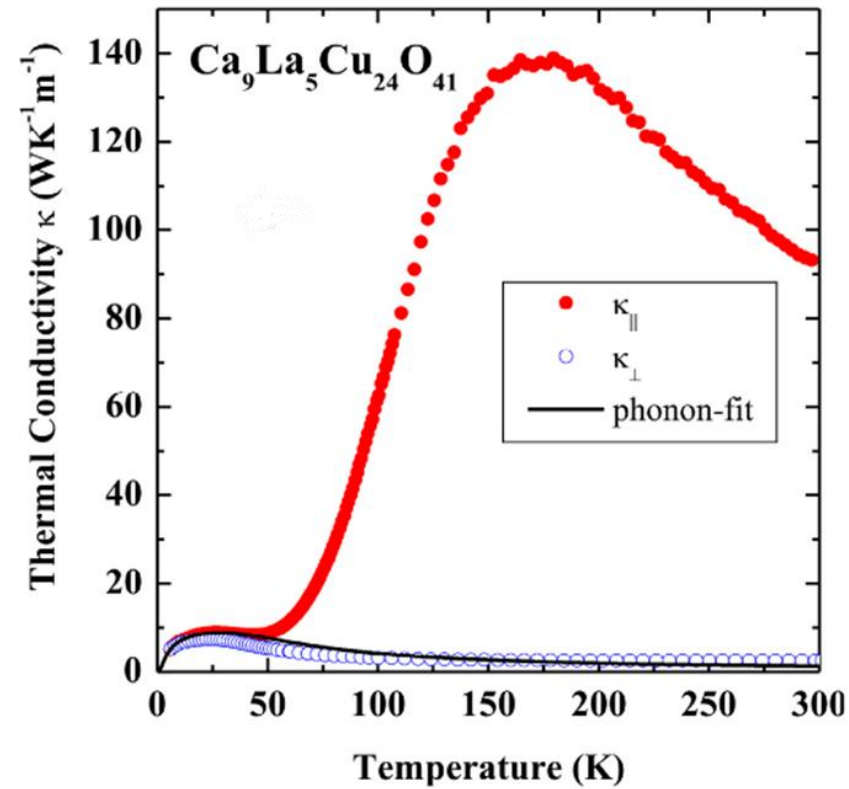
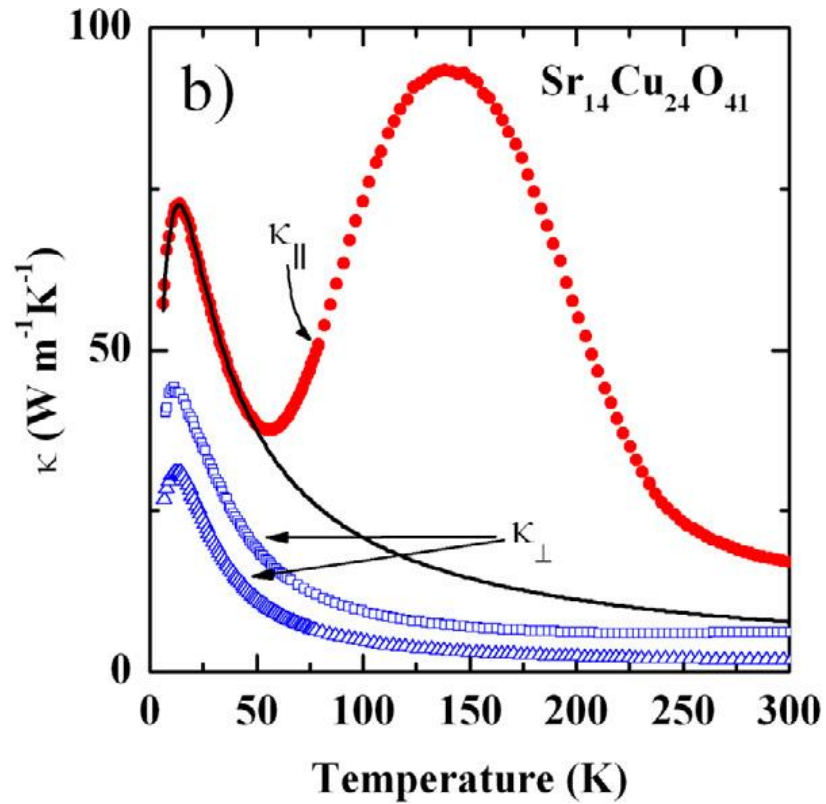


Hess et al., Physics Reports 811 (2019)



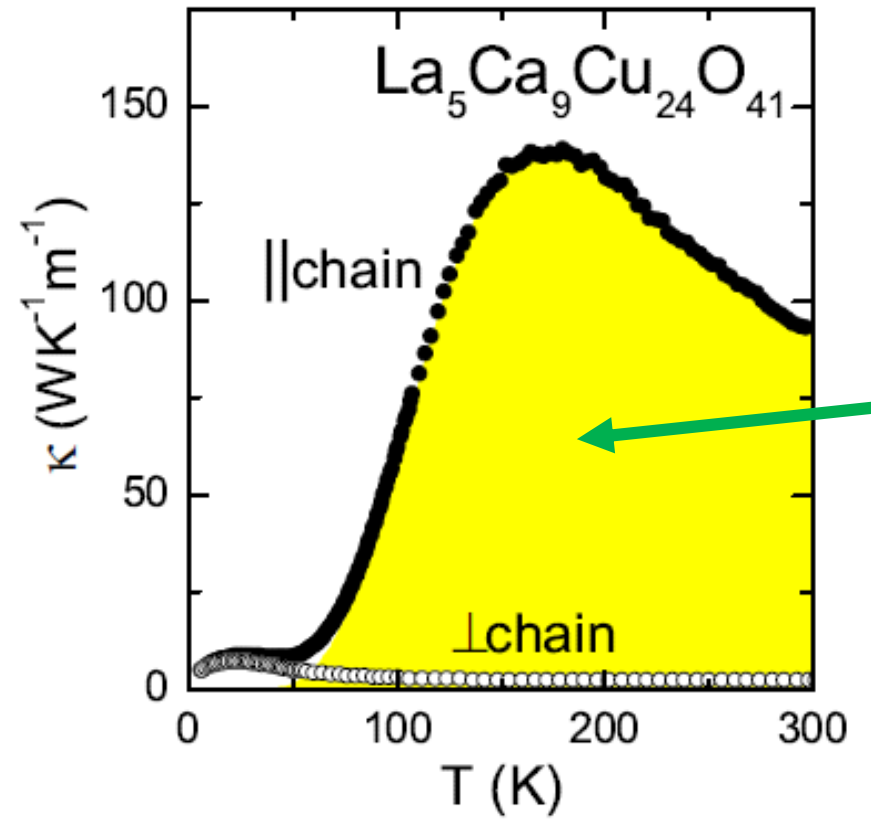
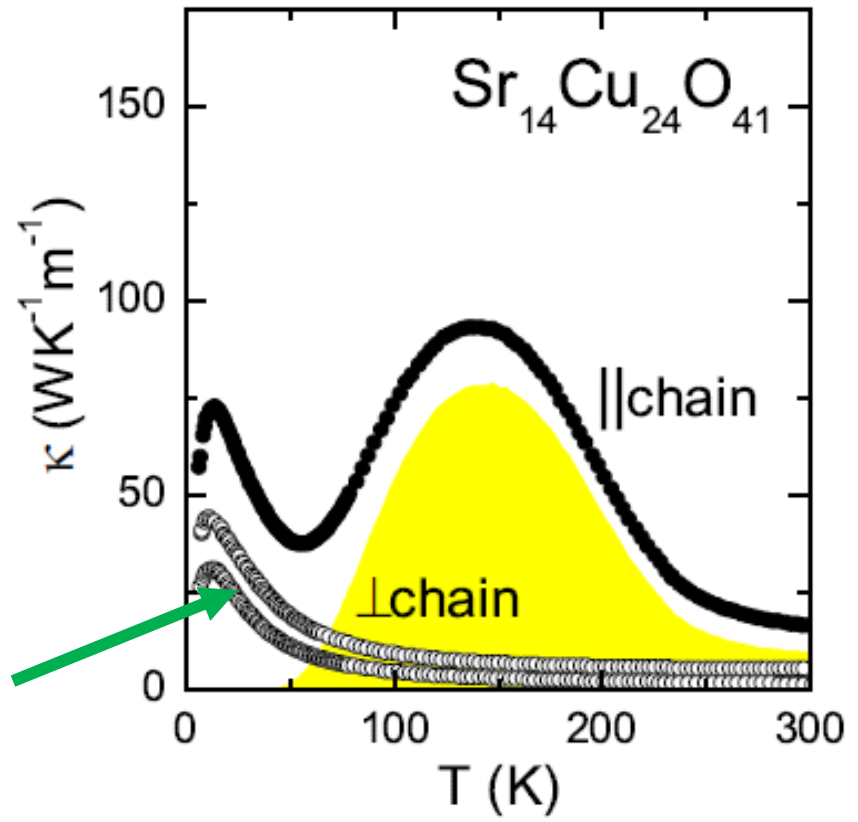
but also  $\text{Ca}_9\text{La}_5\text{Cu}_{24}\text{O}_{41}$

$$\kappa_c = \kappa_{ph} + \kappa_{mag} \longrightarrow \kappa_{mag} = \kappa_{\parallel} - \kappa_{\perp}$$



Hess et al., Physics Reports 811 (2019)

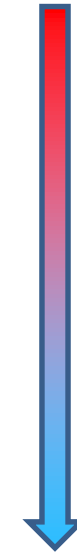
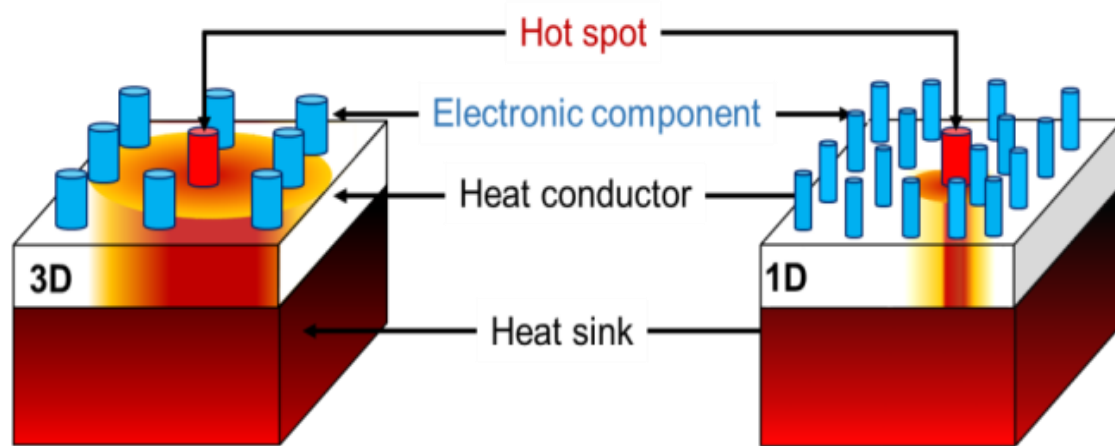
$$\kappa_c = \kappa_{ph} + \kappa_{mag} \longrightarrow \kappa_{mag} = \kappa_{\parallel} - \kappa_{\perp}$$



Phonons

Unconventional magnetic excitations

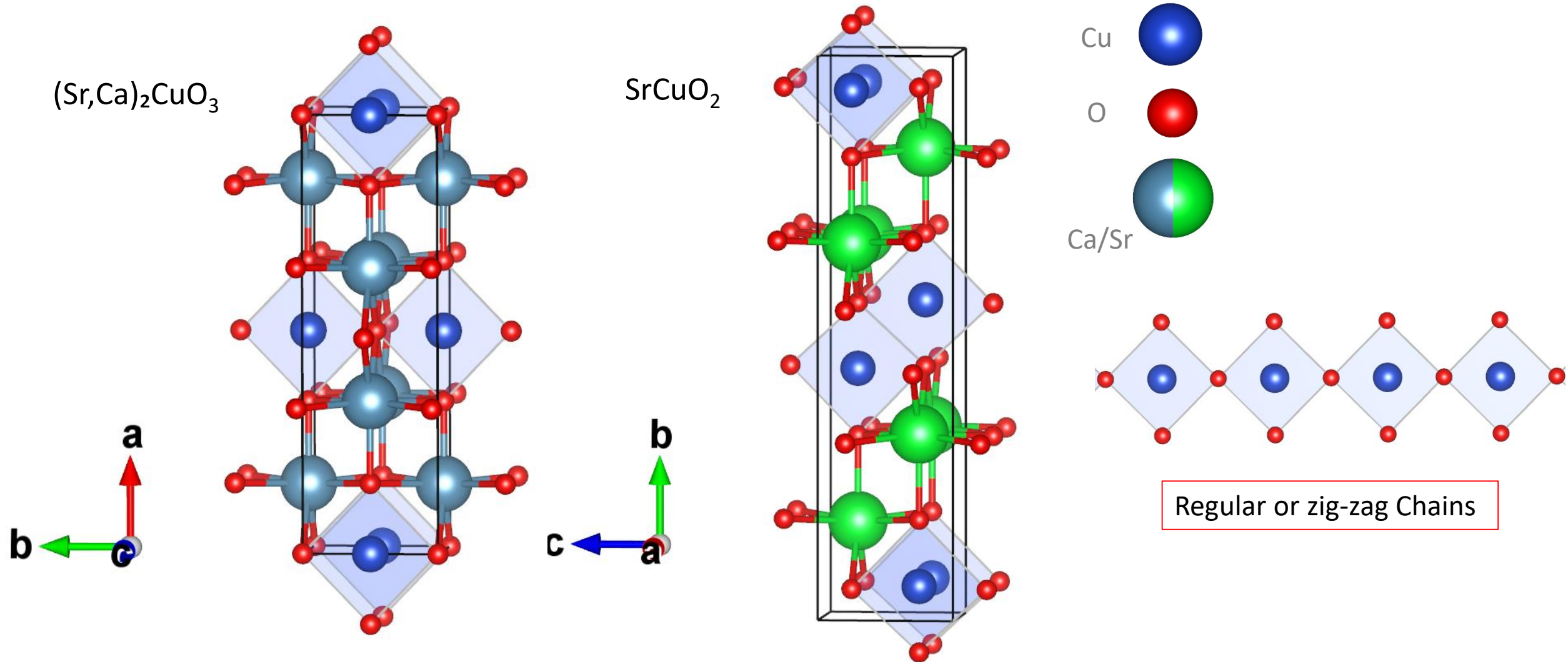
# Applications ?



Heat is evacuated along  
1D highways !!

D. Bounoua, Phd thesis (2017)

# Spin chains cuprates $\text{SrCuO}_2$ , $\text{Sr}_2\text{CuO}_3$ , $\text{Ca}_2\text{CuO}_3$

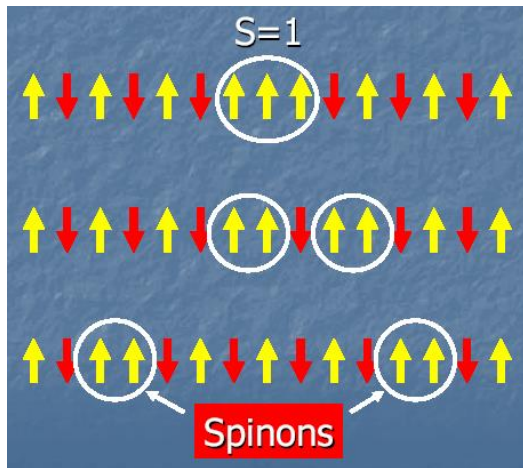


# Spinons in 1D chains

$$H_{\text{XXZ}} = J \sum_i \epsilon (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y) + S_i^z S_{i+1}^z$$

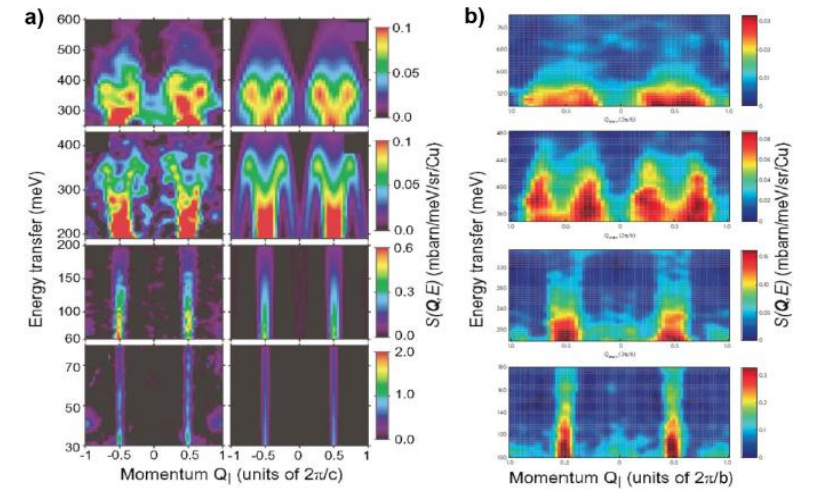
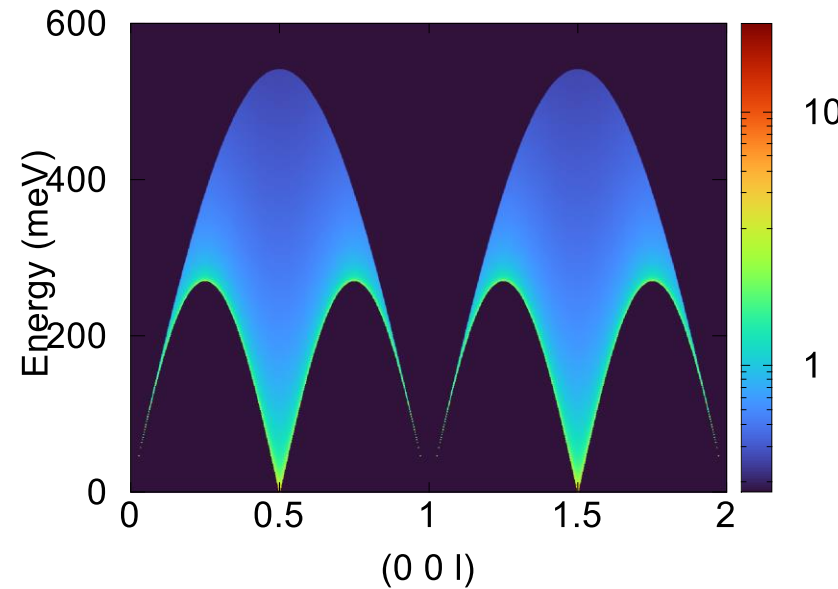
Spinons are very peculiar spin 1/2 excitations typical of 1D XXZ spin chains

≈ domain walls



Courtesy F. Mila

Visible by means of neutron scattering (2-spinons continuum)

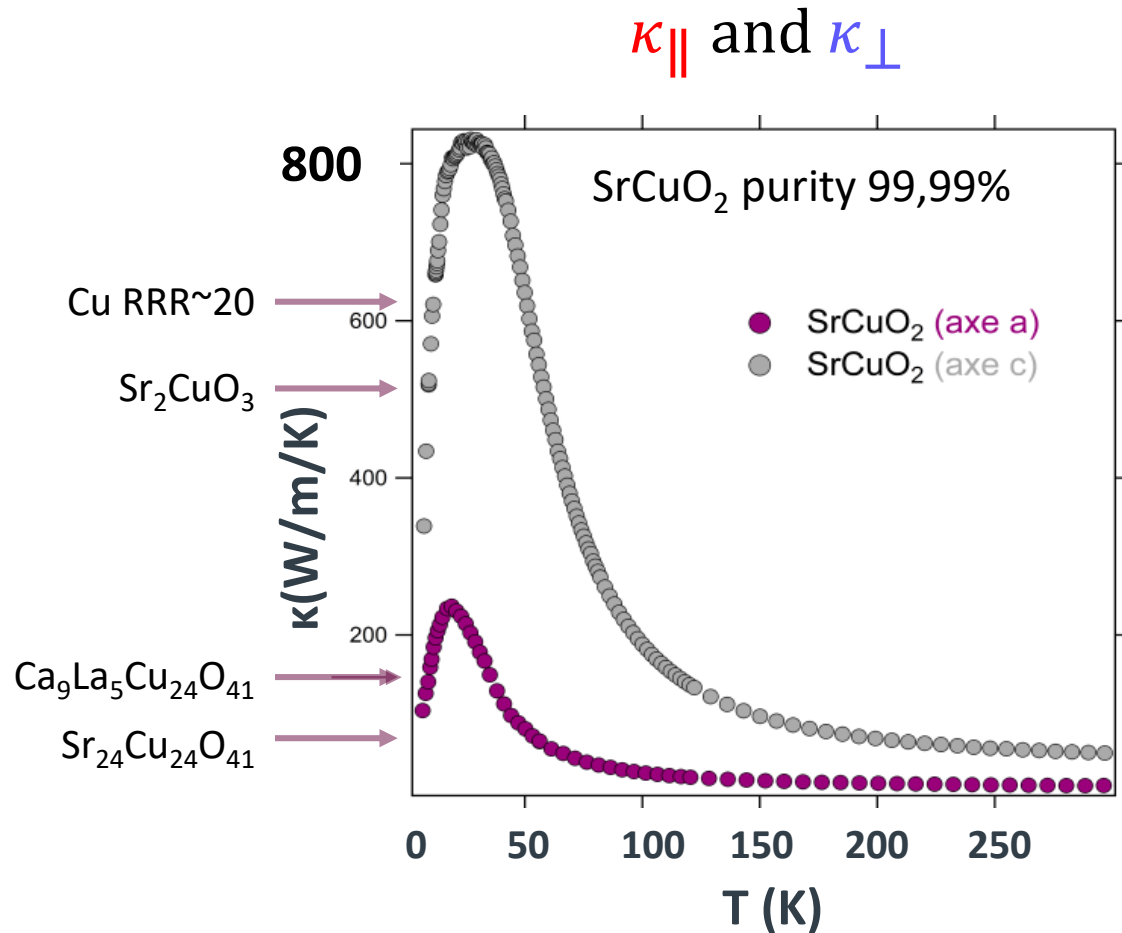


Zaliznyak et al., Phys. Rev. Lett. 93, 087202 (2004)

**Huge exchange  
coupling :  
J ≈ 200 meV ≈ 2000 K**

# Spinons in 1D chains

Hlubek et al., J. Stat. Mech. : Theory and Experiment (2012)



- Thermal conductivity is anisotropic
- Large maximum (HUGE J)
- Strongly decreases with increasing temperature

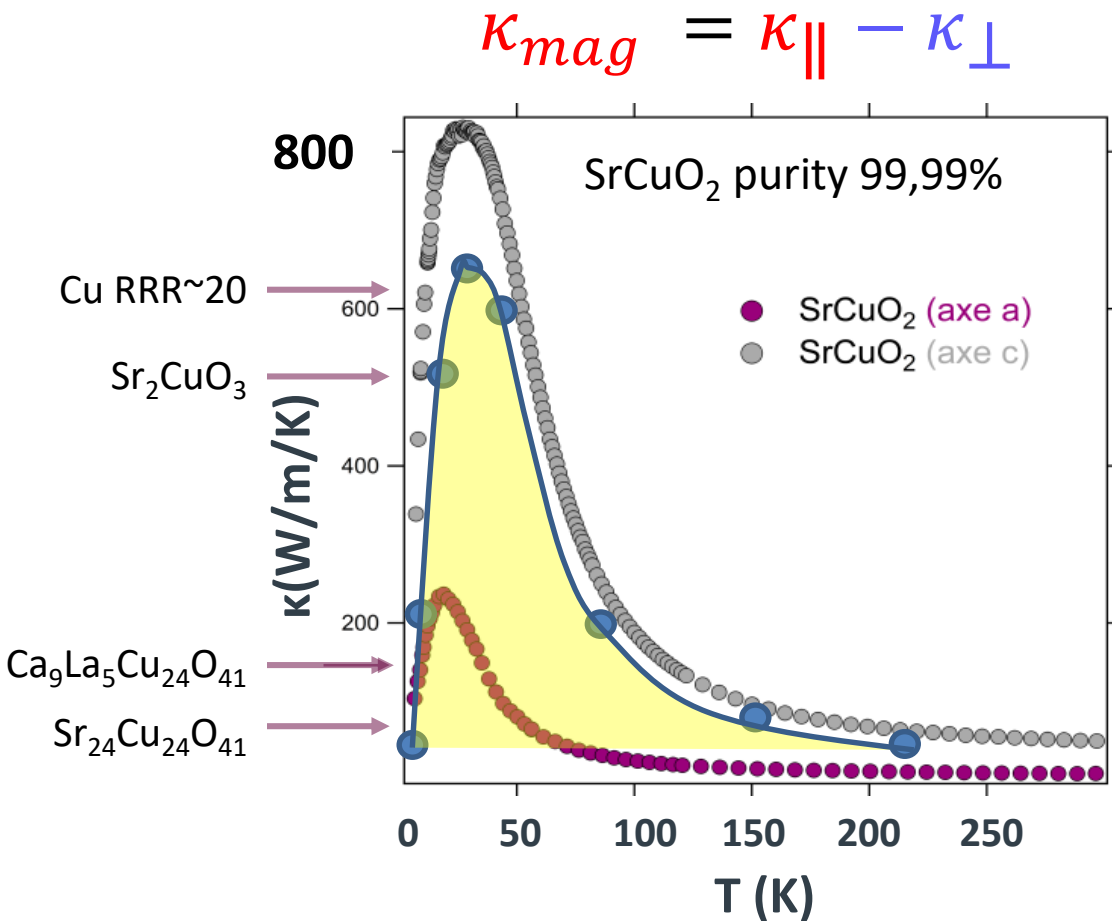
# Spinons in 1D chains

Hlubeck et al., J. Stat. Mech. : Theory and Experiment (2012)

$$\mathcal{H} = \sum_{\langle ij \rangle} J(\mathbf{r}_i - \mathbf{r}_j) \mathbf{S}_i \cdot \mathbf{S}_j,$$

Weak coupling

Strong coupling

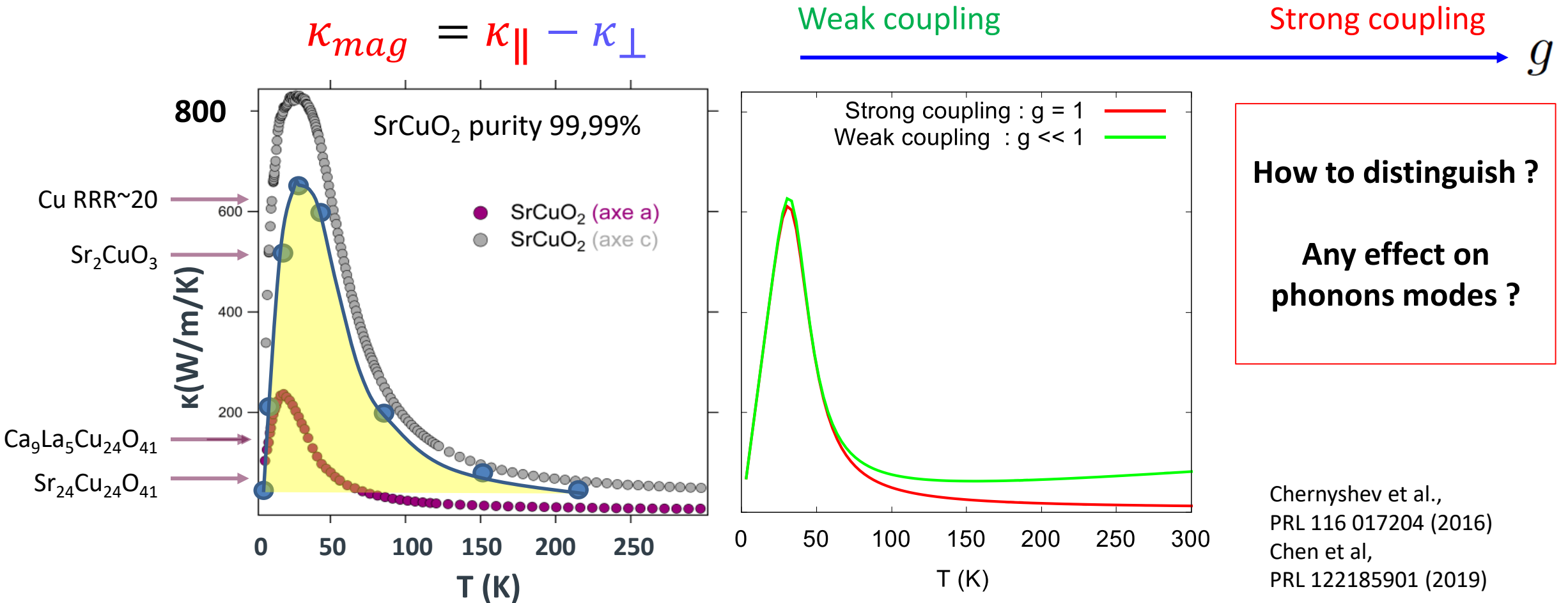


**Two models,  
two different limits**

# Spinons in 1D chains

Hlubek et al., J. Stat. Mech. : Theory and Experiment (2012)

$$\mathcal{H} = \sum_{\langle ij \rangle} J(\mathbf{r}_i - \mathbf{r}_j) \mathbf{S}_i \cdot \mathbf{S}_j,$$



**How to distinguish ?**

**Any effect on phonons modes ?**

Chernyshev et al.,  
PRL 116 017204 (2016)  
Chen et al.,  
PRL 122185901 (2019)



# I. Sample synthesis & characterization (ICMMO)

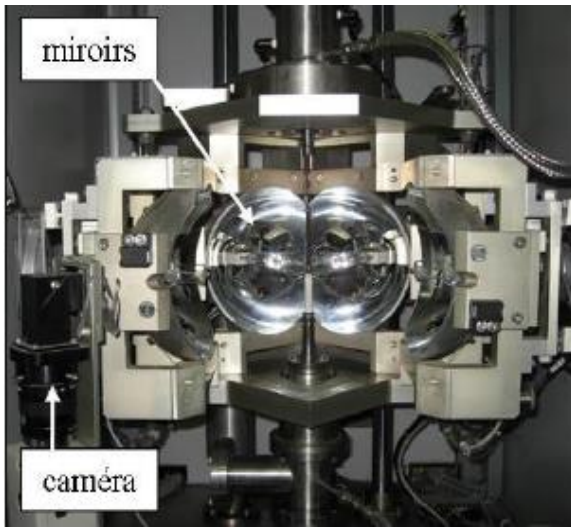
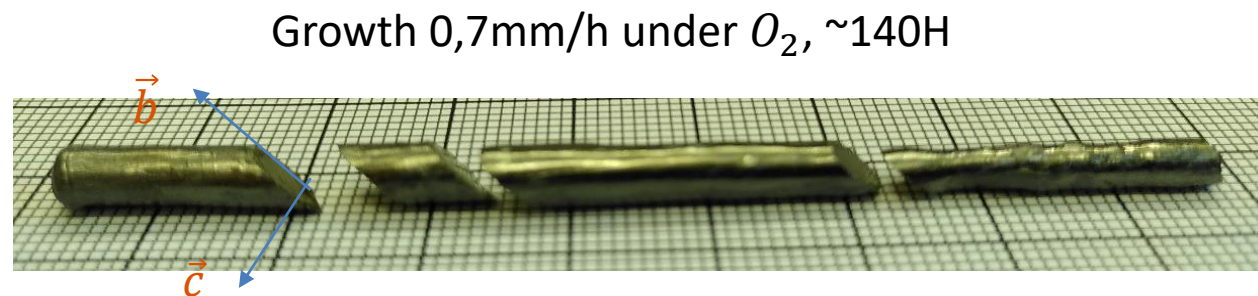


Image furnace @ ICMMO

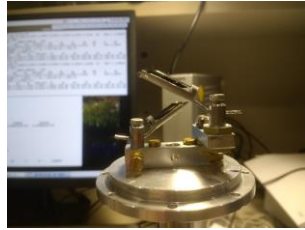


$\text{Sr}_2\text{CuO}_3$  Single crystals



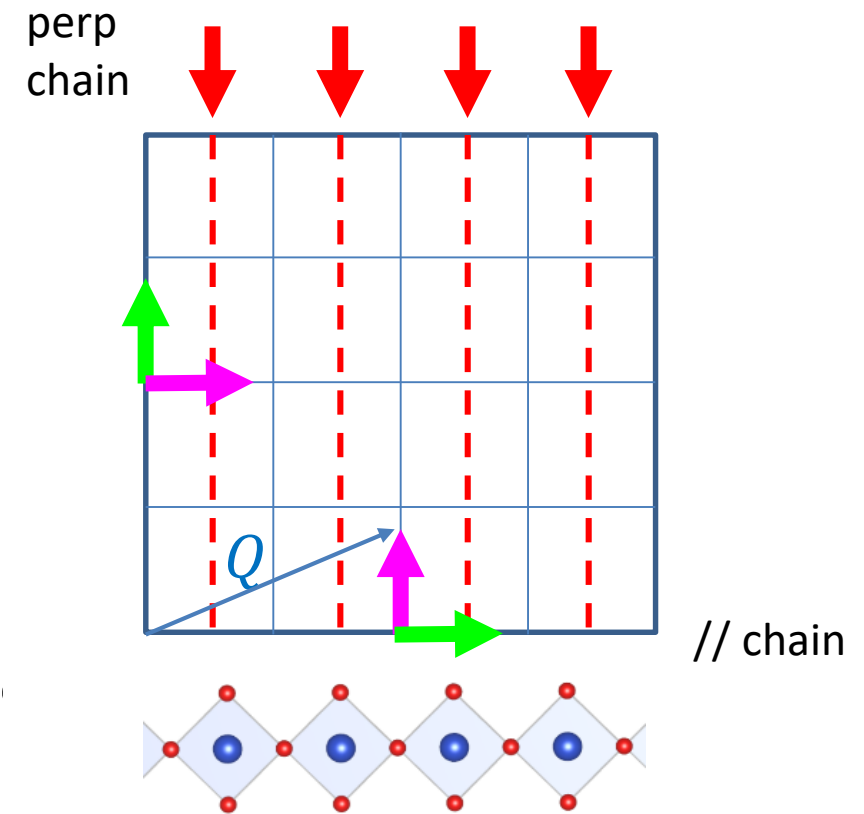
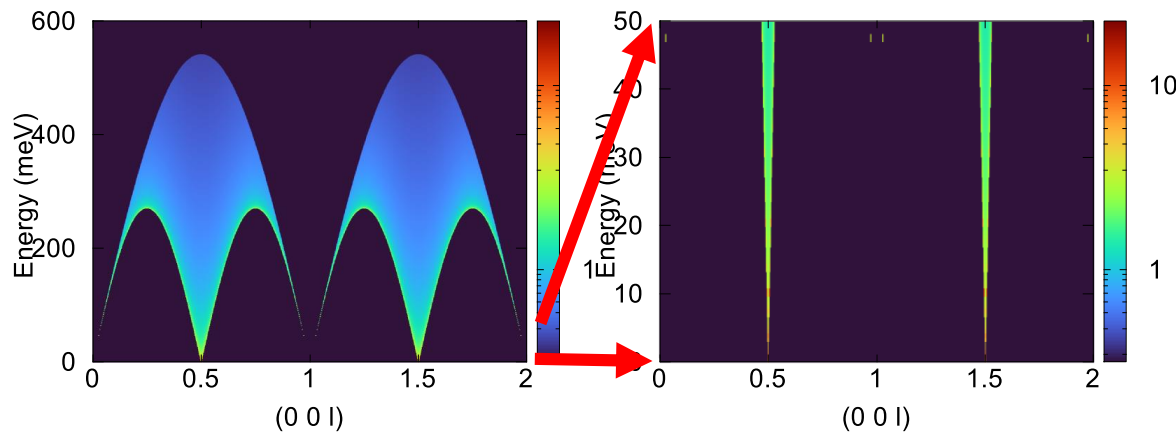
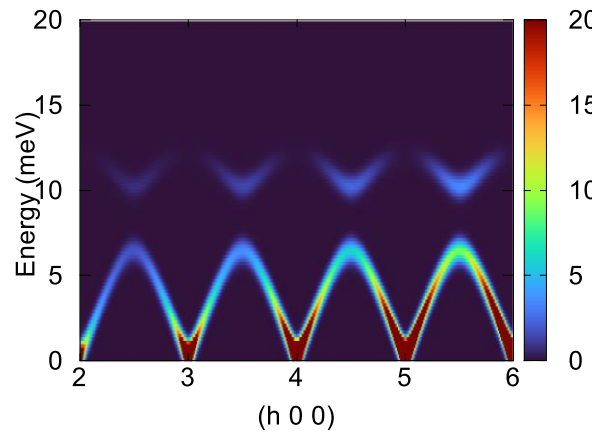
$\text{Ca}_2\text{CuO}_3$  Single crystals

# II. Inelastic neutron scattering (ILL & LLB-Orphée)

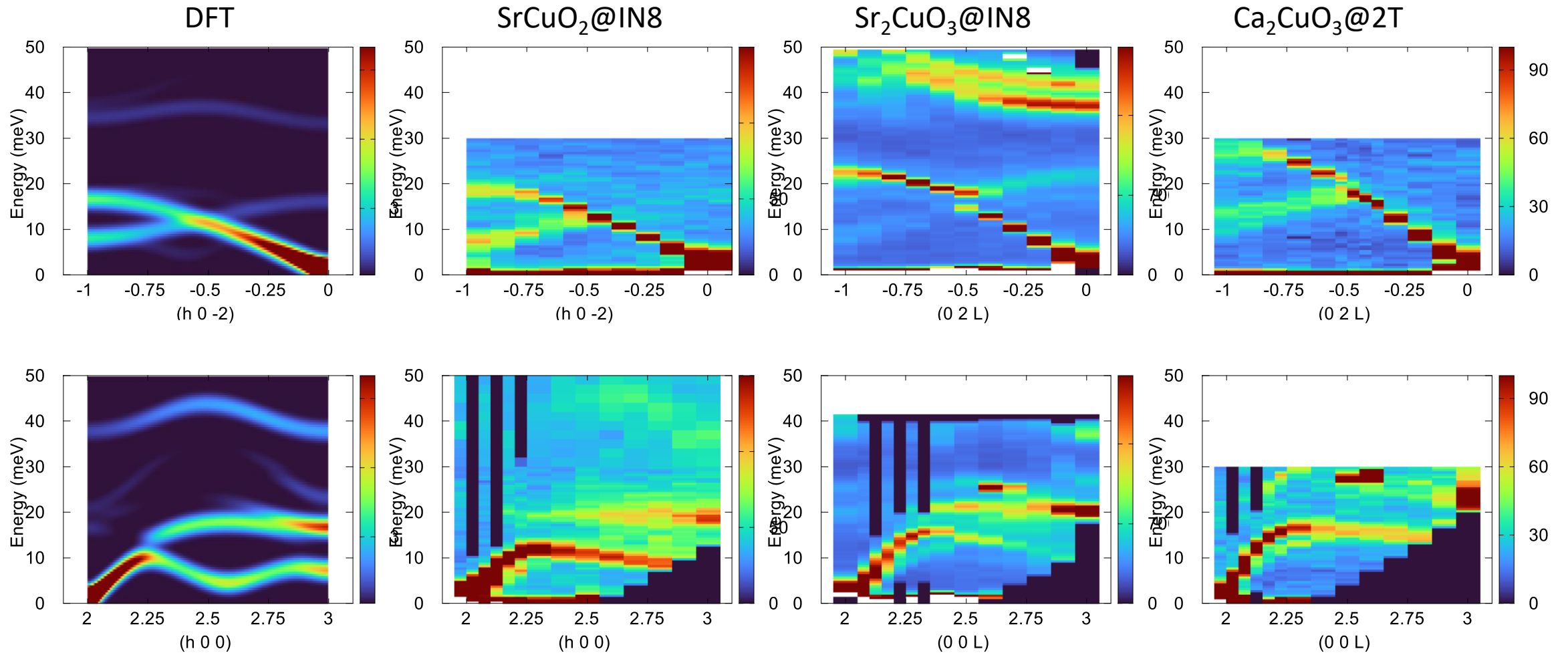


Map out  $(Q, \omega)$  space to reveal phonons and spinons. Keep in mind that spinons are :

- 1D
- And much faster than phonons  $J \gg \omega_{ph}$

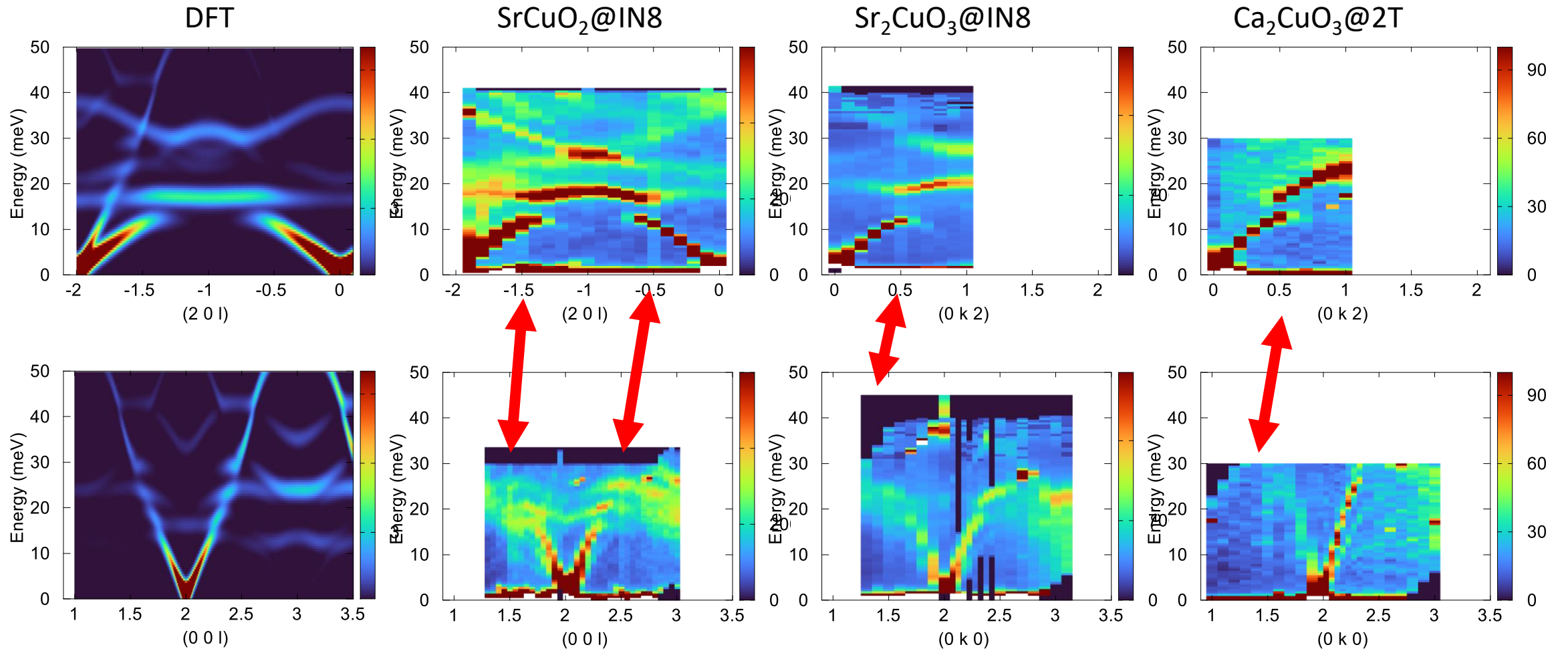


# Survey of phonons propagating **perp** to the chains



Larger # of avoided crossings + « Soft » modes, all predicted by DFT

# Survey of phonons propagating **along** the chains

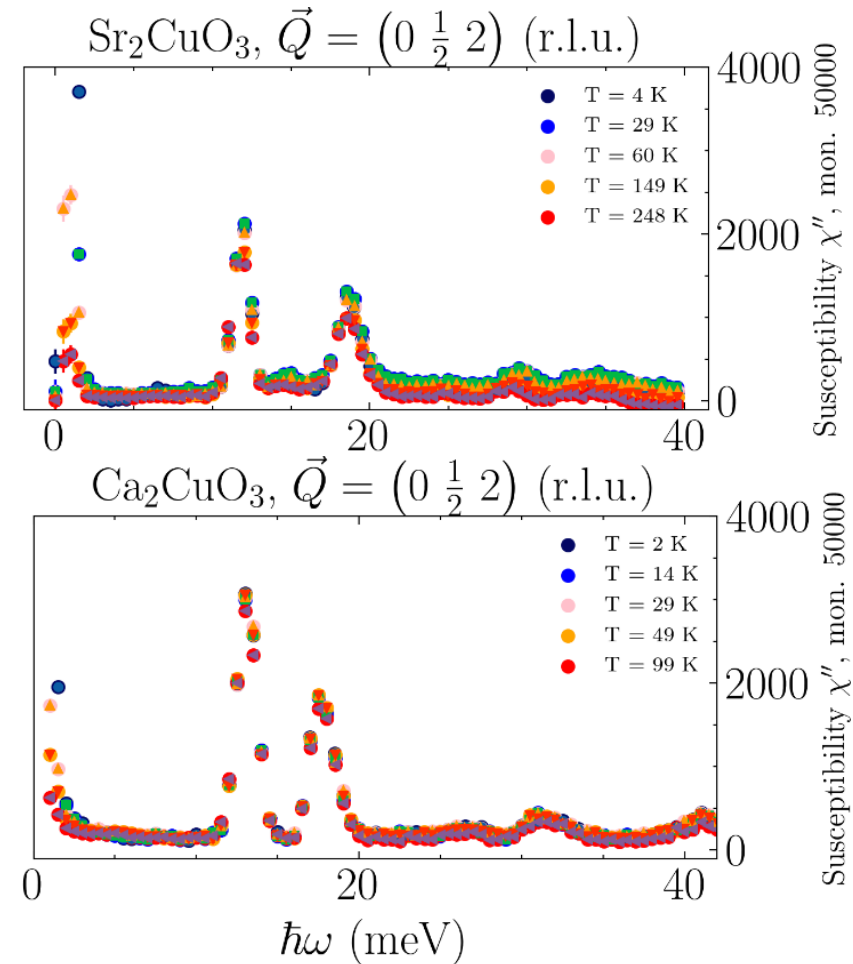
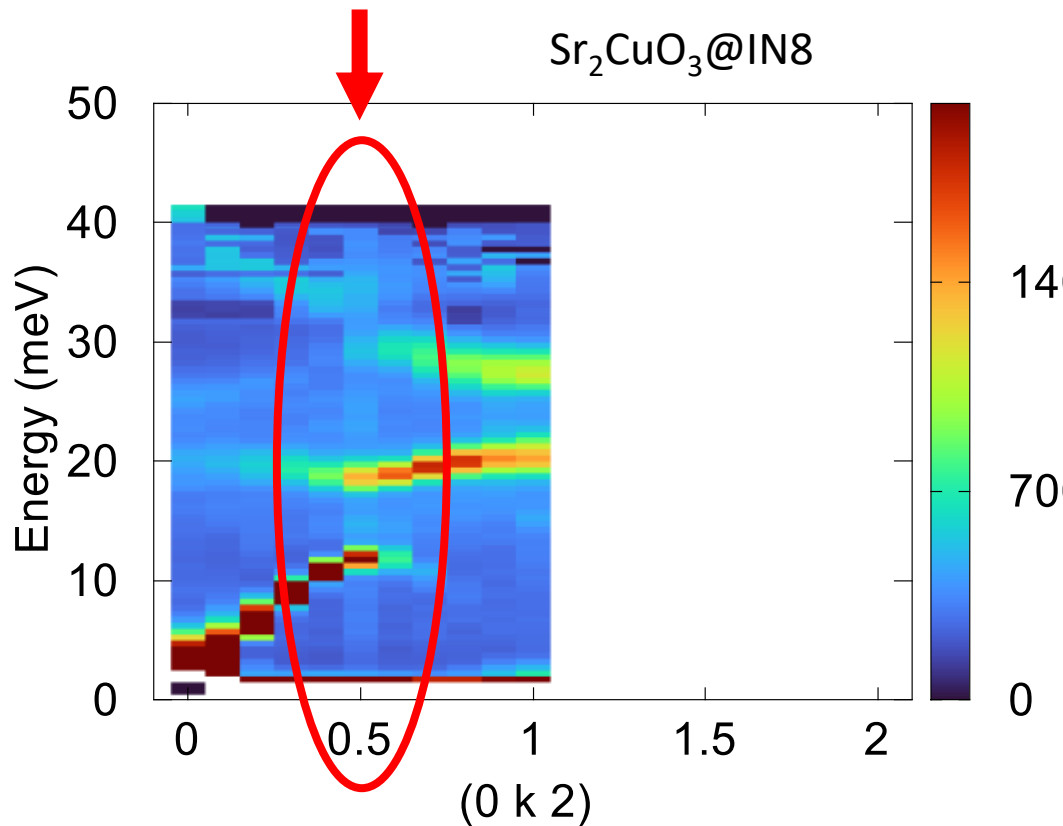


Larger # of avoided crossings + « Soft » modes, all predicted by DFT

# When phonon **cross** the 2-spinons continuum :

Any significant broadening? NO ...

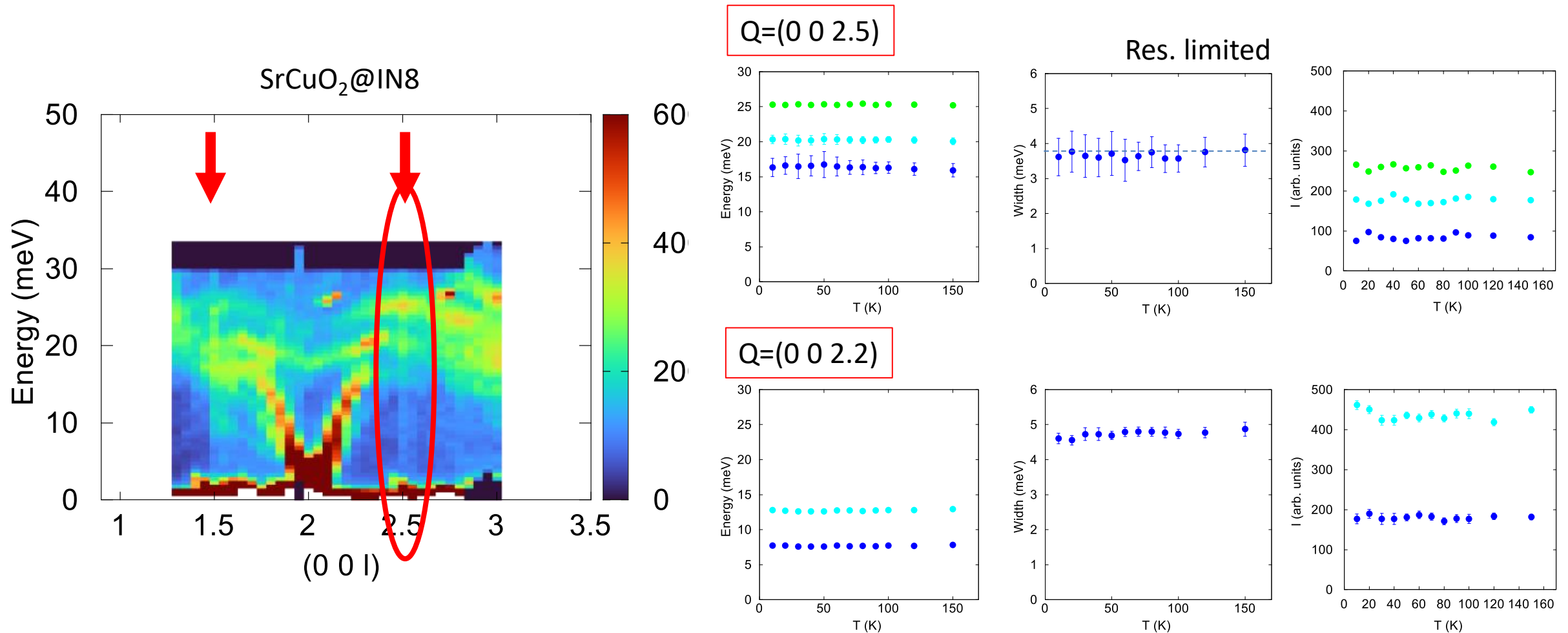
Any significant evolution with increasing temperature ? NO ...



# When phonon **cross** the 2-spinons continuum :

Any broadening? NO ...

Any significant evolution with increasing temperature ? NO ...



- Complicated lattice dynamics, with **avoided crossings** + **low energy modes**, indicating that the structure is soft in certain directions.
- These features are essentially **predicted by DFT**.
- NO remarkable anomalies as a function of temperature (**within experimental resolution**), suggesting that the spin-phonon coupling is **WEAK**.

## Perspectives

- Improve energy resolution, theoretical background for phonon linewidth ?
- Going beyond the simple expression  $\kappa_{mag} = \kappa_{\parallel} - \kappa_{\perp}$





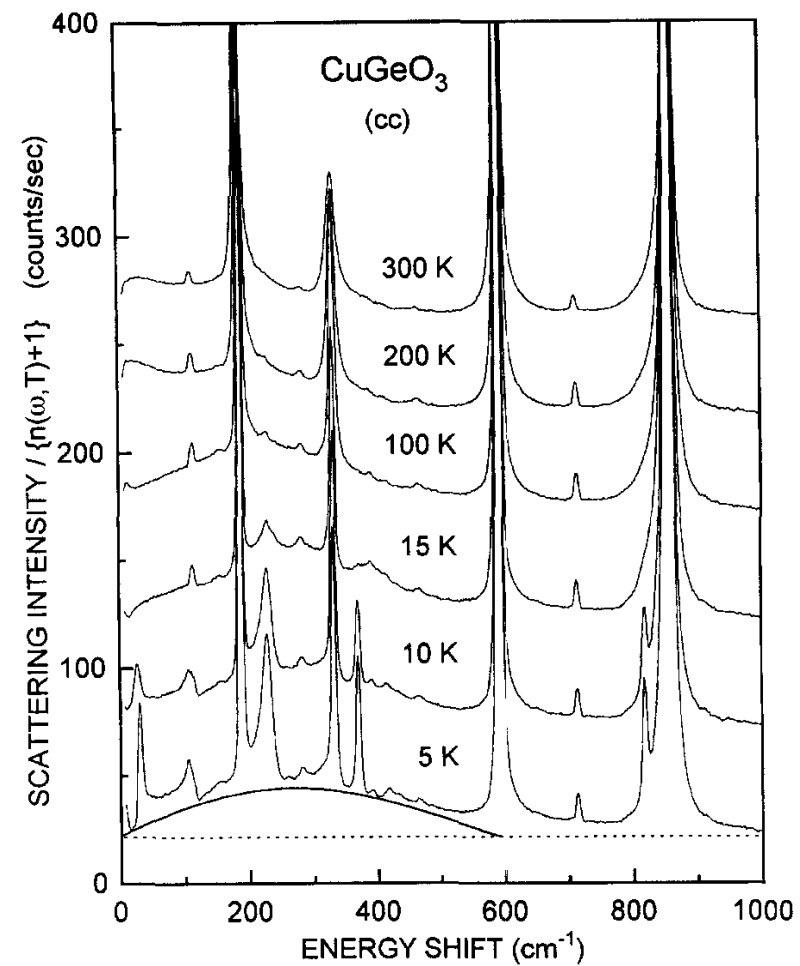
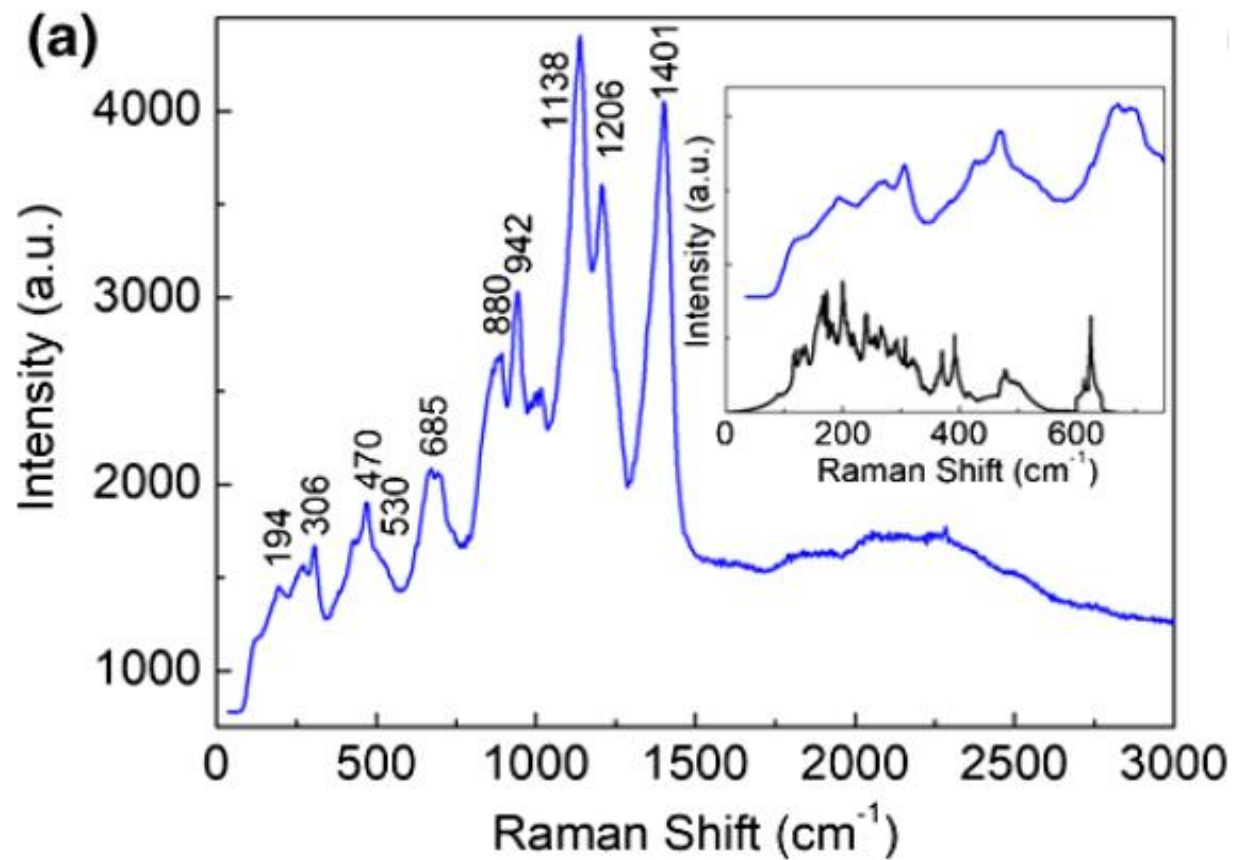
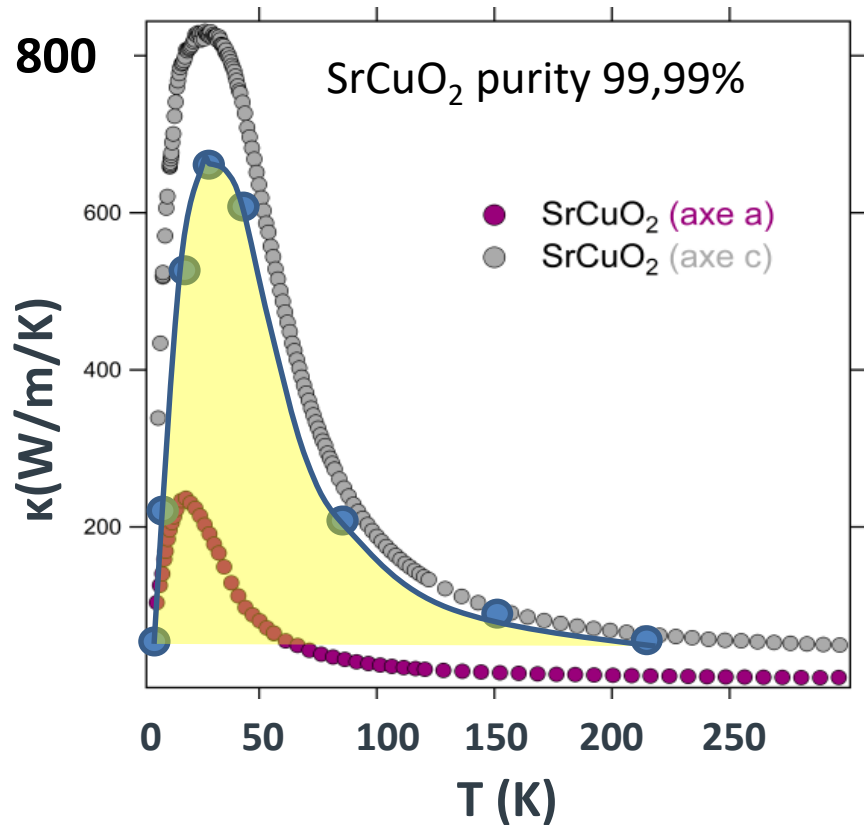


Fig. 3. Temperature dependence of low energy parts of (cc) Raman spectra of  $\text{CuGeO}_3$ .

# Magnetic degrees of freedom in spin chains

$$\mathcal{H} = \sum_{\langle ij \rangle} J(\mathbf{r}_i - \mathbf{r}_j) \mathbf{S}_i \cdot \mathbf{S}_j,$$

$$\kappa \approx \frac{\pi}{3} n_s k_B \frac{k_B T}{\hbar} \ell$$



Hlubeck et al., J. Stat. Mech. : Theory and Experiment (2012)

Spinons scatter on optical phonons (essentially at rest)

$$\frac{1}{\ell} \approx \frac{1}{\ell_d} + \frac{2g^2 J}{a} \frac{1}{T \sinh \omega_o/T}$$

Weak coupling

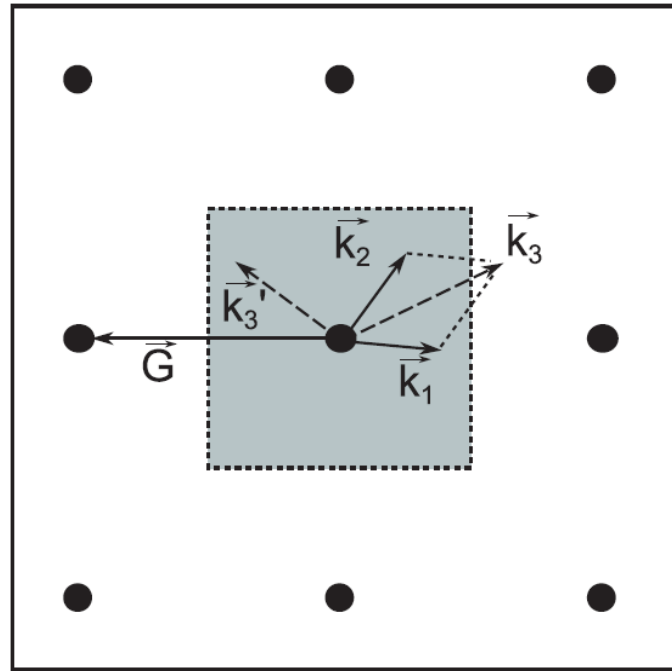
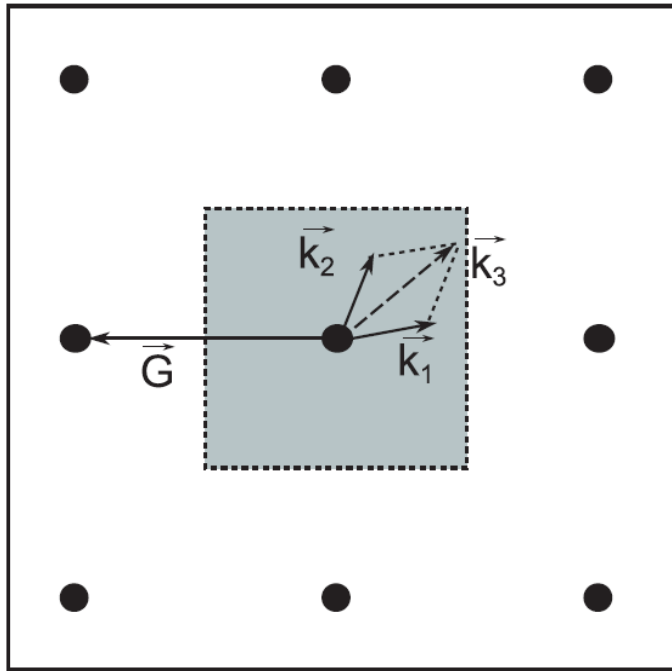
Heuristic spinon mean free path  
Spinons scatter on acoustic phonons

$$\frac{1}{\ell} \approx \frac{1}{\ell_d} + \frac{g^2}{a} \frac{T}{J} e^{-T^*/T}$$

Strong coupling



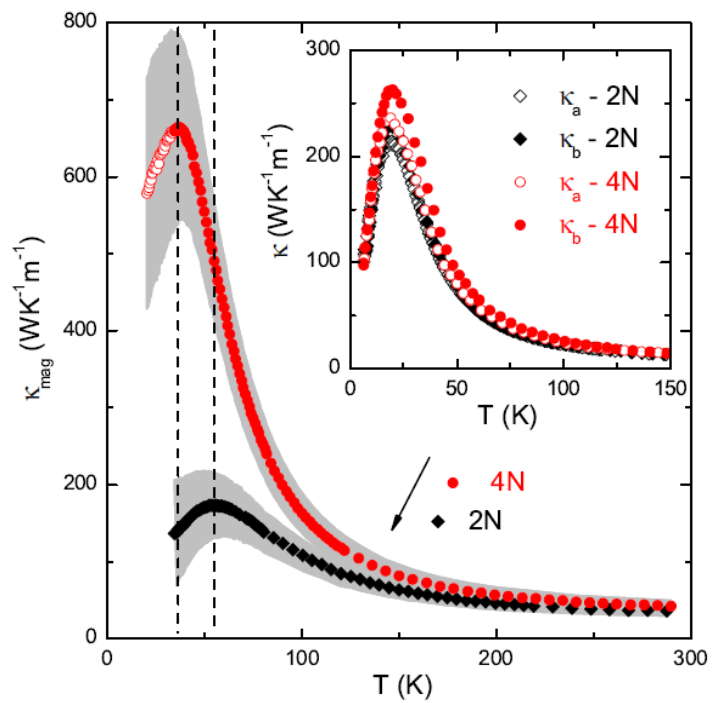
Spin Peierls  
(dimerization as in  
CuGeO<sub>3</sub>)



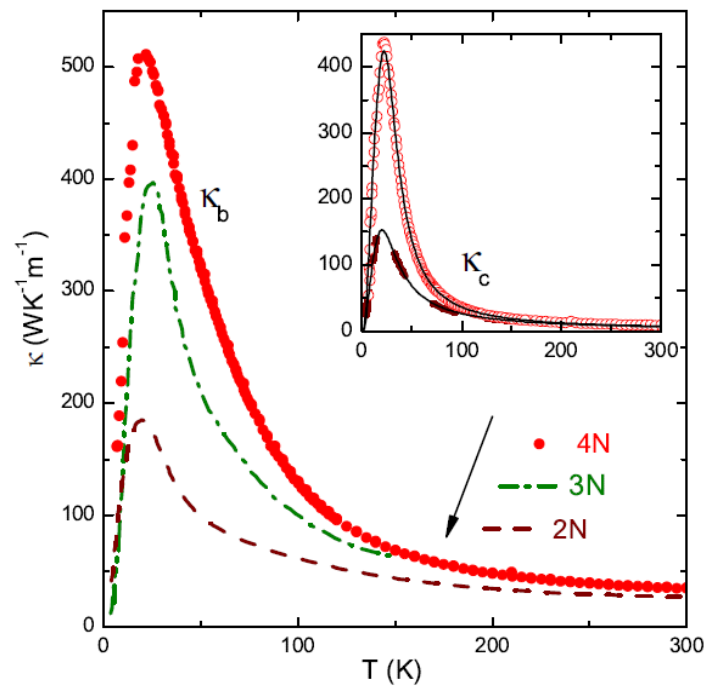
$$\hbar\omega_1 + \hbar\omega_2 = \hbar\omega_3$$

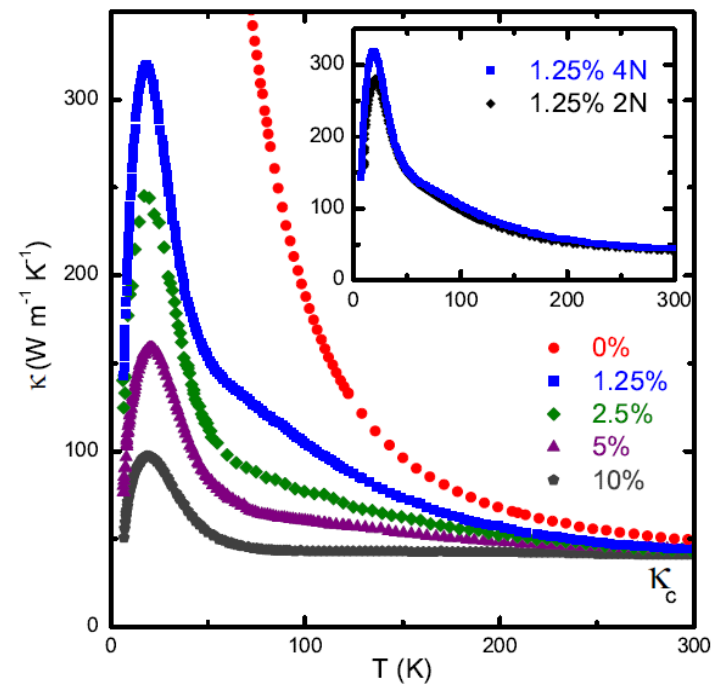
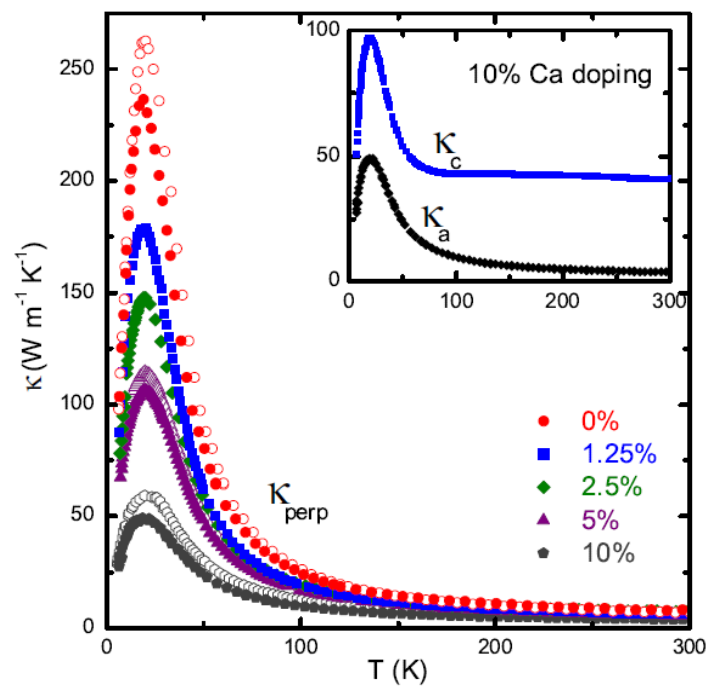
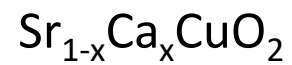
$$\vec{k}_1 + \vec{k}_2 = \vec{k}_3 + \vec{G}$$

$\text{SrCuO}_2$

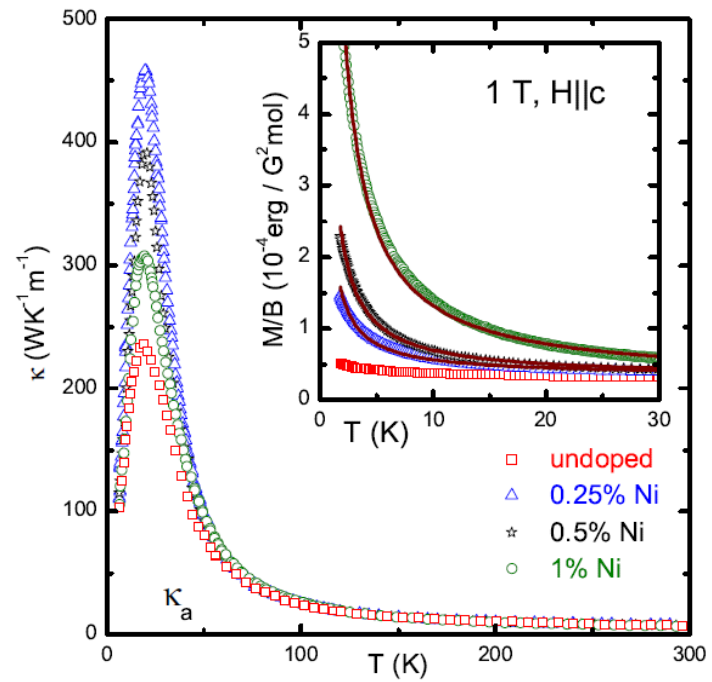
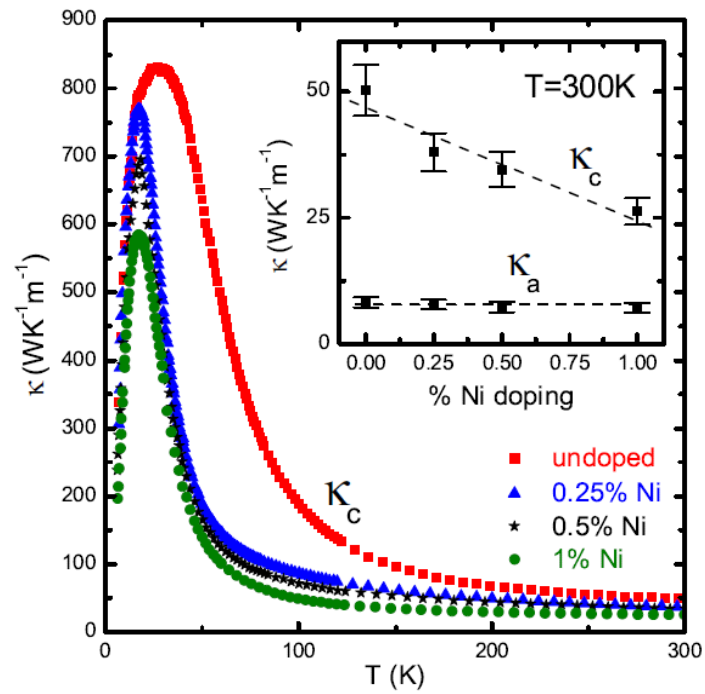


$\text{Sr}_2\text{CuO}_3$

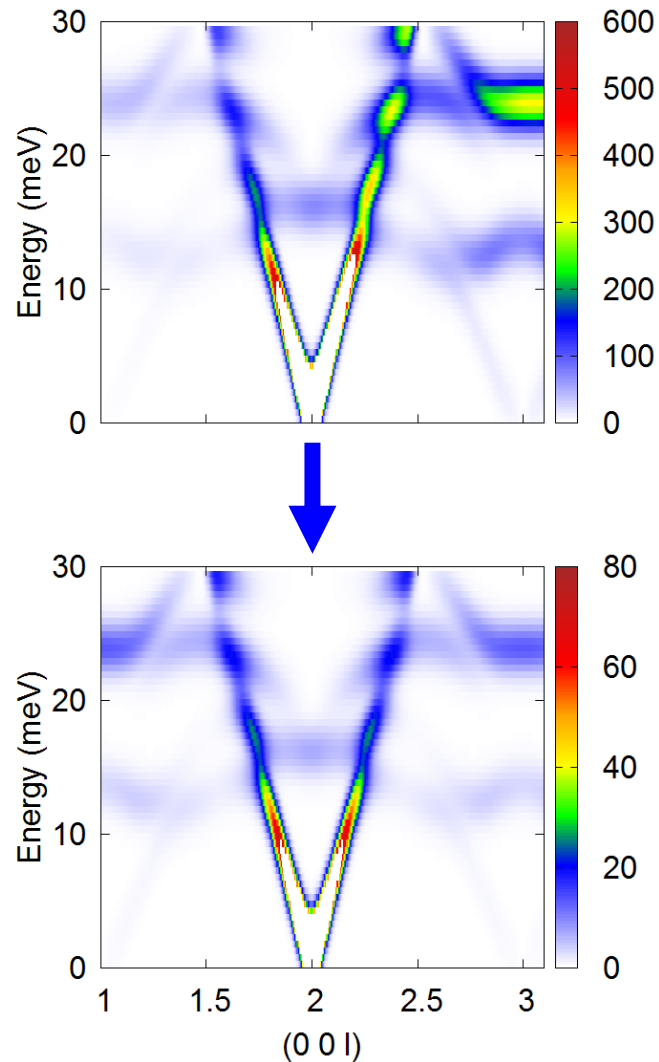




# SrCuO<sub>2</sub> doped with Ni (S=1 impurity)



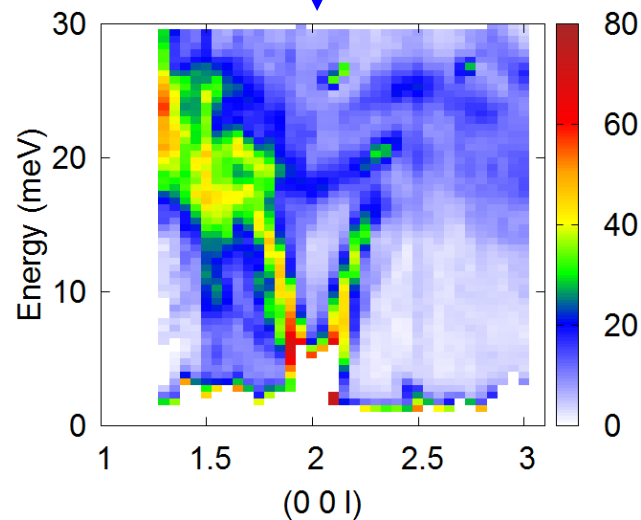
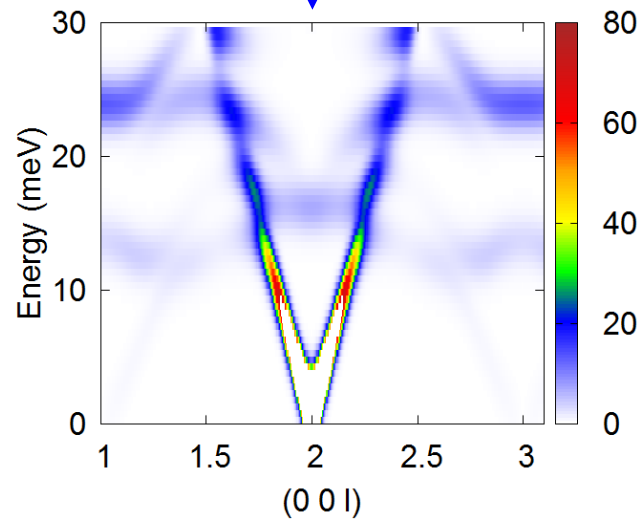
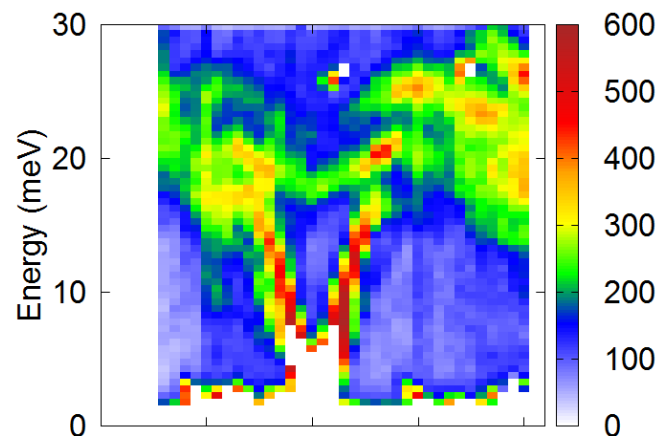
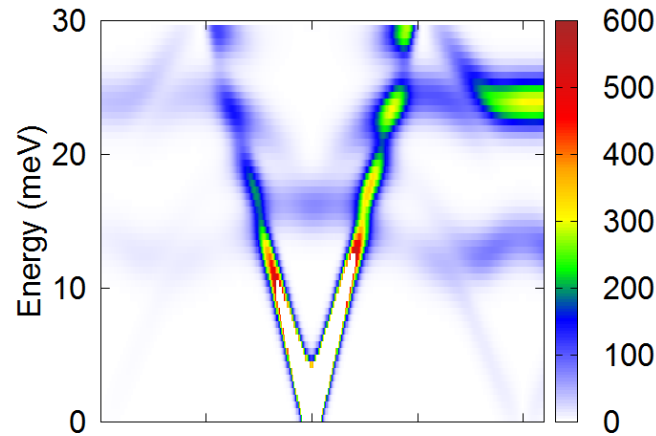
# Any effect ?



Correct the data for classical  $Q^2$  dependence and for the Debye-Waller :

$$\chi'' = \frac{I}{Q^2 e^{-W} [1 + n(\omega)]}$$

# Any effect ?



The spectral weight is anomalously strong at low  $Q$ .

Is it related to the magnetic form factor ?

No definitive conclusion